

KIVI Chair - Big Data Science Master Class

# Computer Graphics and Visualization

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10 November 2016

[Ritschel, Eisemann, Ha, Kim, Seidel - CGF 2011]

[Kehl, de Haan – Gi4DM 2012]

[Kroes, Post, Botha -PLoS ONE 2012]

## Introduction

- Computer Graphics has many applications
  - Architecture/Design
  - Engineering/Medical
  - Education
  - Movies
  - ...



## **Sensors everywhere...**

- **Big brother is measuring you...**

There will be a trillion (!) sensors within the next 5 years...

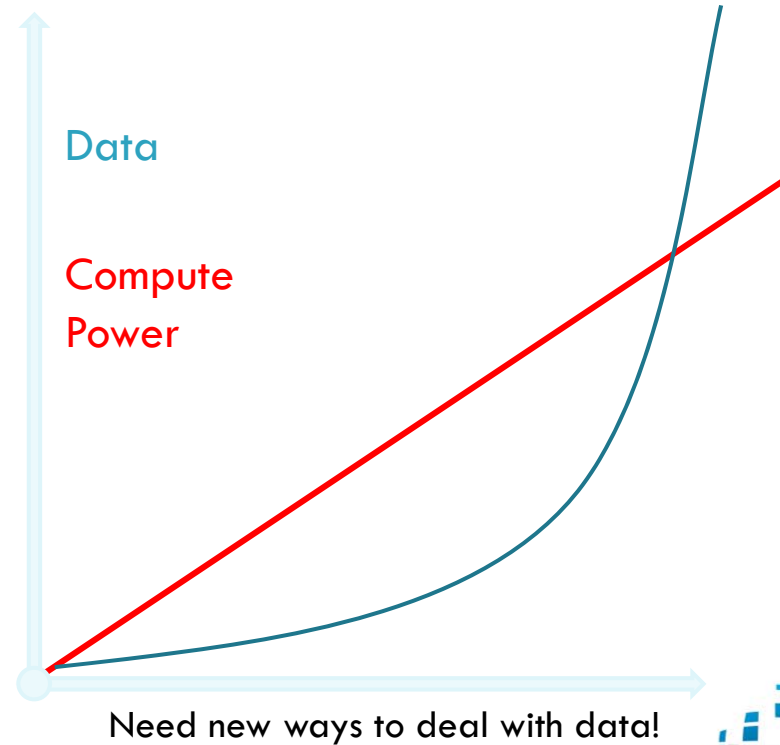
E.g., Google Earth already stores 21 Million Gigabytes

How can we make use of this data?



## Data Development

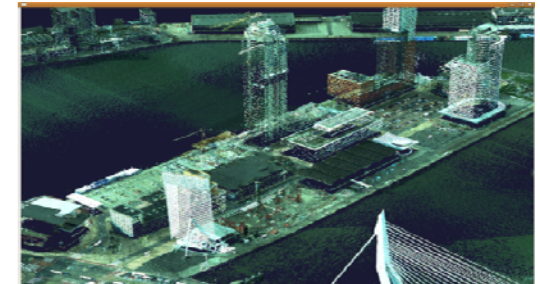
- **Processing**
- **Analysis**
- **Interaction**
- **Visualization**
- **Guidance**



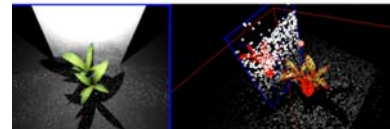
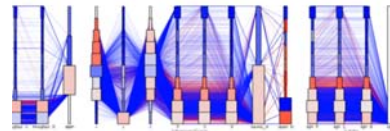
# Modern Visualization Systems

Very complex:

- Large-scale Data Handling
- Effective Illustrations
- Responsive Interactivity
- Analysis Solutions



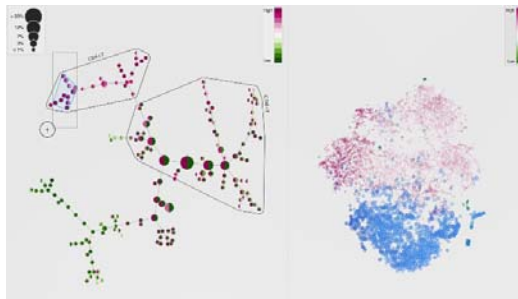
Massive 3D Pointclouds



Light-Transport Analysis



Flooding Simulation



Cell-type Analysis



Volume Rendering



Multi-touch Data Mining

## What topics to cover? ...

>20 topics in 3h...

- Realistic Rendering
- Graphics in Data Visualization
- Aesthetic imagery
- Human perception
- Real-time processing
- Real-time large-scale data rendering
- Compression
- Multi-dimensional data
- Analysis (with Machine Learning Components)
- Basic graphics approaches
- Aeronautics
- Object Simplification
- User experience/Interaction
- Solutions used in practice
- Collision Detection
- Fabrication
- Geoscience ...



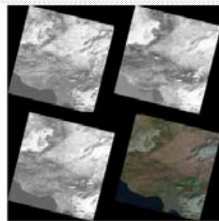
# Effective Data Visualization Requires



- **Large-Scale Rendering**



- **Visualization and Perception**



- **Data Analysis**

## Large-Scale Rendering

- Ray Tracing
- Graphics Pipeline
- Specialized Methods for Different Data Types
  - Height-Field Data, Voxel Data, Data Management, Compression



# Visualization and Perception

- Realistic Rendering
- Perceptual Methods
- Visualization & Interface



## Data Analysis

- High-dimensional/Heterogeneous Data
- Dimensionality Reduction
- Visual Analytics



## Large-Scale Rendering

- Ray Tracing
- Graphics Pipeline
- Specialized Methods for Different Data Types
  - Height-Field Data, Voxel Data, Data Management, Compression



## How to produce an image?

- Computers can only calculate...

Well, what do you expect when you just tell me "10101001101..."



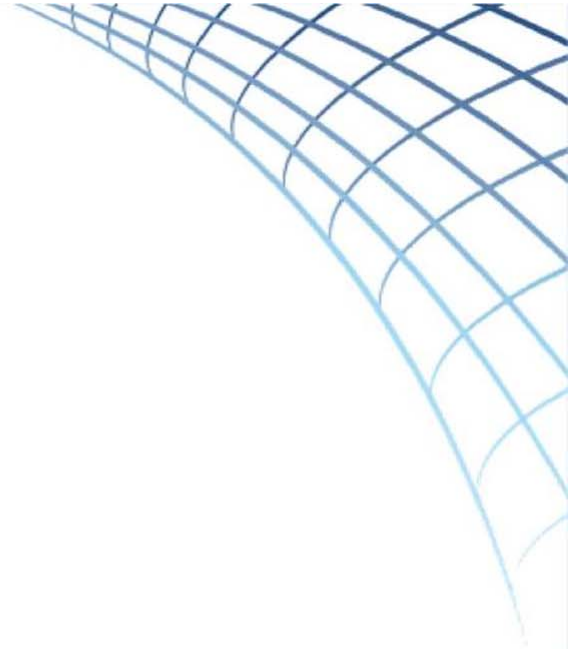
You just don't understand me...



# Making images with a Computer



**Pixel**



## Pixels – Picture elements

- A colored pixel has typically  
Red Green Blue values.

123

- We color by numbers...  
sounds simple...  
but choosing the values can be difficult

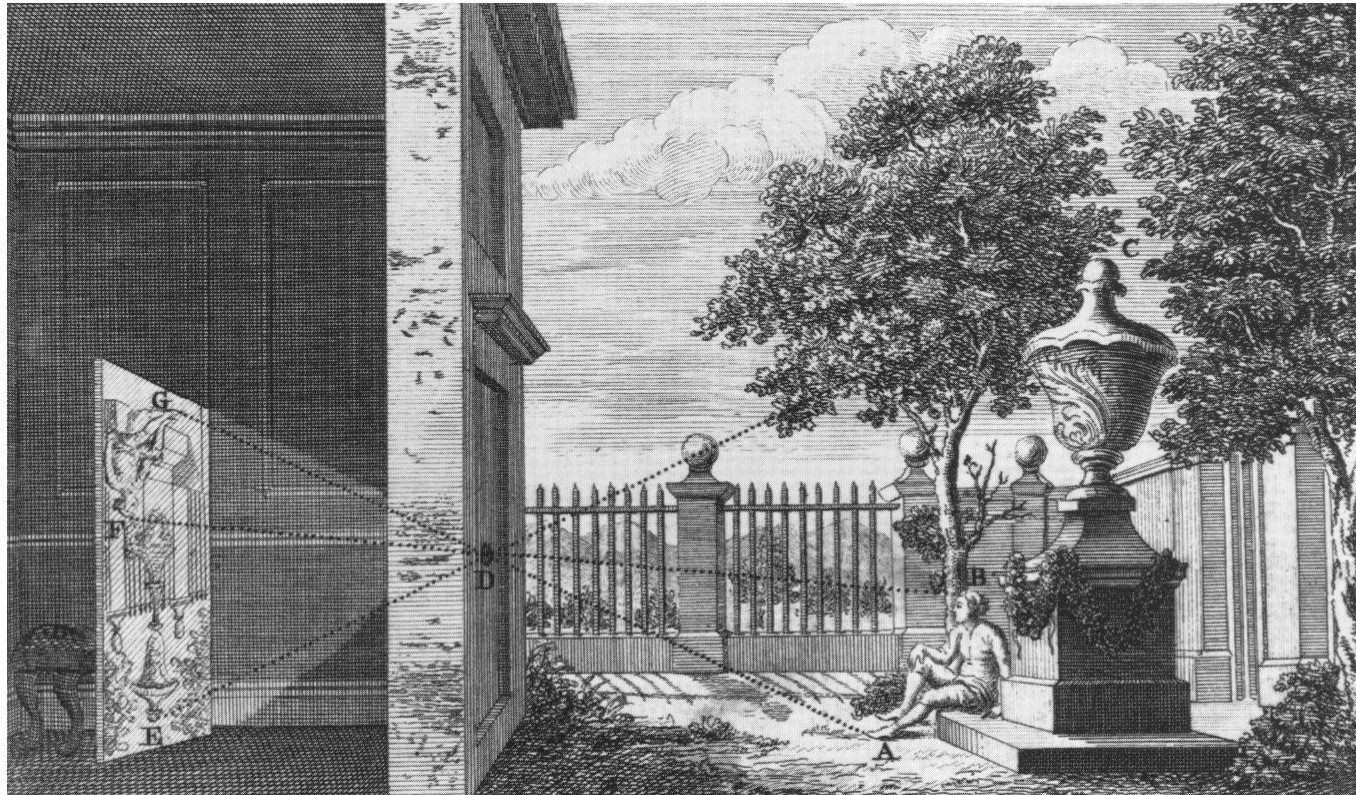


# Producing Images in the Real World





## Producing Images in the Real World



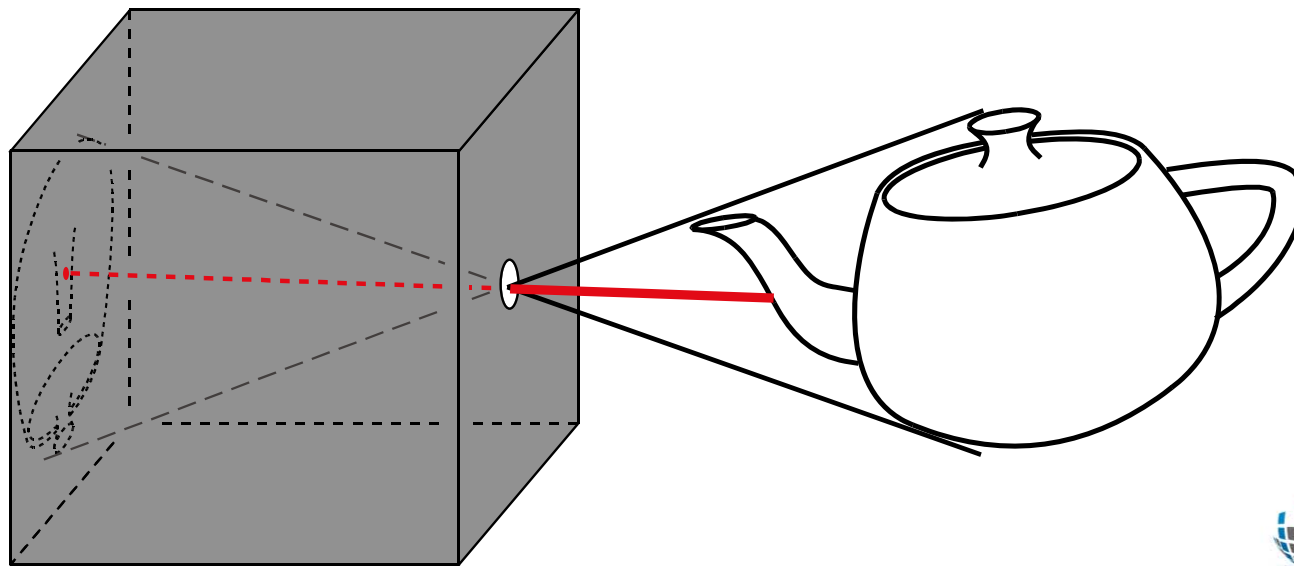
Camera obscura



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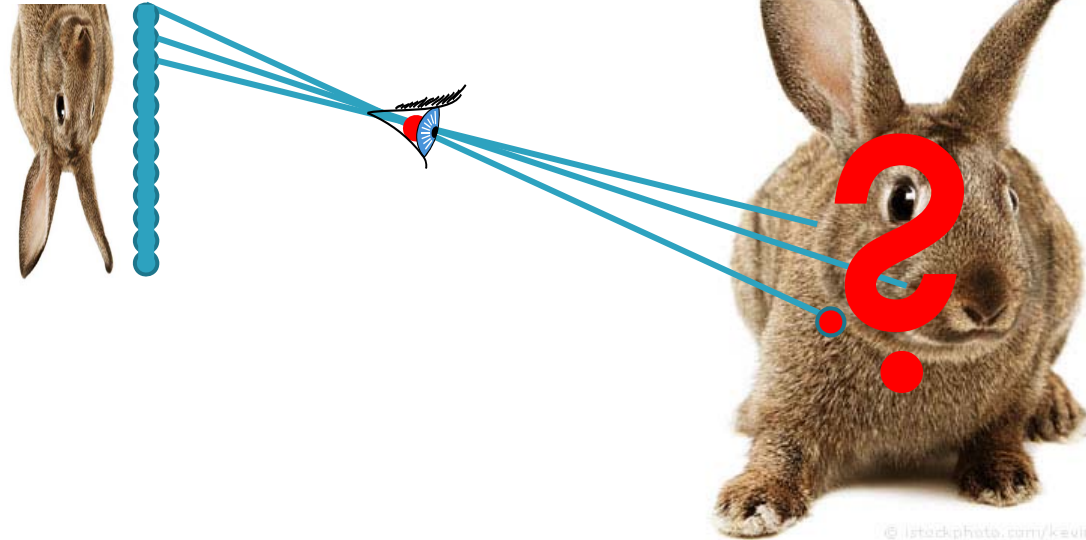
## Pinhole camera

- Box with hole
- Perfect image for "point-sized" hole



## Virtual Camera

- Take a pixel on the image in the virtual world
- Compute ray through pixel and camera center
- Intersect ray with scene [?]

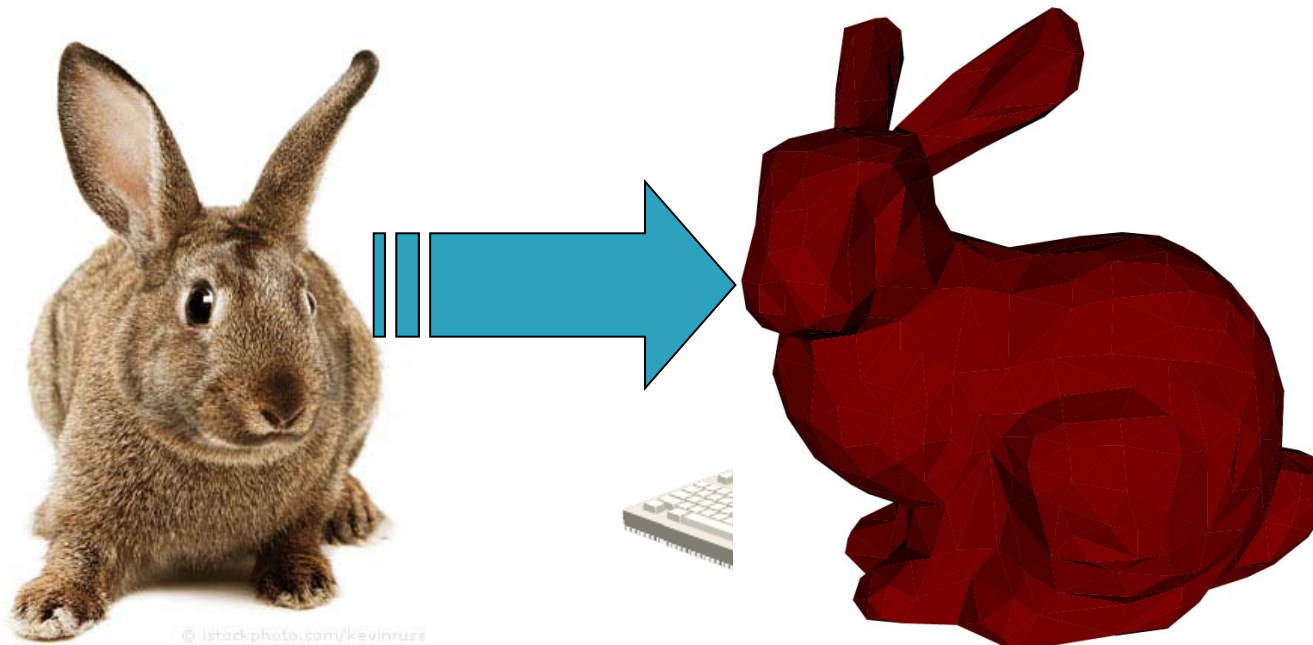


© iStockphoto.com/kevinruzz

**DELFT  
DATA  
SCIENCE**

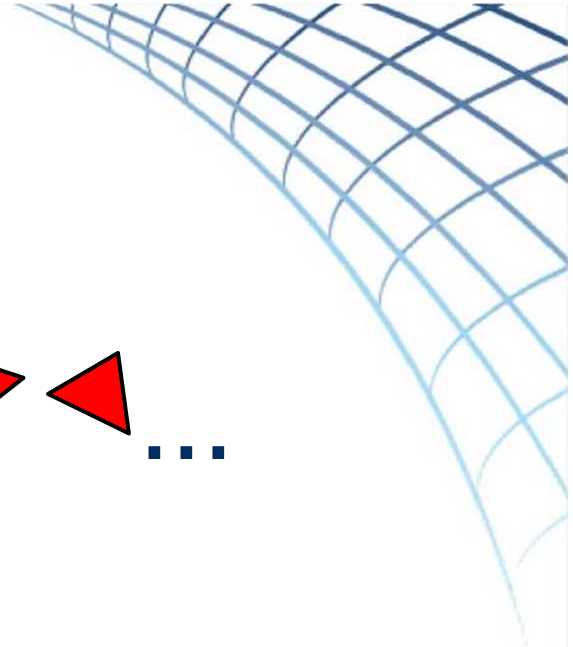
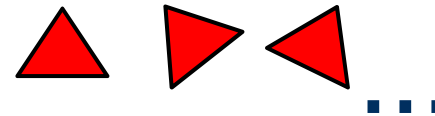
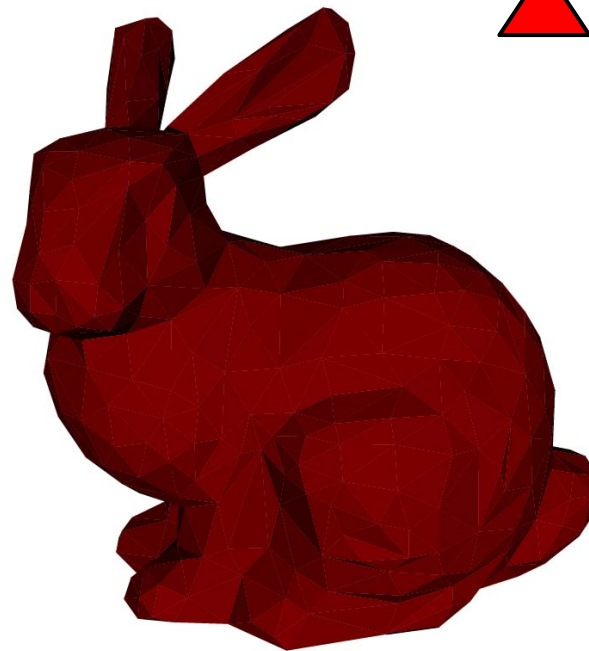
## Models

- Representing reality



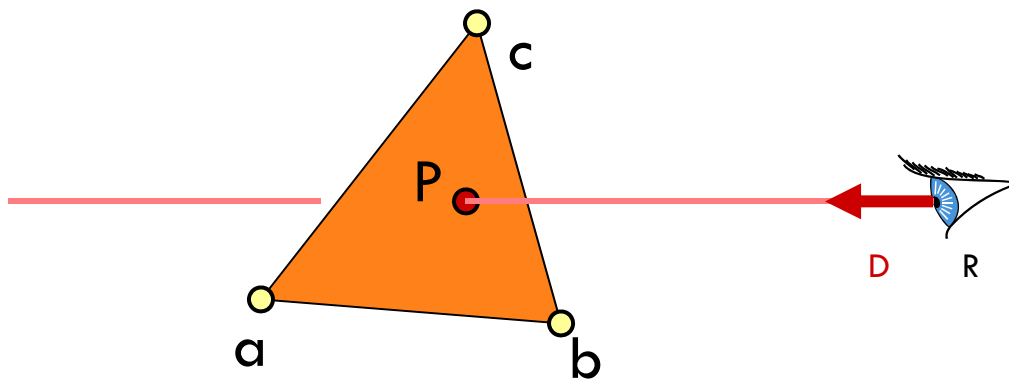
## Models

- Models are typically lists of **triangles**



## Solve Equations

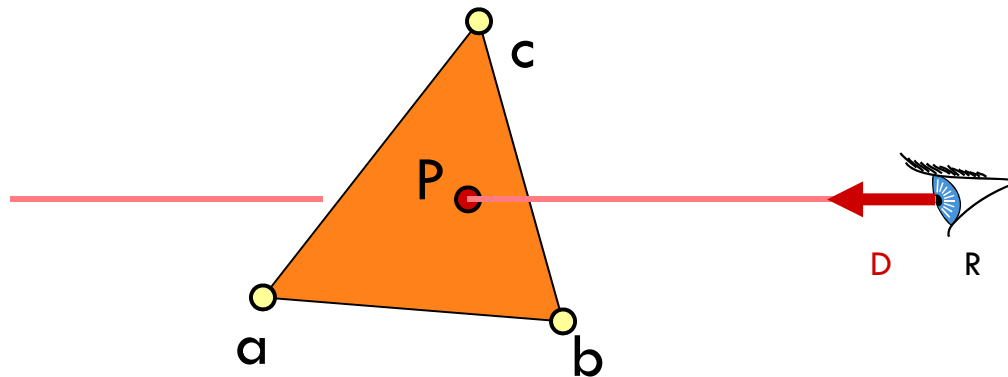
- $R+tD= a+\beta (b-a)+\gamma (c-a)$



## Solve Equations

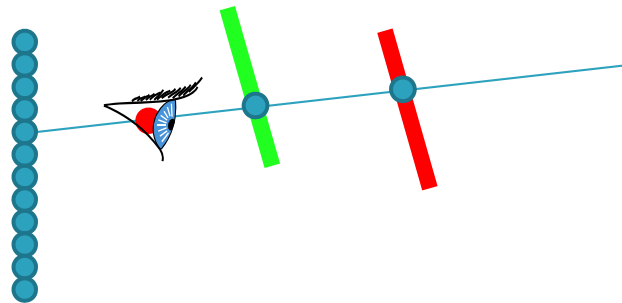
- $R_x + tD_x = a_x + \beta(b_x - a_x) + \gamma(c_x - a_x)$
- $R_y + tD_y = a_y + \beta(b_y - a_y) + \gamma(c_y - a_y)$
- $R_z + tD_z = a_z + \beta(b_z - a_z) + \gamma(c_z - a_z)$

$$\begin{bmatrix} a_x - b_x & a_x - c_x & D_x \\ a_y - b_y & a_y - c_y & D_y \\ a_z - b_z & a_z - c_z & D_z \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} a_x - R_x \\ a_y - R_y \\ a_z - R_z \end{bmatrix}$$



## Produce Final Image

- Keep the closest intersection point





## Ray Tracing - Recap

For each pixel

Distance=MAX

Color=0

Ray=computeRay(pixel)

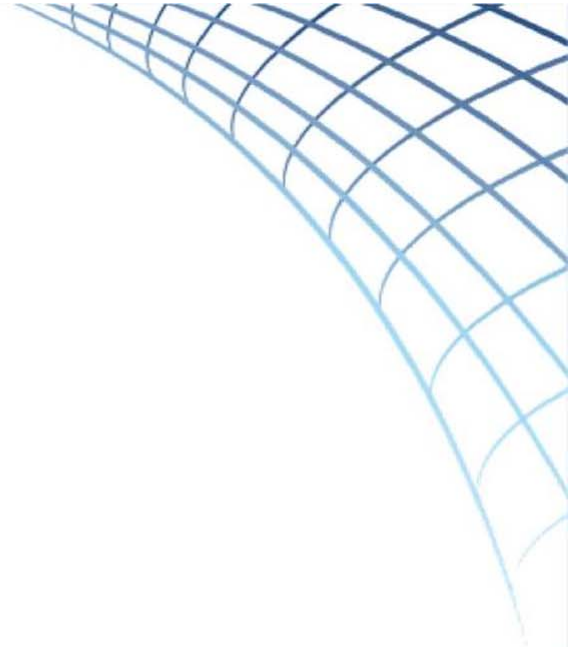
For each triangle

(CurrColor,CurrDistance)=computeIntersection(Ray)

If (CurrDistance<Distance)

Distance=CurrDistance

Color=CurrColor



## Ray Tracing - Cost

For each pixel

Distance=MAX

Color=0

R=computeRay(pixel)

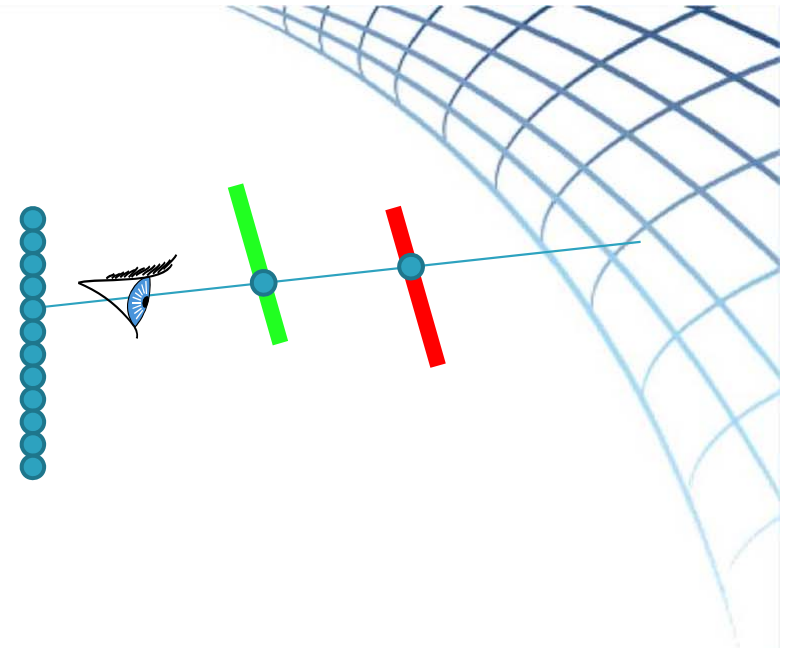
For each triangle

(CurrColor,CurrDistance)=testIntersection(R)

If (CurrDistance<Distance)

Distance=CurrDistance

Color=CurrColor



## Performance Analysis

- **Stupid** implementation:
- Ray Tracing:  
Cost = Pixels \* Triangles

e.g., **100.000** triangles and a **1000<sup>2</sup>** screen:

Raytracing:  $100.000 * 1.000.000 = 10^{11}$



## Performance Analysis

- **Smart** implementation:
- Ray Tracing:

$$\text{Cost} = \text{Pixels} * \log(\text{Triangles})$$

→ + building a structure

e.g., **100.000** triangles and a  $1000^2$  screen:

$$\text{Raytracing: } 1.000.000 * 5 + \text{X} = 5 * 10^6$$

Especially suitable for static data

## What about real-time (30 Images/Sec)

“building a structure” is generally slow

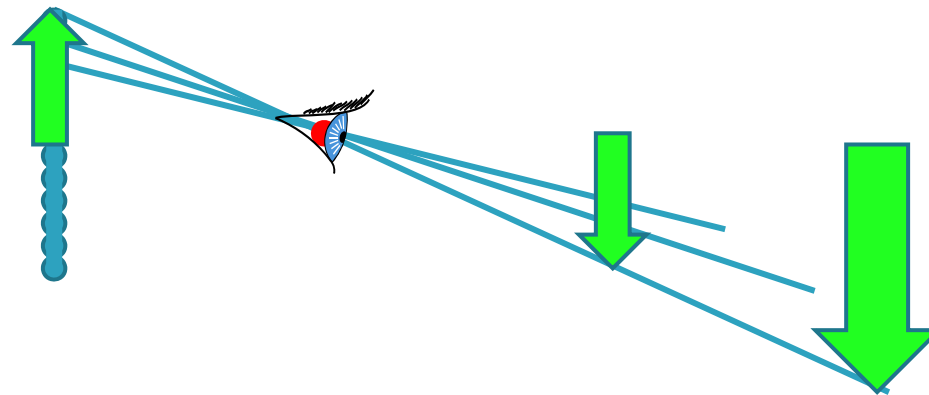
Alternative approach:

Rasterization via the Graphics Pipeline



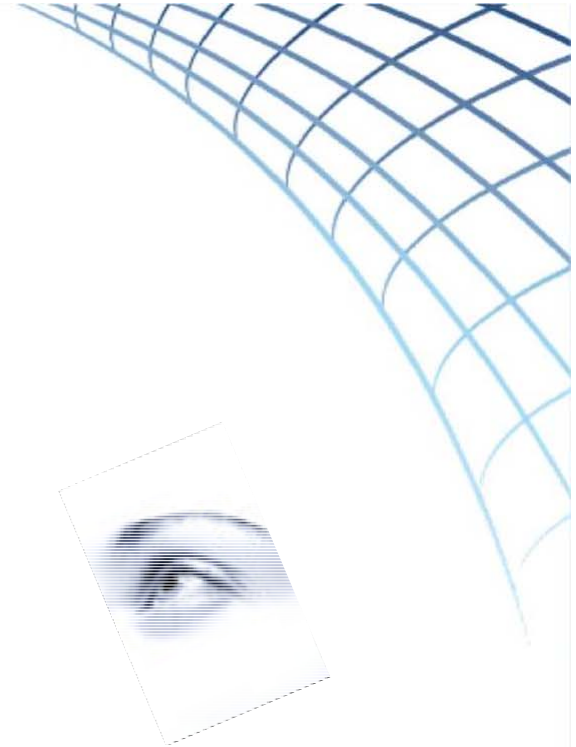
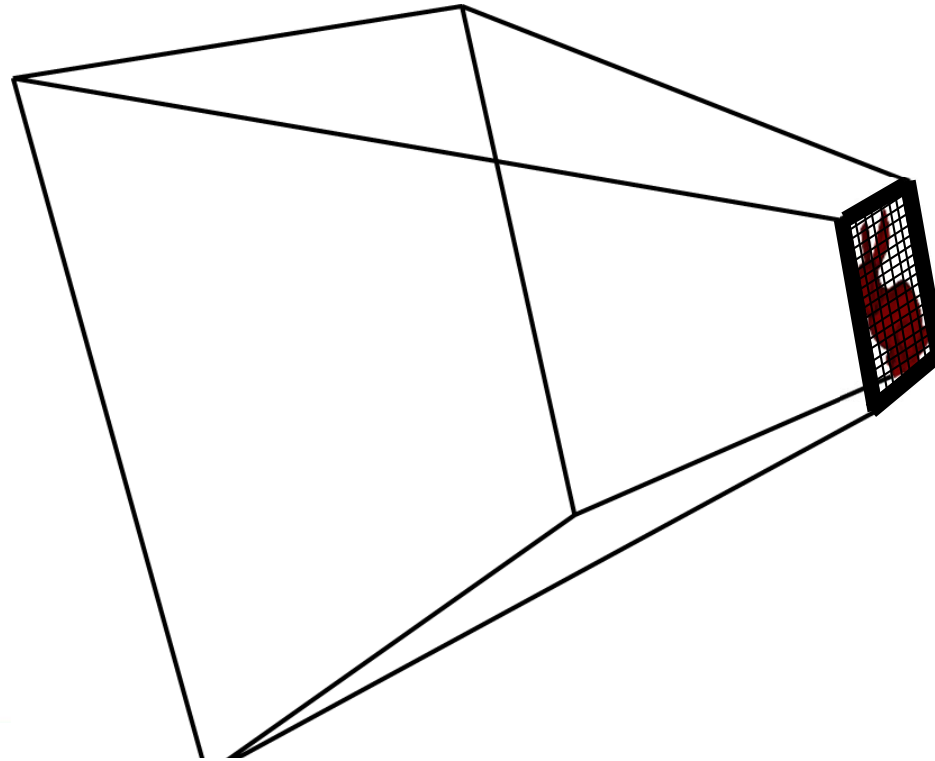
## Virtual Camera

- Camera Plane in front of the eye



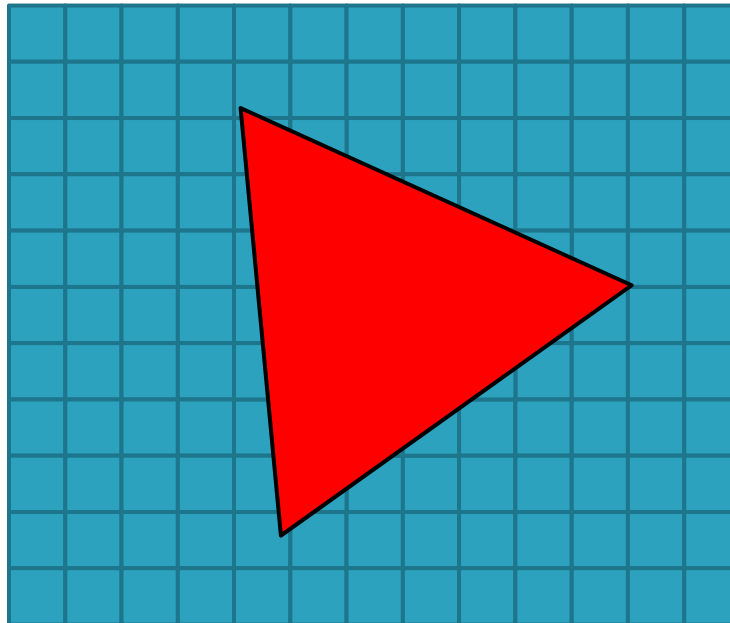
# Simplified Graphics Pipeline

- **Projection:** Transform coordinates to screen



# Simplified Graphics Pipeline

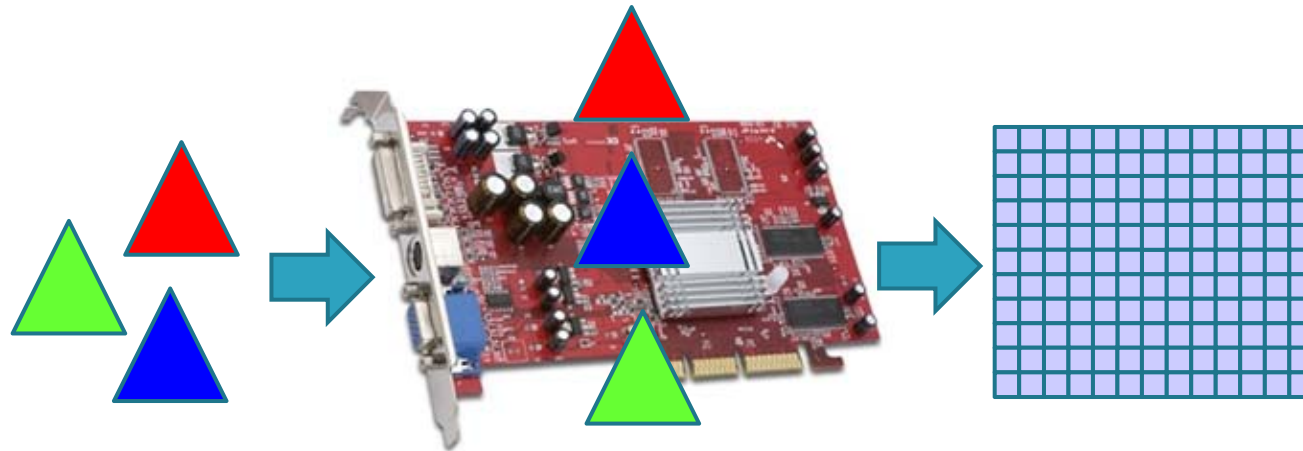
- **Rasterization:** Fill screen pixels





# Simplified Graphics Pipeline

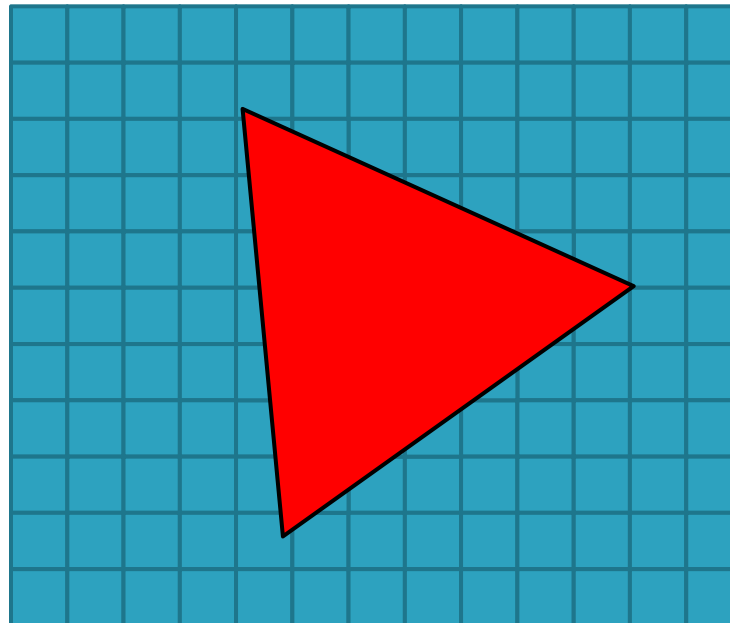
- Highly parallelizable → GPUs



Thousands of processors working in parallel

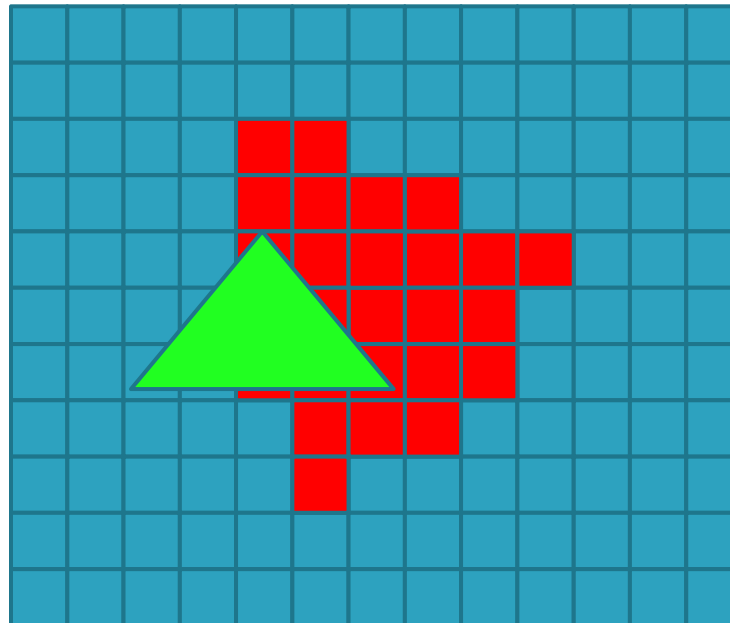
# Simplified Graphics Pipeline

- **Catch:** Let's look at a second triangle...



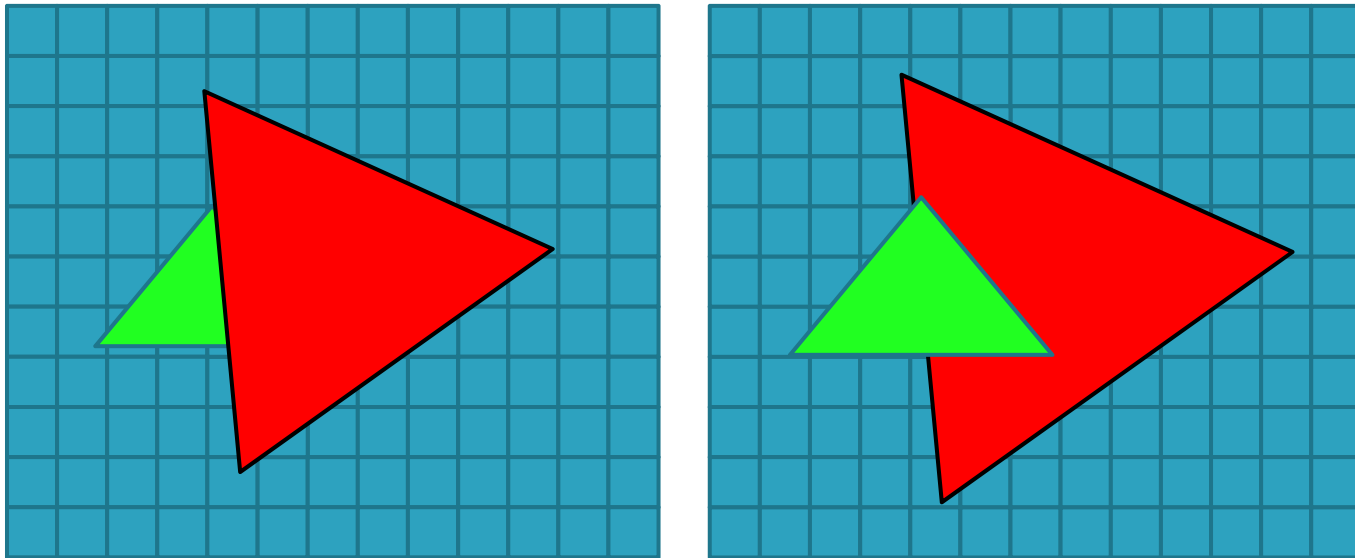
# Simplified Graphics Pipeline

- **Catch:** Let's look at a second triangle...



# Simplified Graphics Pipeline

- **Catch:** Triangle drawing order changes result

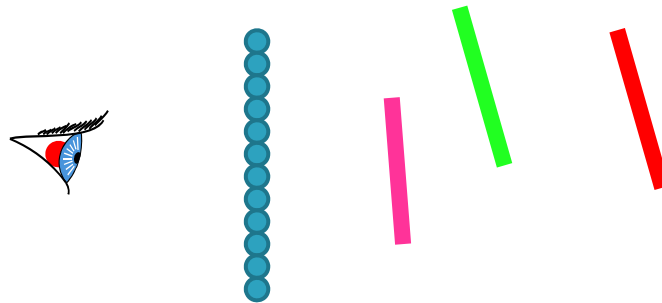


As for ray tracing: need the closest triangle

[Catmull74] , [Strasser74]

# Simplified Graphics Pipeline

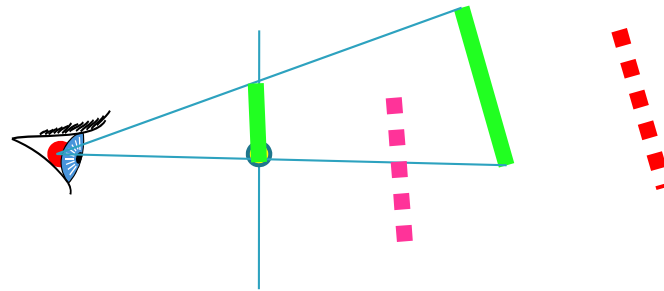
- **Depth Buffer:** Avoid sorting triangles!
- Store a color and **depth** in each pixel



[Catmull74] , [Strasser74]

# Simplified Graphics Pipeline

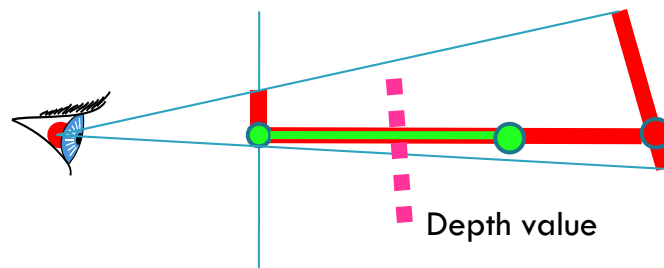
- **Depth Buffer:** Avoid sorting triangles!
- Store a color and **depth** in each pixel



[Catmull74] , [Strasser74]

# Simplified Graphics Pipeline

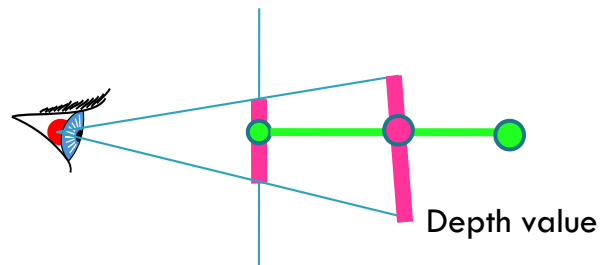
- **Depth Buffer:** Avoid sorting triangles!
- Store a color and **depth** in each pixel



[Catmull74] , [Strasser74]

# Simplified Graphics Pipeline

- **Depth Buffer:** Avoid sorting triangles!
- Store a color and **depth** in each pixel

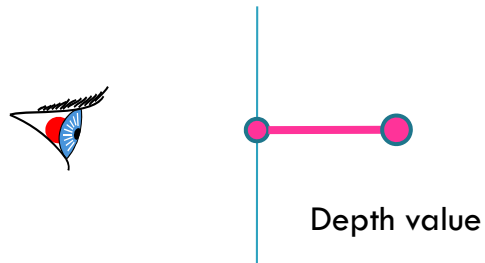




[Catmull74] , [Strasser74]

# Simplified Graphics Pipeline

- **Depth Buffer:** Avoid sorting triangles!
- Store a color and **depth** in each pixel



## Depth Buffering [1974]

But was applied much later... Why?

Memory requirements

320x200 pixel -> 200 KB of memory !

2000x1000 pixel -> 6 MB of memory !

1974 : \$314,573 /MB

1986 : \$ 300 /MB

1993 : \$28 /MB (Nvidia)



## Cost of Rasterization

Algorithm:

For each triangle

    projTri=projectTriangle(triangle)

    fillPixels(projTri)

Cost = Triangles + “drawn pixels”



## Performance Analysis

Ray Tracing:

$$\text{Cost} = \text{Pixels} * \log(\text{Triangles}) + \text{structure}$$

vs.

Rasterization:

$$\text{Cost} = \text{Triangles} + \text{"drawn pixels"}$$

e.g., 100.000 triangles and a  $1000^2$  screen:

$$\text{Raytracing: } X+5 * 1.000.000$$

$$\text{Rasterization: } 100.000 + \text{"drawn pixels"}$$

$$\text{Raytracing/Rasterization time: } \sim 50$$



## Performance Analysis

Ray Tracing:

$$\text{Cost} = \text{Pixels} * \log(\text{Triangles}) + \text{structure}$$

vs.

Rasterization:

$$\text{Cost} = \text{Triangles} + \text{"drawn pixels"}$$

e.g., 100.000.000 triangles and a 1000<sup>2</sup> screen:

$$\text{Raytracing: } X+8 * 1.000.000$$

$$\text{Rasterization: } 100.000.000 + \text{"drawn pixels"}$$

$$\text{Raytracing/Rasterization time: } \sim 0.1$$

... but Rasterization can be made smarter too...



## What complexity do we work with?

- Today's Games:
  - 200.000 triangles
- Today's Movies
  - more than 1 Billion



## Movie Rendering Costs

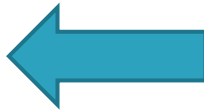
**> 1000 hours!**

Big Hero Six – copyright Disney



## What complexity do we work with?

- Today's Games:
  - 200.000 triangles



**Designed** for optimality

Often real-world data



- Visualization Systems:
  - Millions of Data points
  - Potentially summarizing much more information

- Today's Movies
  - more than 1 Billion



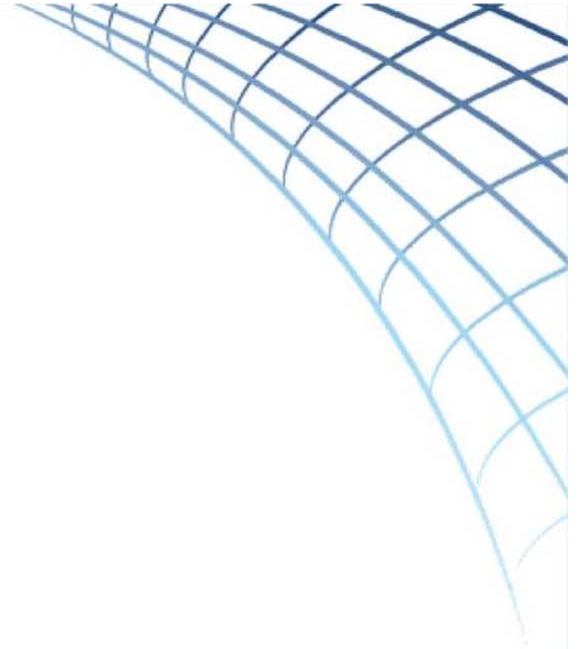
**Designed** for artistic look

For large-scale data display, we need to mix rendering strategies



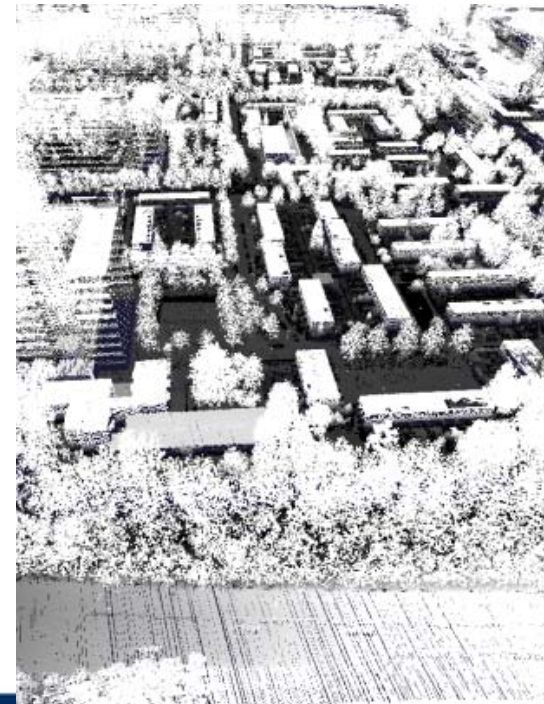
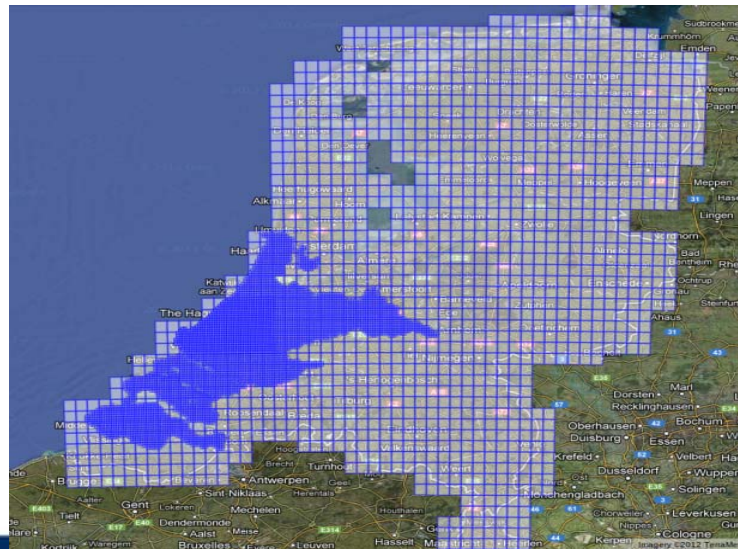


**Questions?**



## Scanned Data Sets

- AHN2 dataset with satellite imagery ~8 TB of data



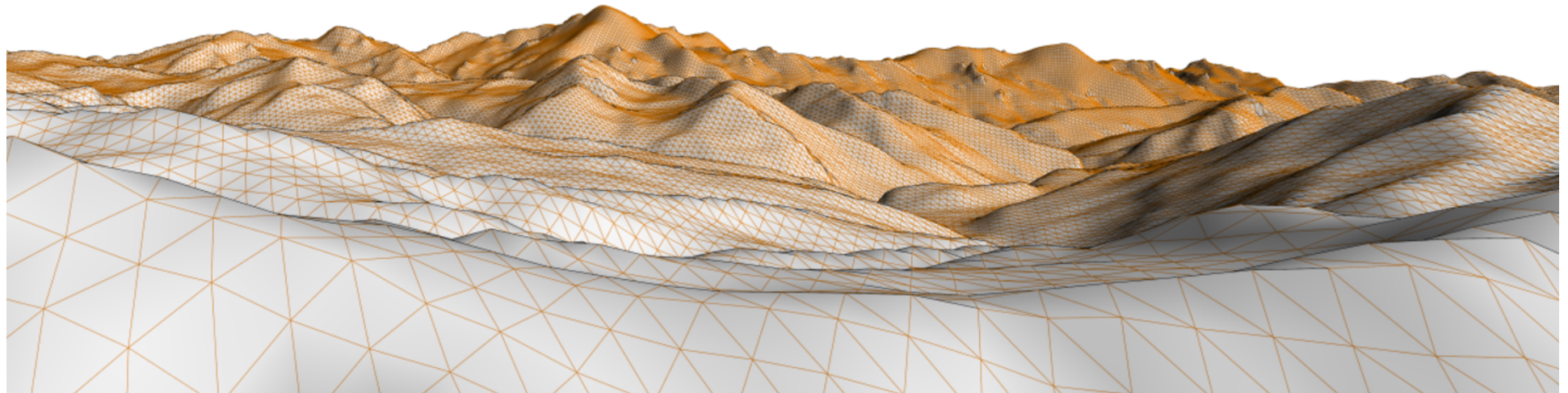
**DELFT  
DATA  
SCIENCE**

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## Scanned Data Sets

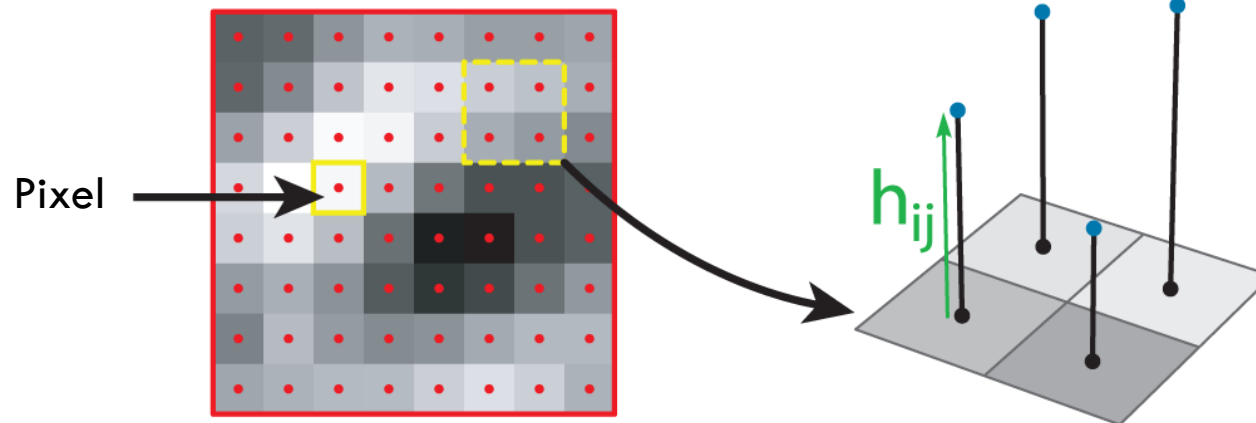


# Height-field Representation

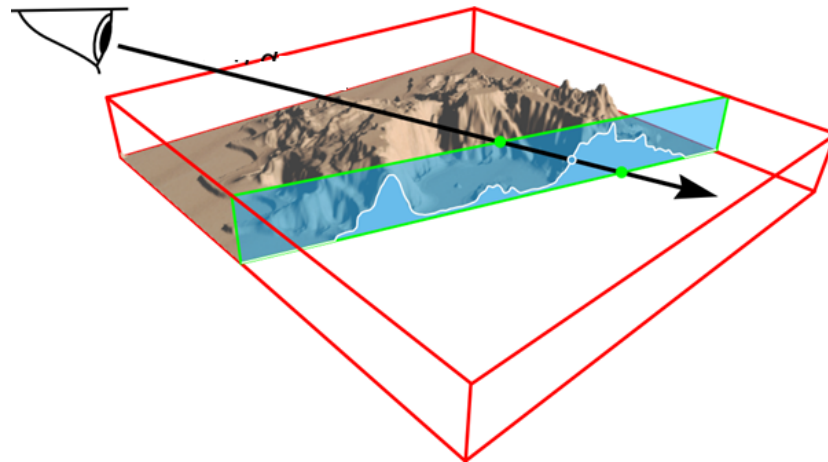


## Height-field Representation

- Storage in form of an 2D image with height per pixel

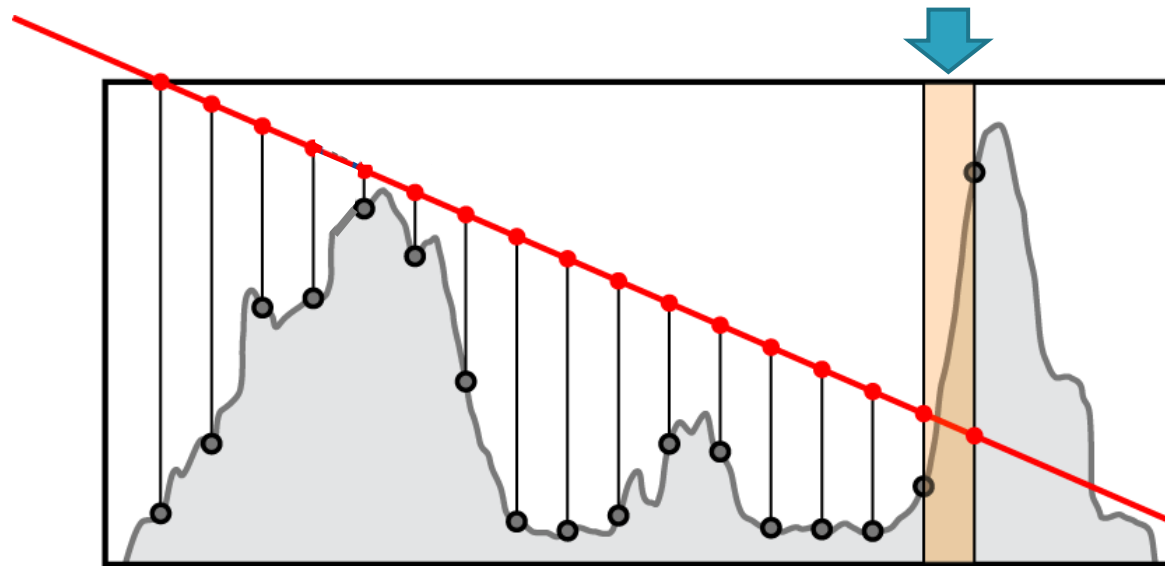


# Height-Field Rendering

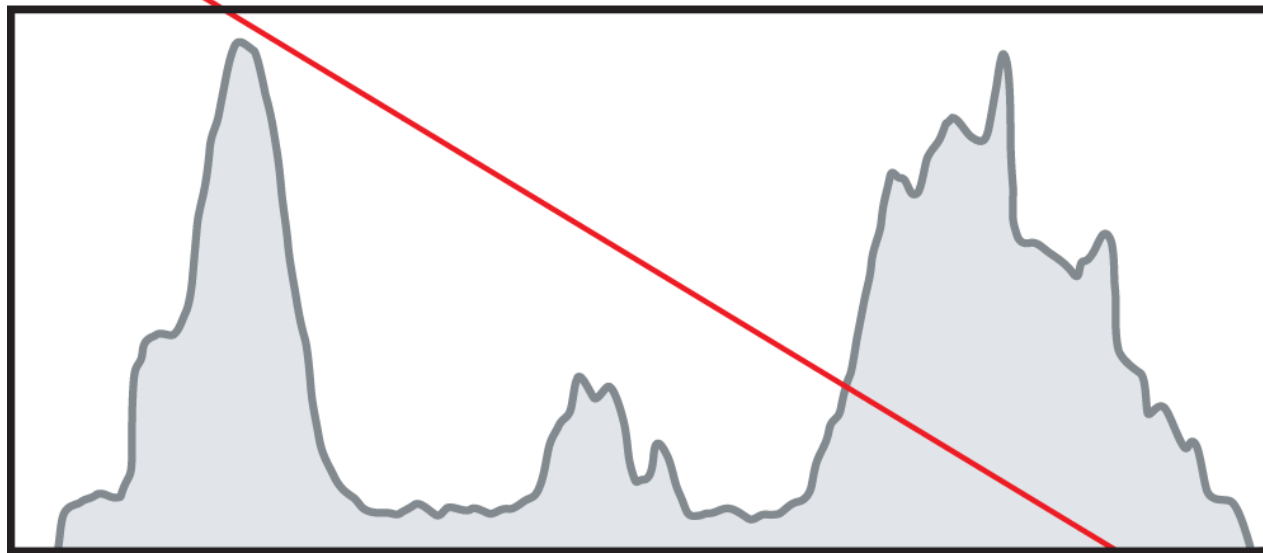


## Traditional Height-Field Rendering

- Many steps necessary and limited precision

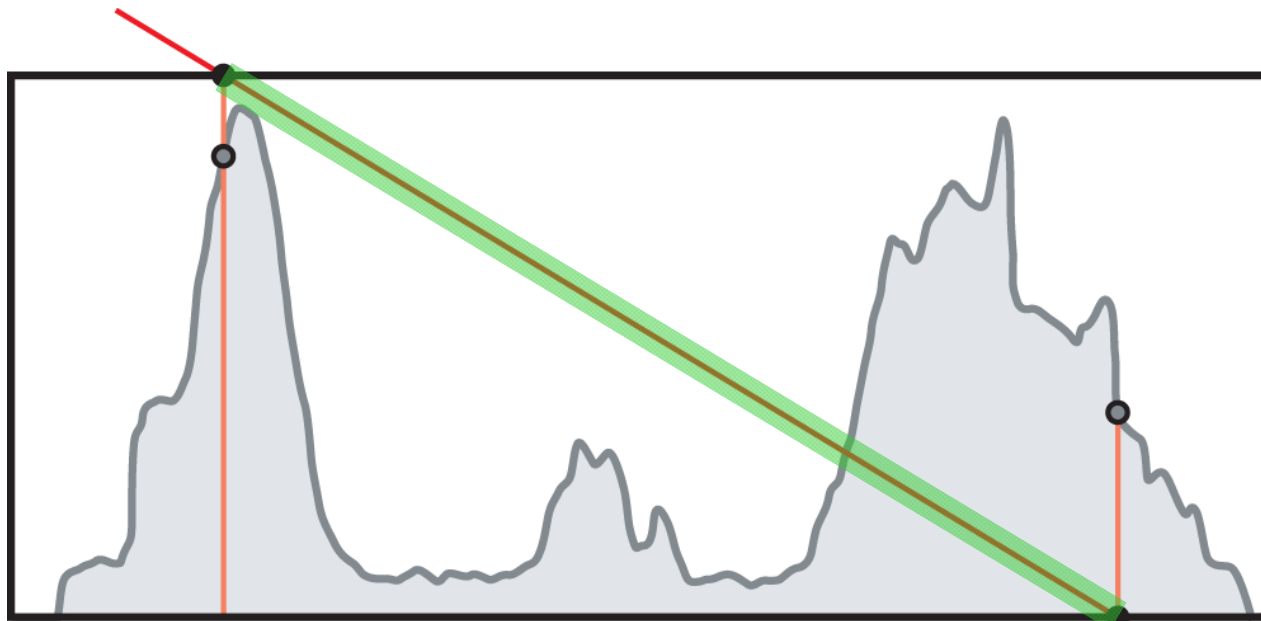


# Intersection Algorithm

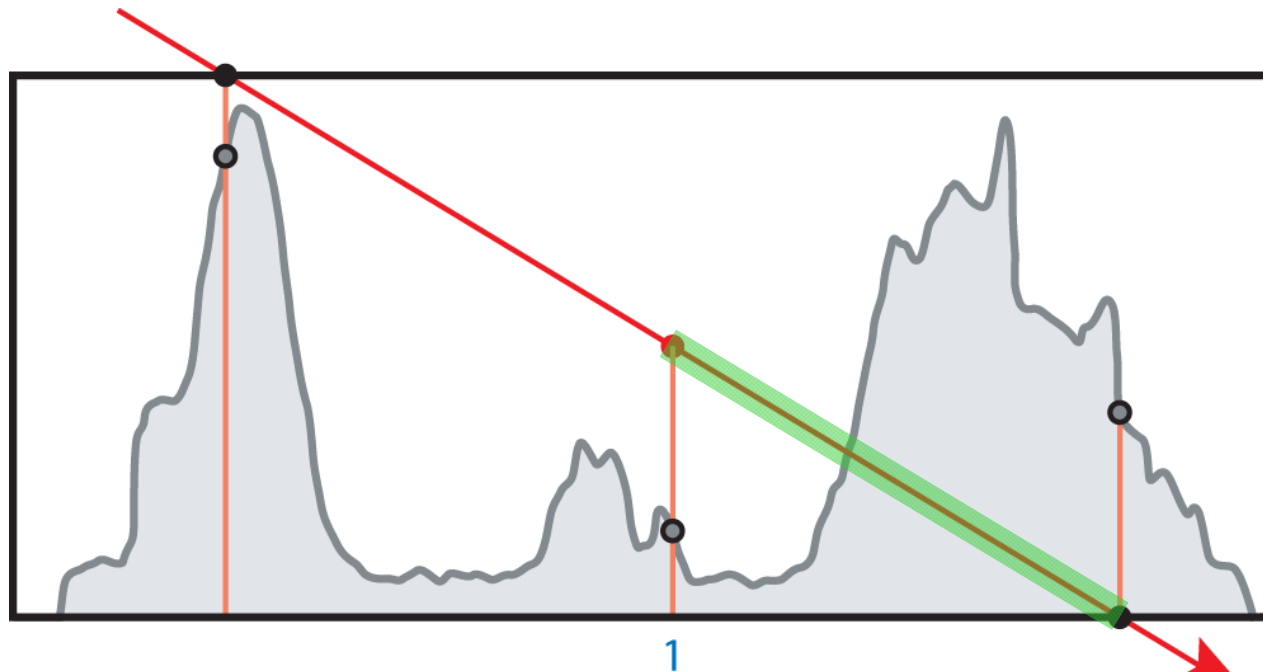




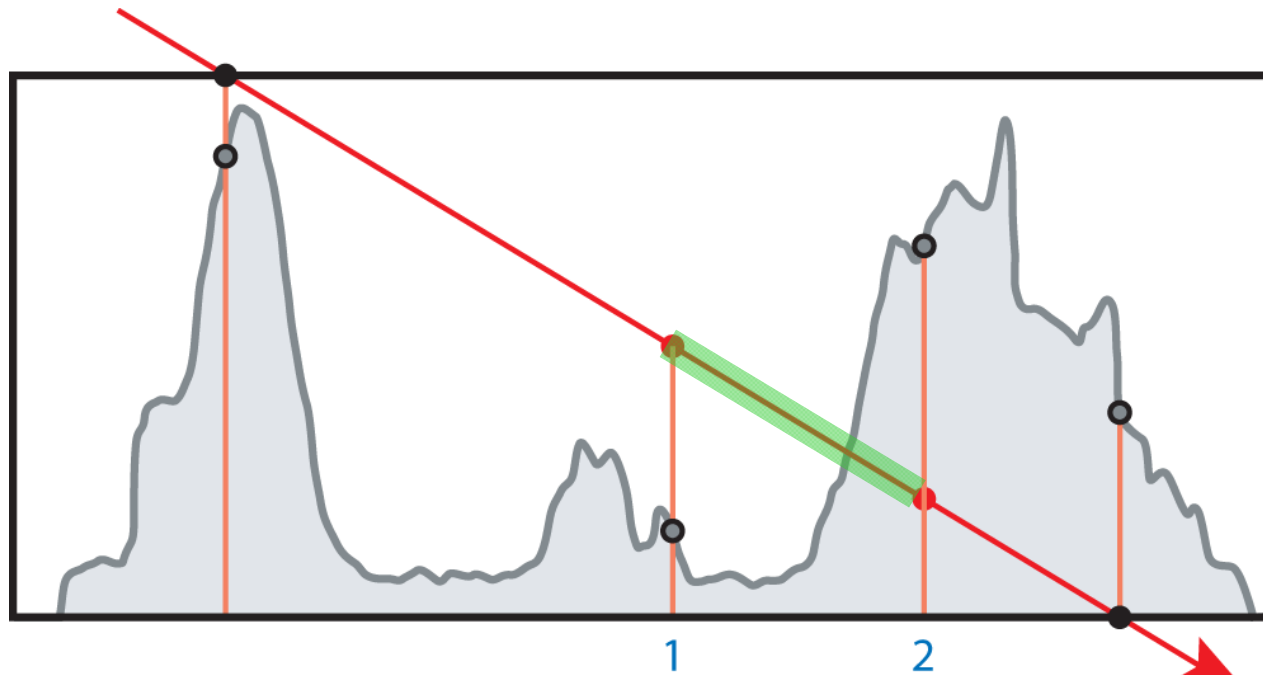
# Intersection Algorithm



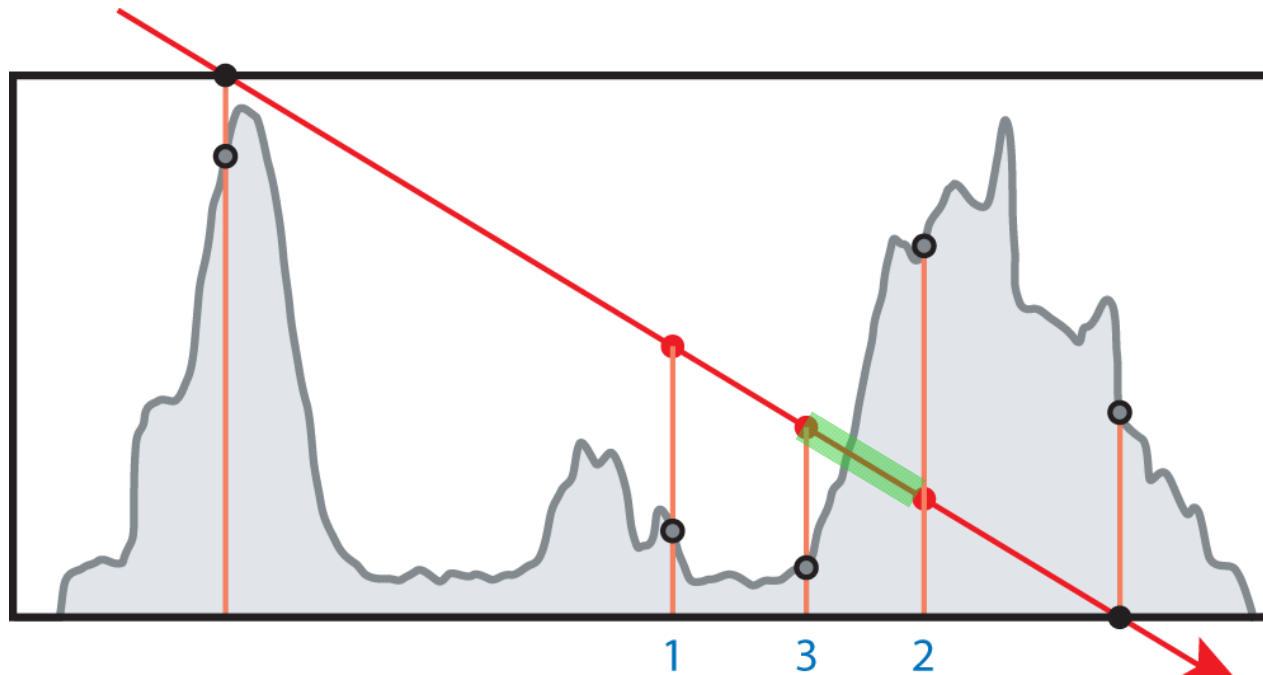
# Intersection Algorithm



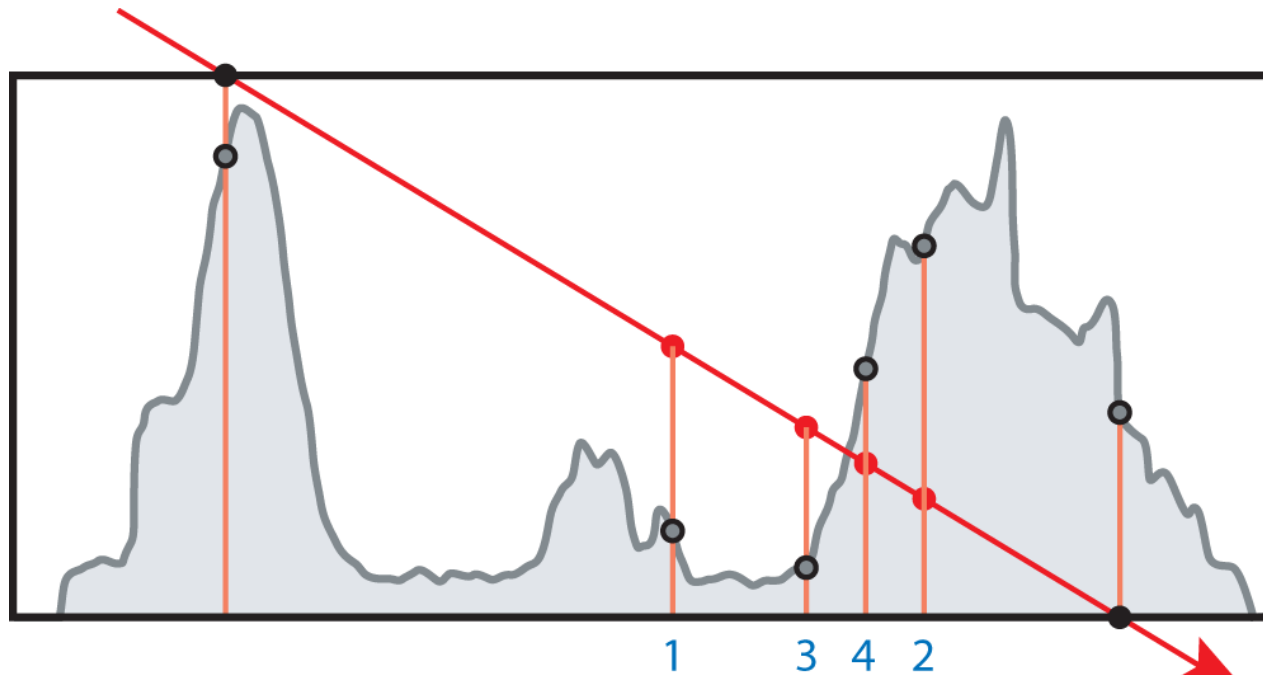
# Intersection Algorithm



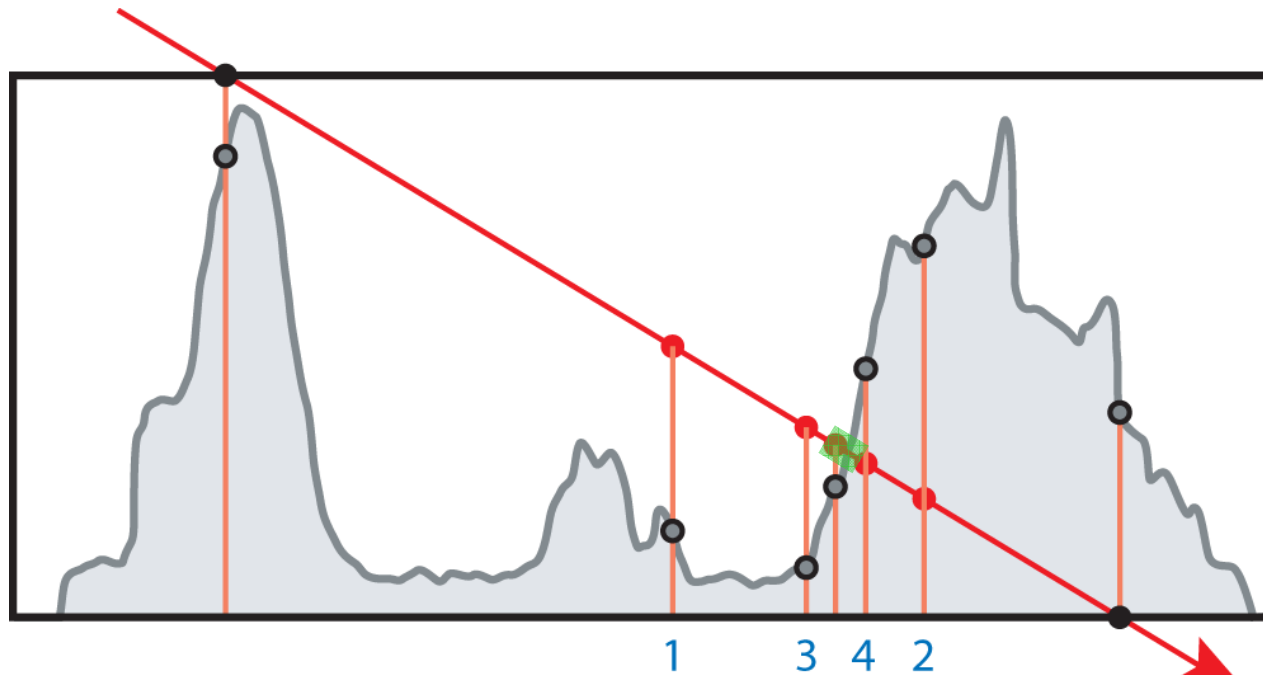
# Intersection Algorithm



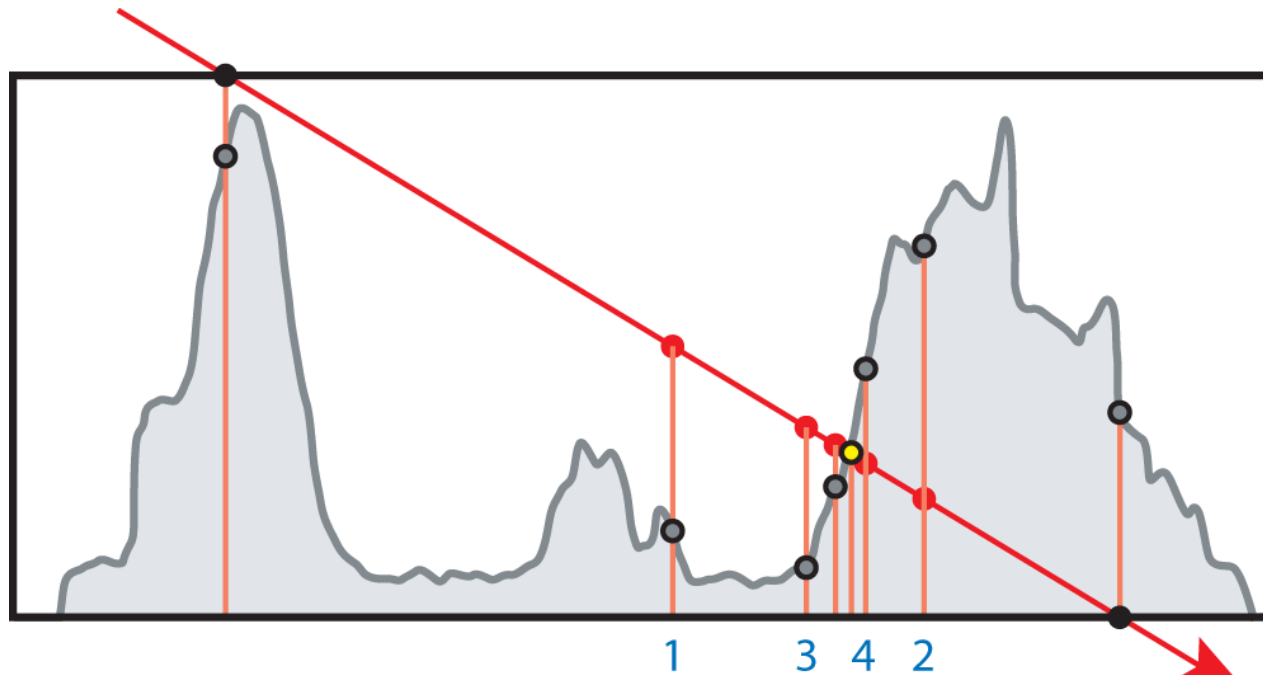
# Intersection Algorithm



# Intersection Algorithm

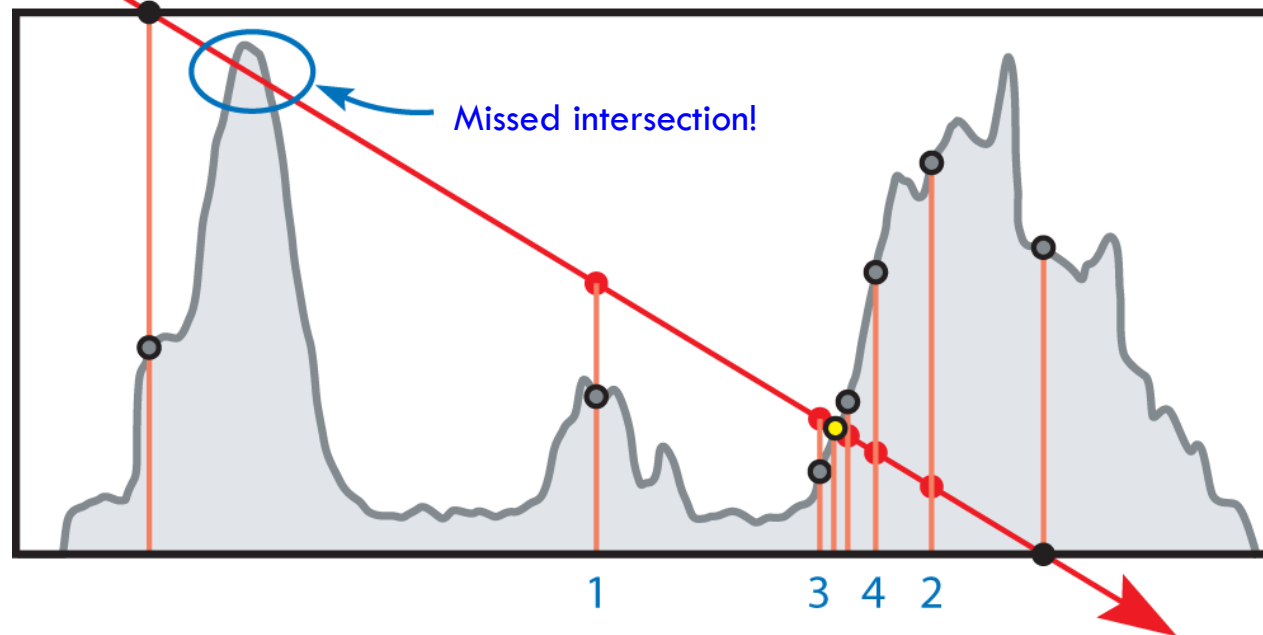


# Intersection Algorithm



## Intersection Algorithm

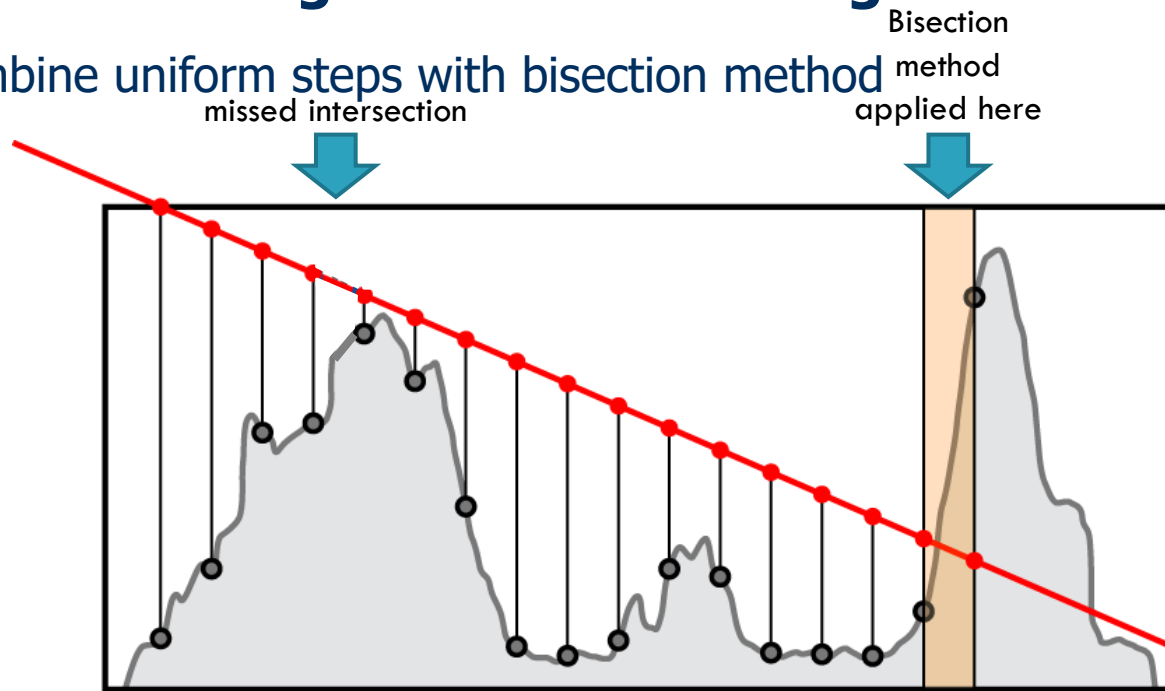
- Observation: Only works for one intersection!





# Traditional Height-Field Rendering

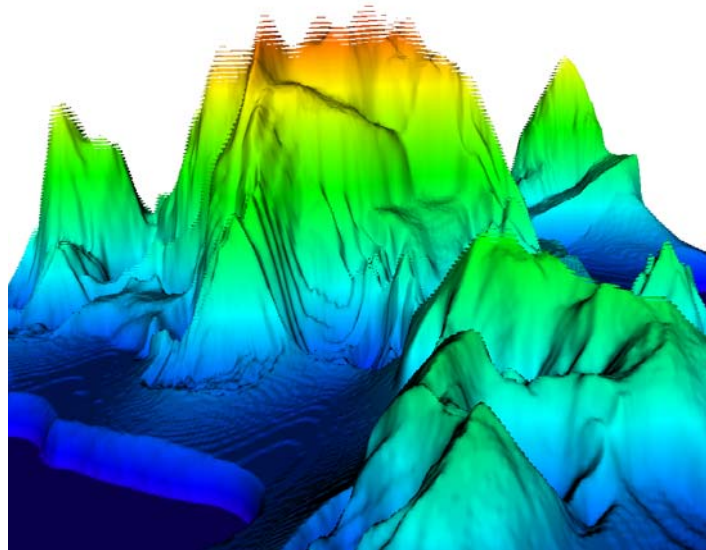
- Combine uniform steps with bisection method



## Previous Work

- Advanced Accelerations  
[Policarpo 05,07], [Tatarchuk 06]

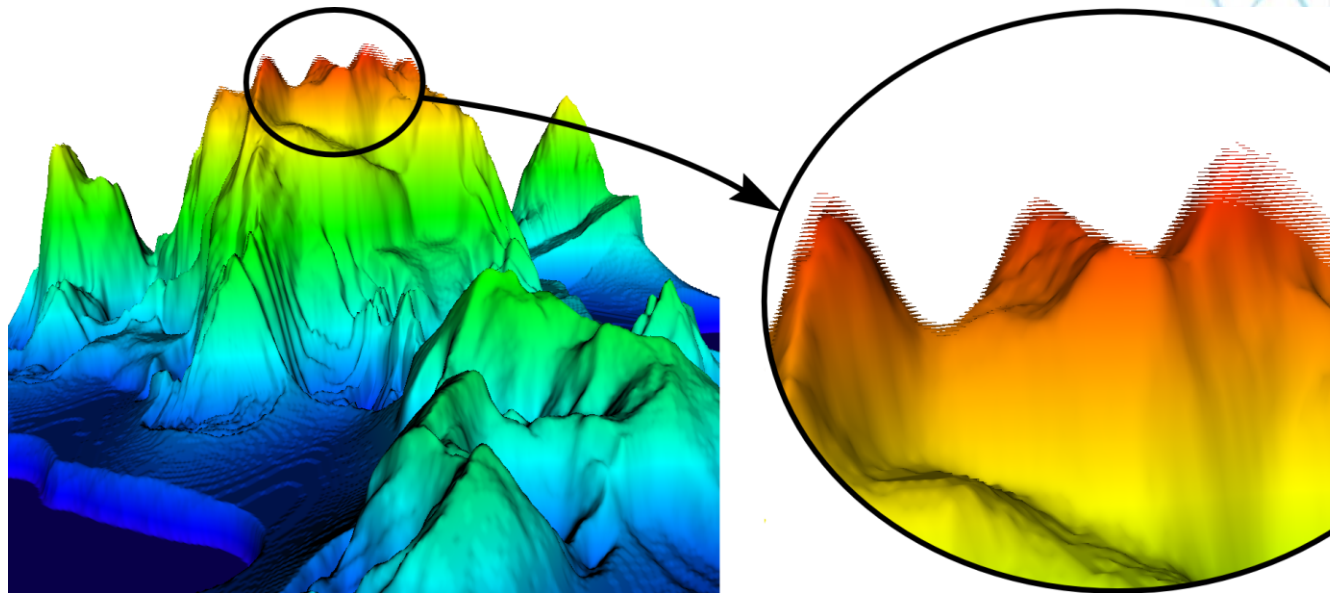
**100  
steps**



## Previous Work

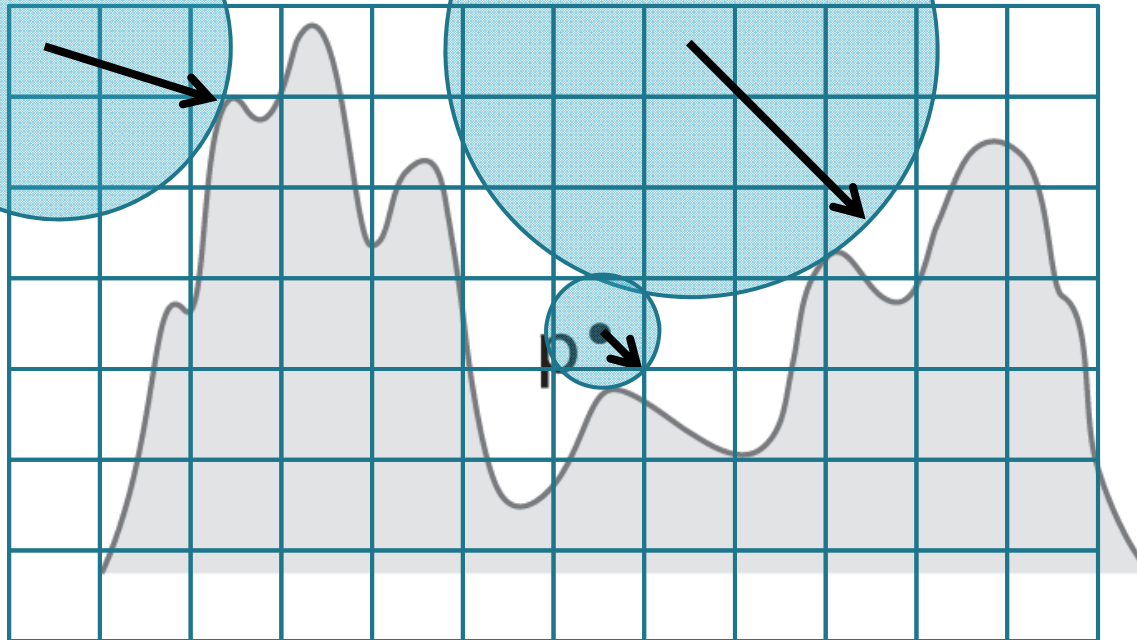
- Advanced Accelerations  
[Policarpo 05,07], [Tatarchuk 06]

**500  
steps**



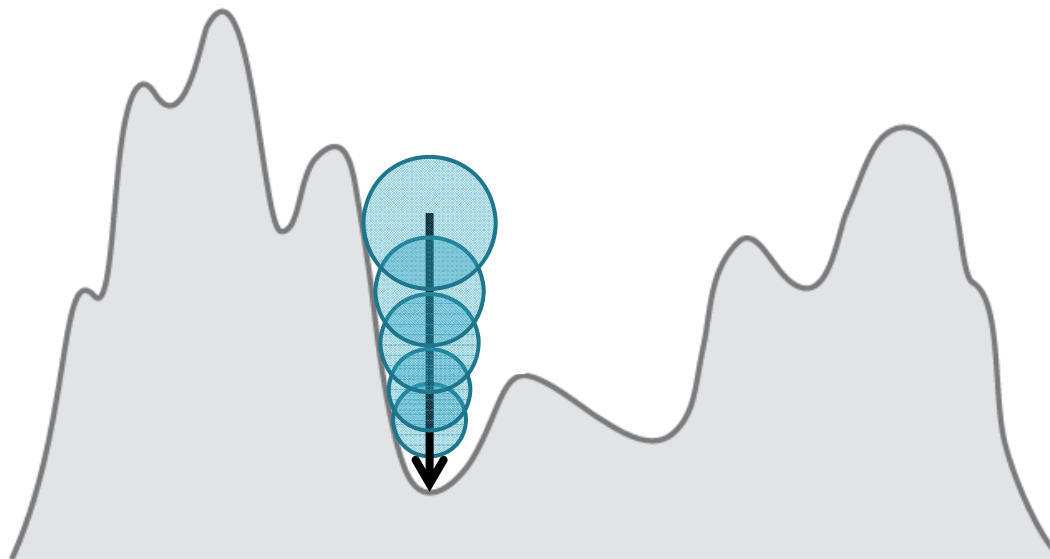
## Marching Shapes – Non-collision distances

- Store distance to surface in 3D volume



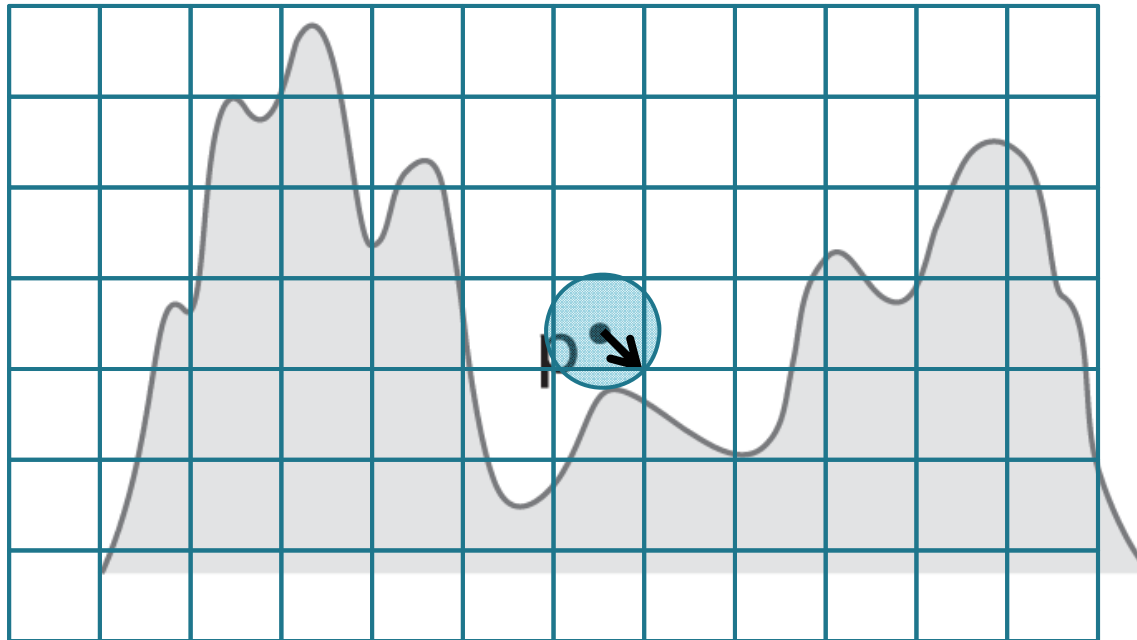
## Marching Shapes – Non-collision distances

- Problems: Requires 3D storage  
No converge on surface



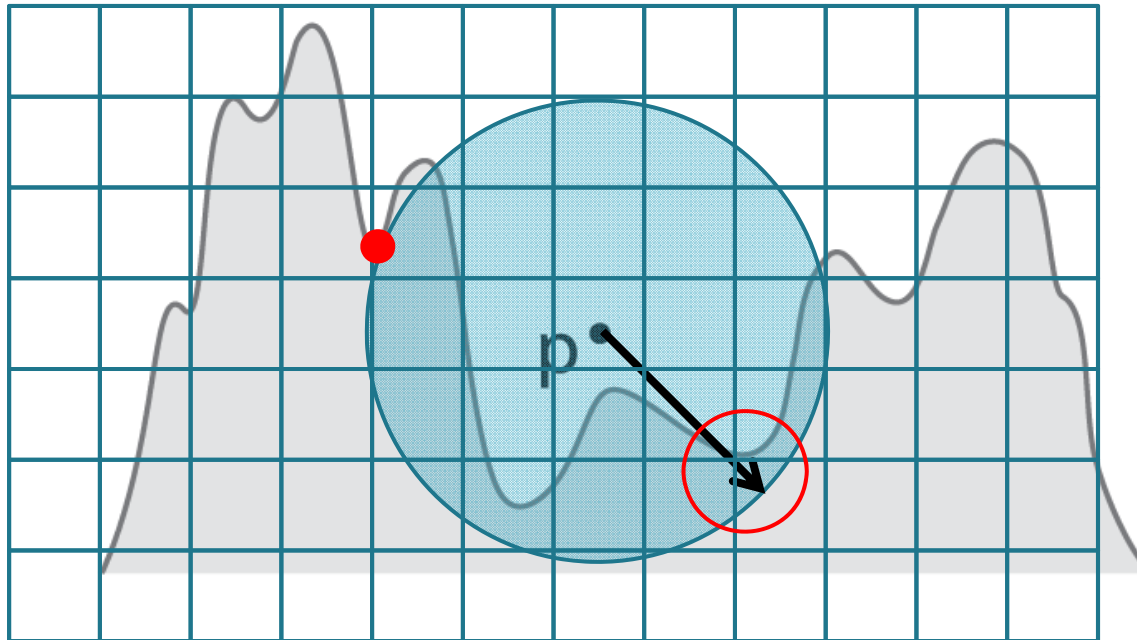
## Marching Shapes

- Store distance to surface in 3D volume



## Safety Shapes

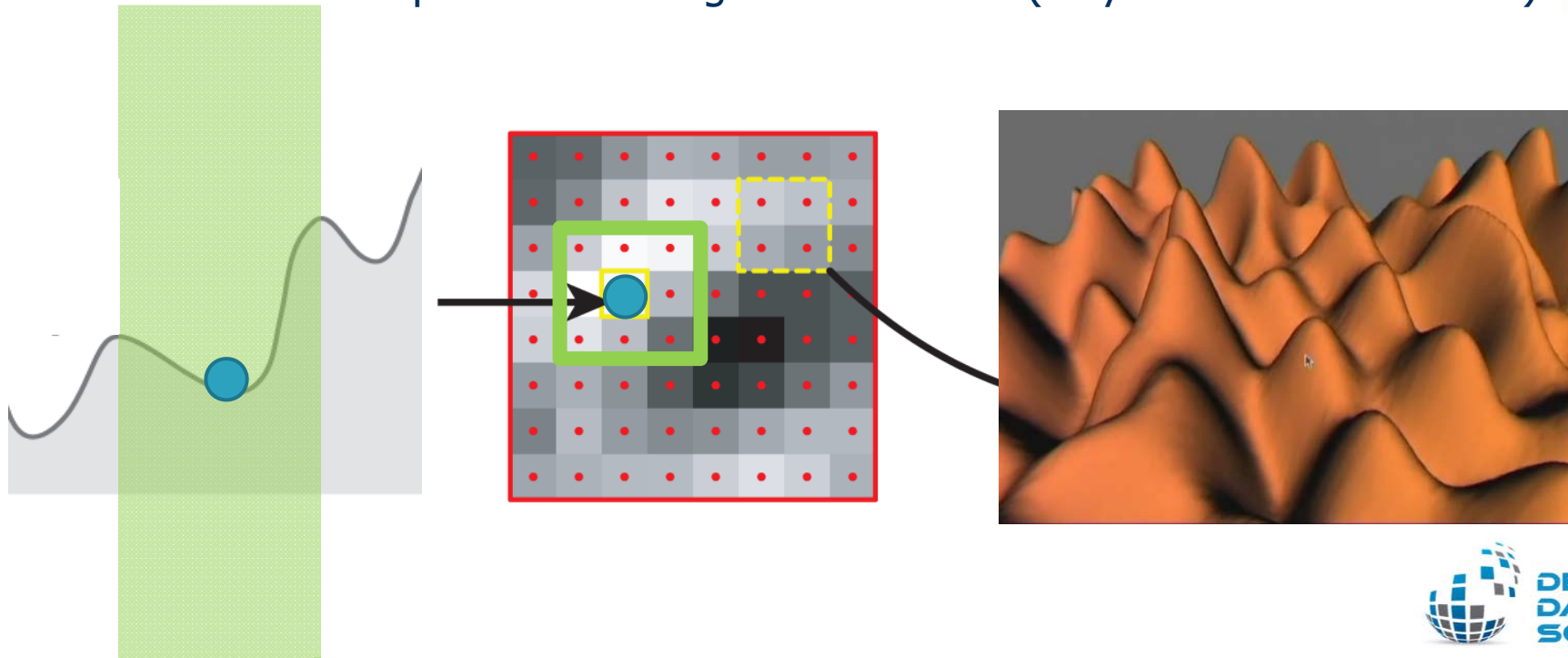
- Store distance to 2<sup>nd</sup> surface in 3D volume



Start bisection method

## Reduce Memory Cost

- Store 2D square in the height-field texture (only one additional value)





[Baboud, Eisemann, Seidel – IEEE TVCG 2012]

## Safety Shapes – Bells and Whistles

- Fast Computation
- Novel Interpolation Method
- Improved Safety Shapes (Directional, Cylicone etc.)
- Highest Numerical Stability



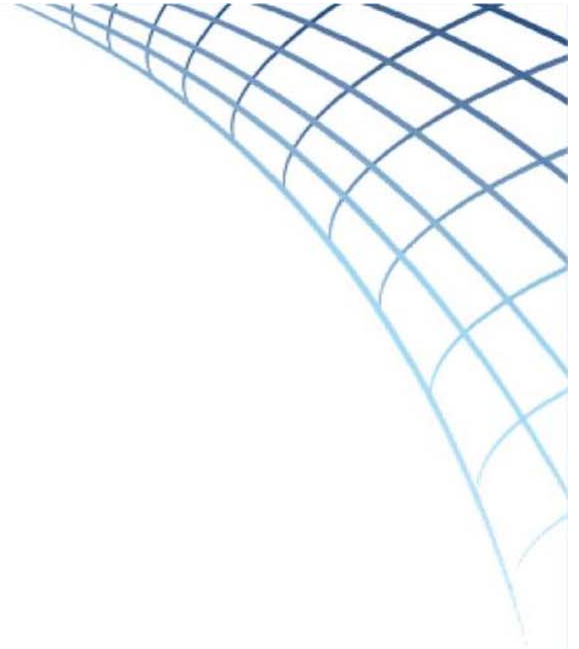
[Baboud, Eisemann, Seidel – IEEE TVCG 2012]

## Precomputed Safety Shapes

- Fast and accurate height-field rendering
- Arbitrary rays
- Low precomputation (3-4 orders of magnitude)
- Pure 2.5D
- All data has to reside in memory

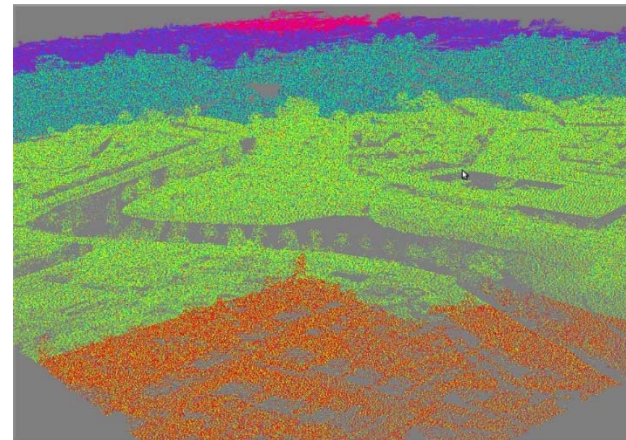
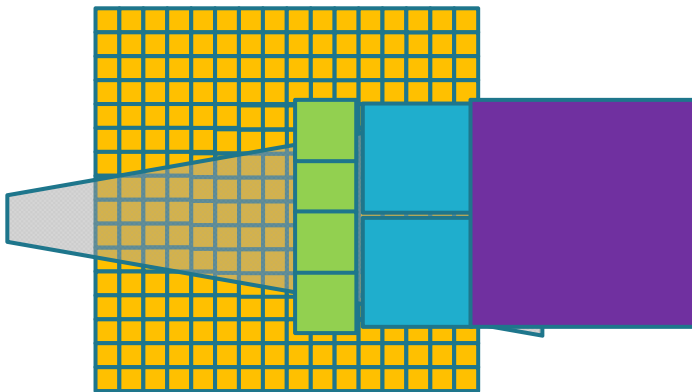


**Questions?**



## Large-scale Out-of-core Rendering

- Create Hierarchy (tile area and create multiple resolution height fields)
- Choose resolution according to viewer
- Cull nodes outside the frustum



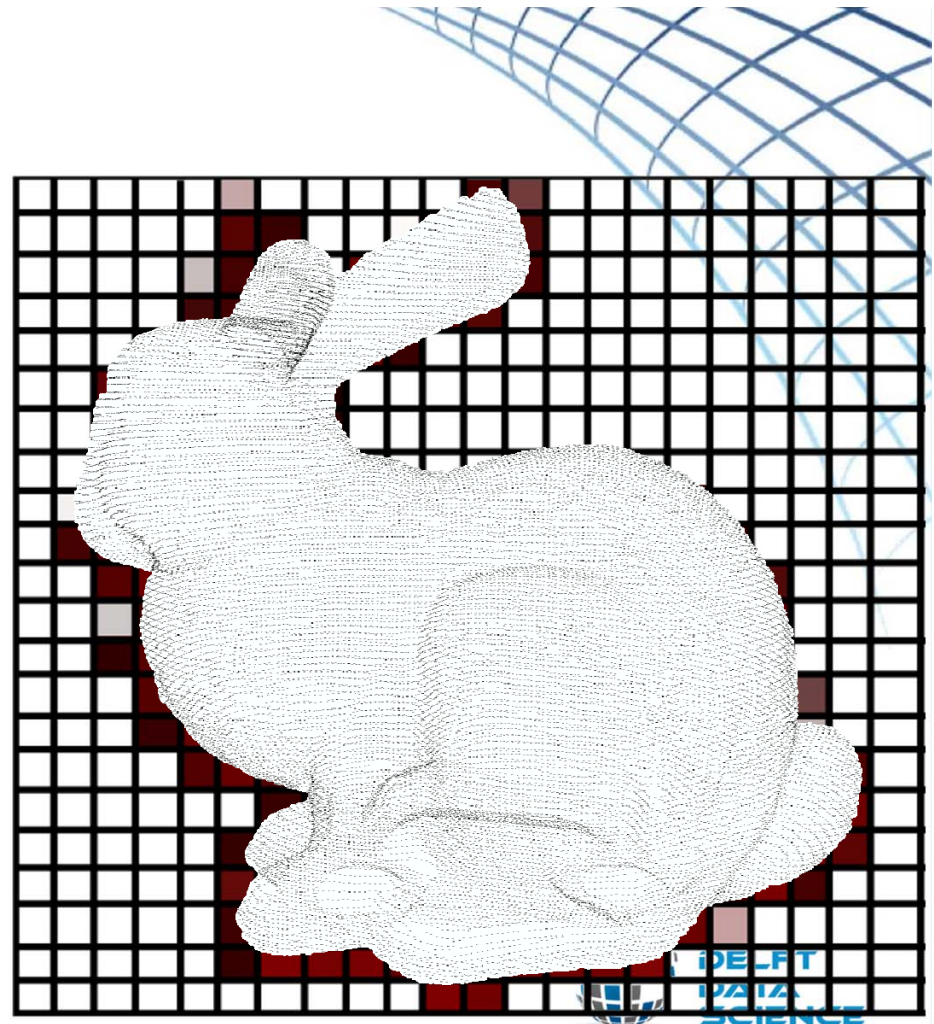
## Large-Scale Data

- Integration of street-view scans into the AHN2 dataset



## Add structure...

- Voxel Representations



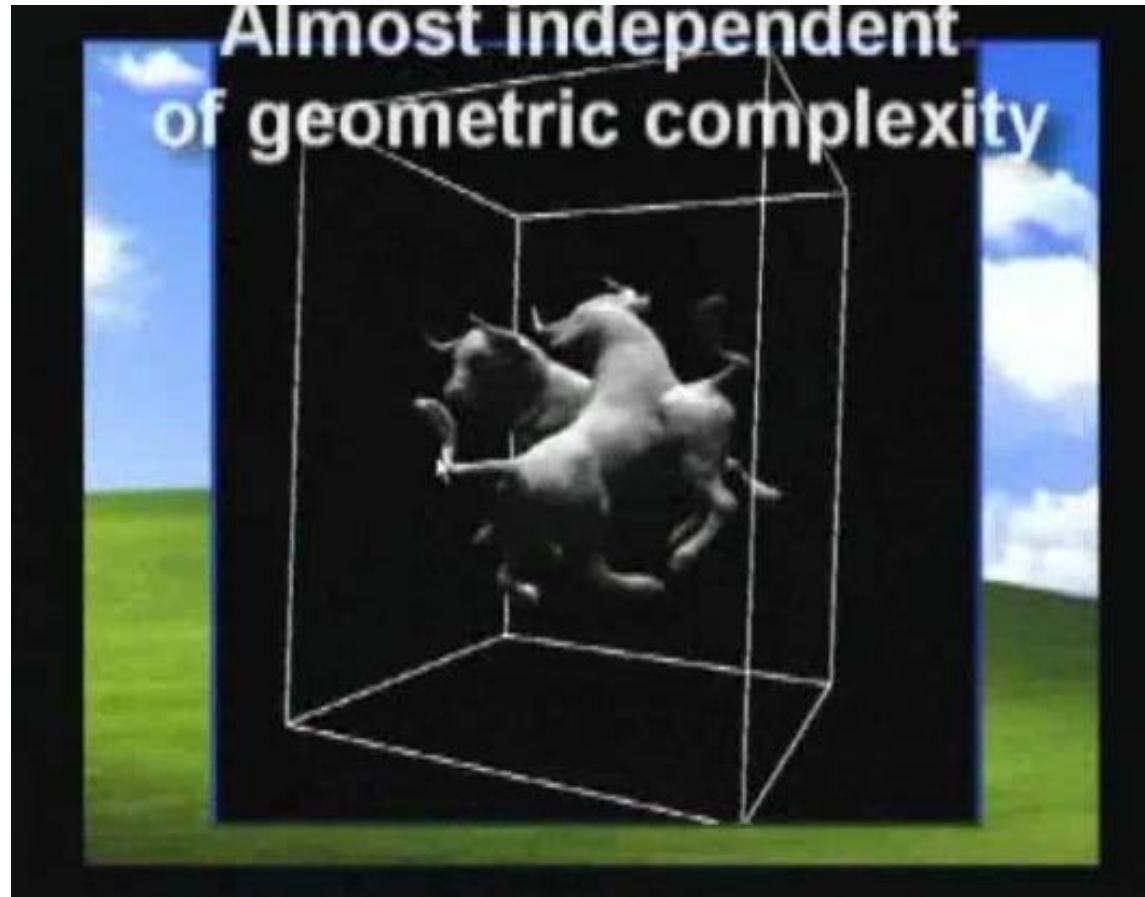
## Voxels - Excursion

- Have many applications
- Allow for random-access queries
- Fast algorithms to voxelize objects in real-time  
[Eisemann & Decoret i3D2006], [Eisemann & Decoret GI2008]  
Back then:  $1024^3$  binary voxelization at 100 fps for 300K triangles (NvidiaG80)



[Eisemann & Decoret i3D2006], [Eisemann & Decoret GI2008]

## Voxels



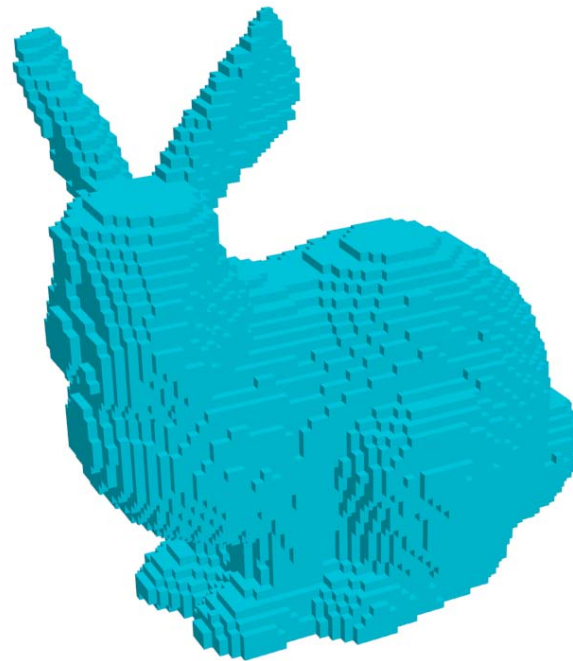


[Eisemann & Decoret i3D2006], [Eisemann & Decoret GI2008]

## Voxels



# Voxels





# Voxel Representations

- **Main problem:**
  - Memory is a key issue!
  - E.g.  $2048^3 \times \text{RGBA} = \mathbf{32\ GB}$



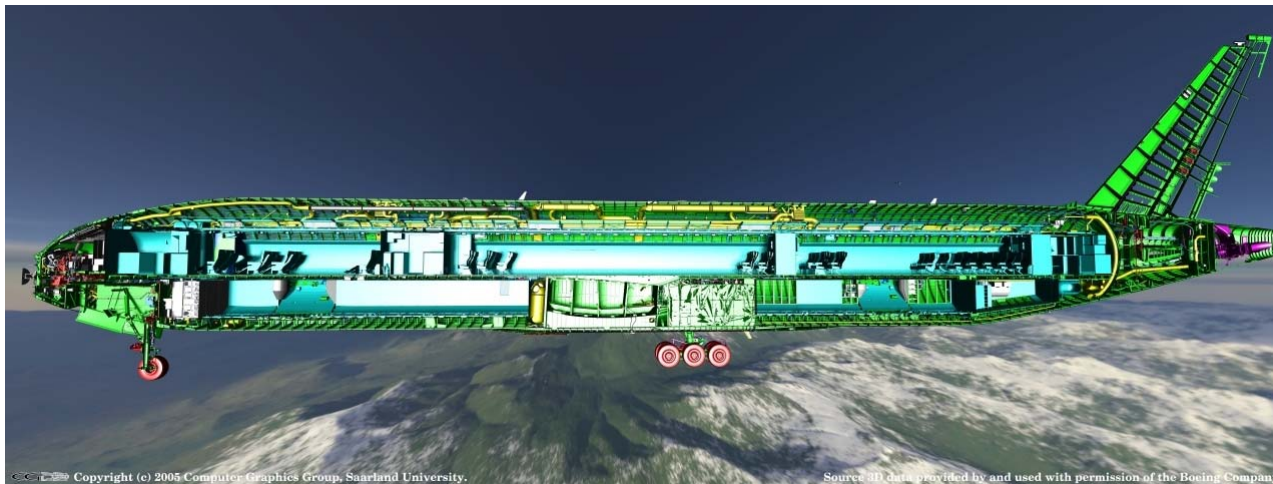
## How to deal with large-scale scenes?

Level of detail, visibility tests, compression...

Today: only a glimpse of what is done...

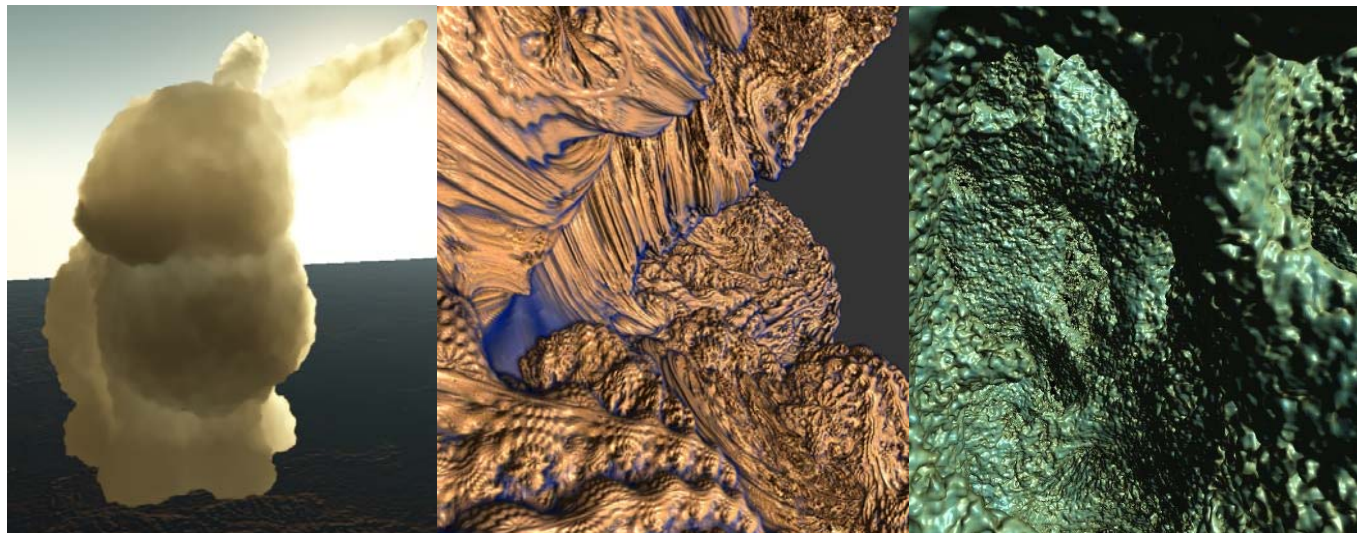
Ray-tracing methods [Wald et al. 2004]

- During ray traversal record missing data and upload



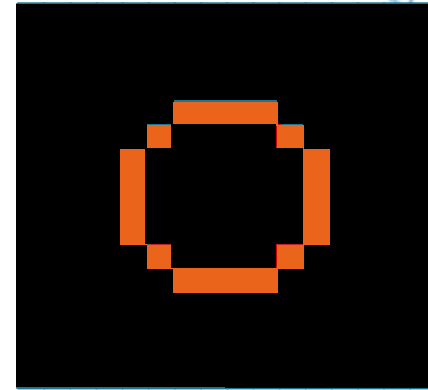
## Modern GPU instances

- Hybrid CPU/GPU approach [Gobetti et al. 2008]
- Full GPU approach [Crassin et al. 2009]



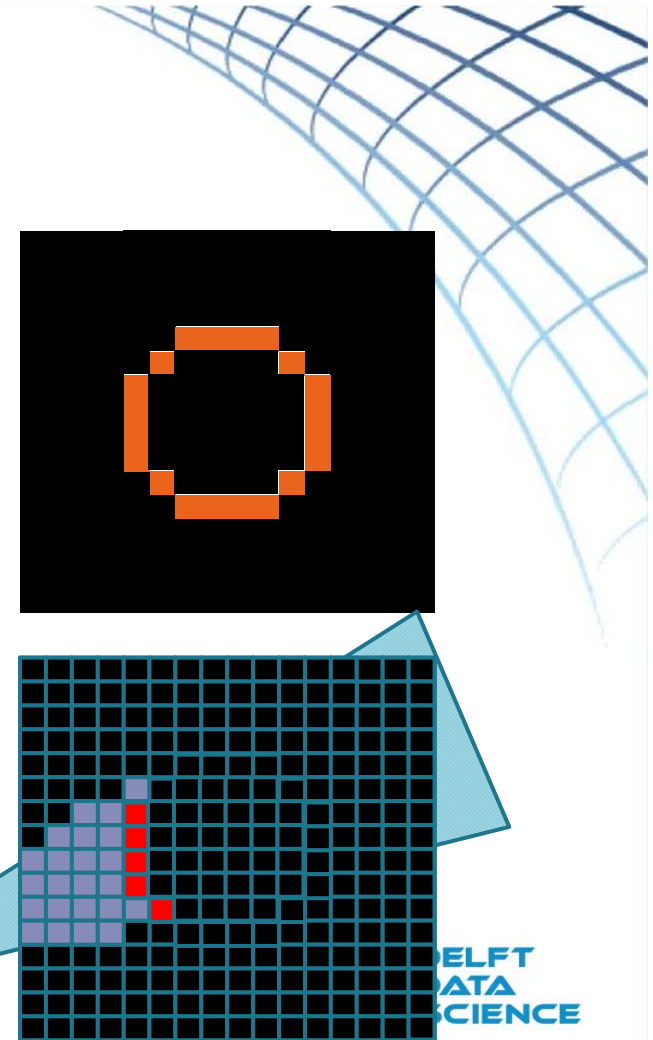
## Ways to deal with large data

- Constant valued areas  
(also empty)



## Ways to deal with large data

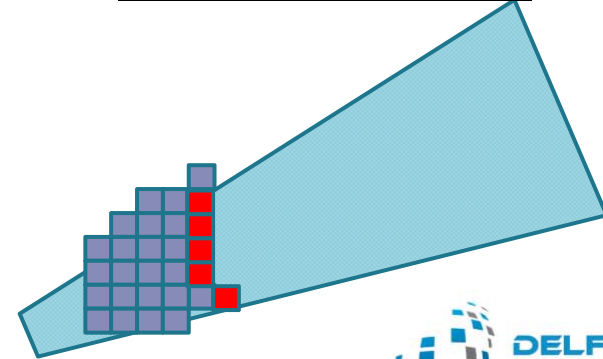
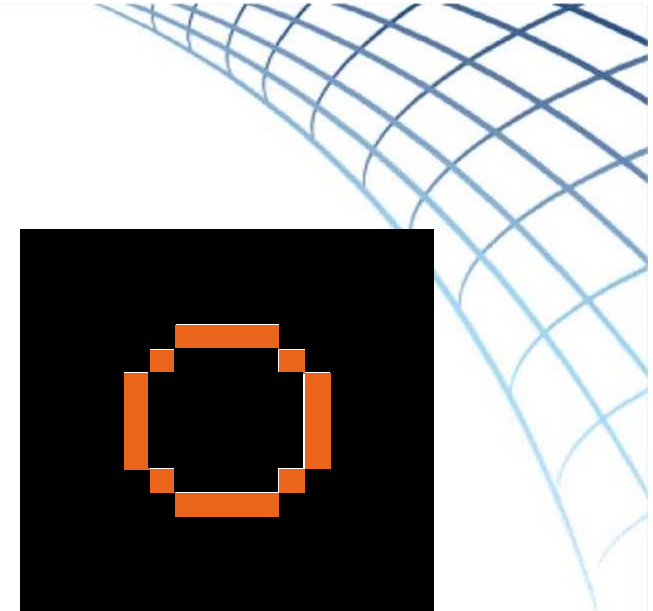
- Constant valued areas  
(also empty)
- View-dependence
  - Visibility





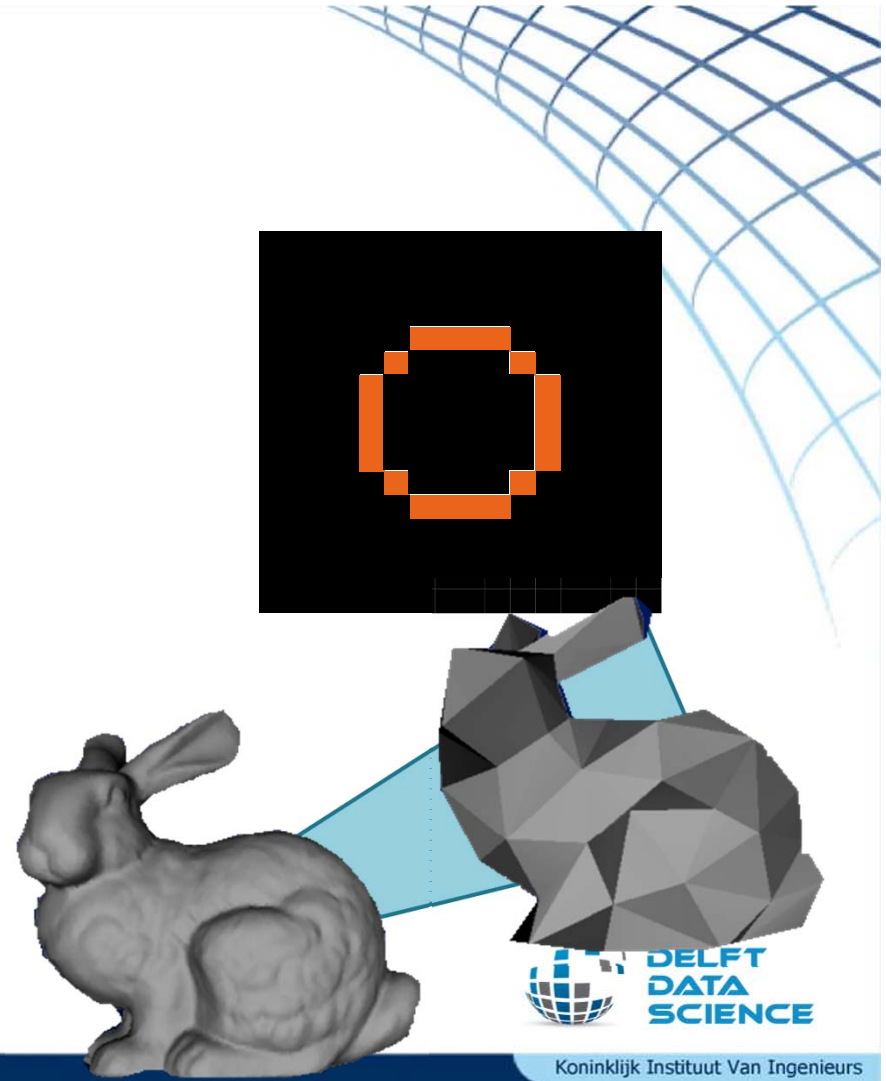
## Ways to deal with large data

- Constant valued areas  
(also empty)
- View-dependence
  - Visibility



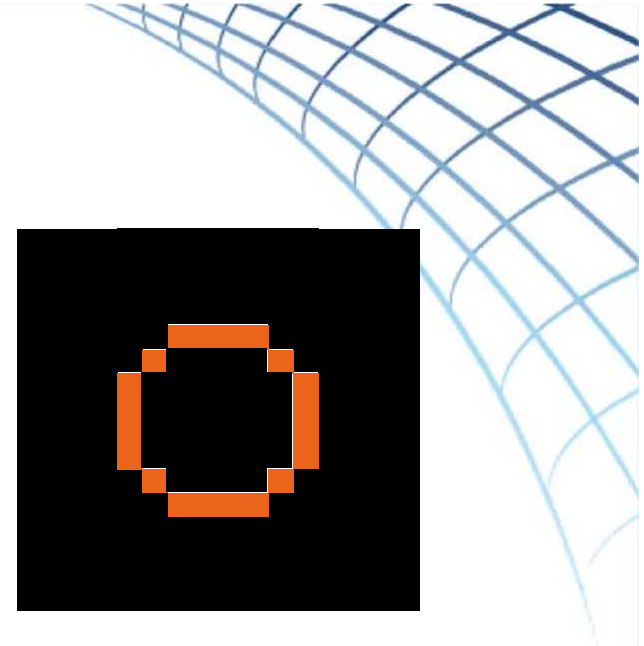
## Ways to deal with large data

- Constant valued areas  
(also empty)
- View-dependence
  - Visibility
  - Level of Detail



## Ways to deal with large data

- Constant valued areas  
(also empty)



- View-dependence
  - Visibility
  - Level of Detail



[Crassin, Neyret, Lefebvre, Eisemann – I3D 2009]

[Crassin, Neyret, Lefebvre, Eisemann – GPUPro2010]

## Free-Viewpoint Details



## Ways to deal with large data

- How to exploit these observations in practice?

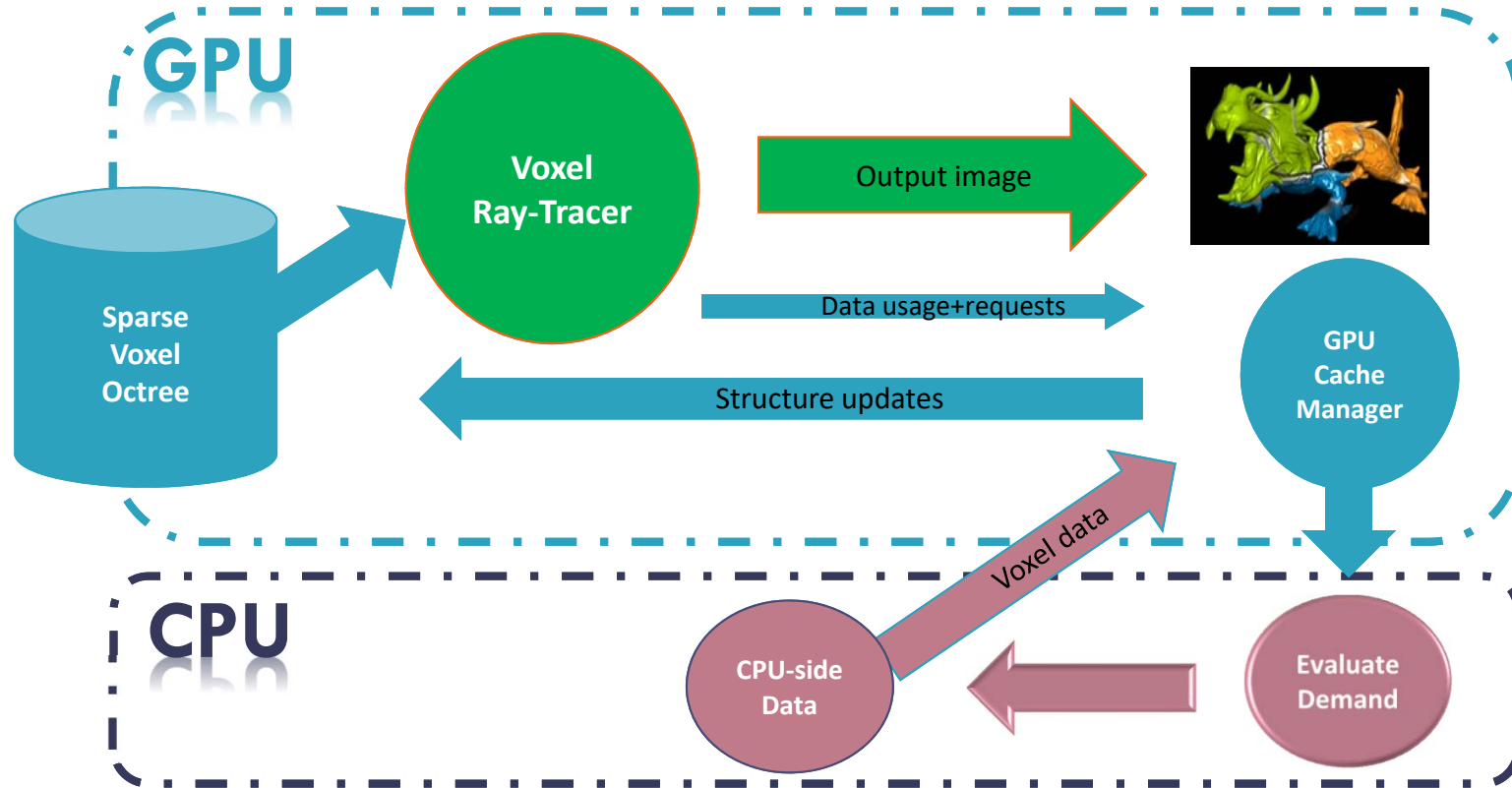
Need:

- Data structure allowing for easy adaptation
- Memory management

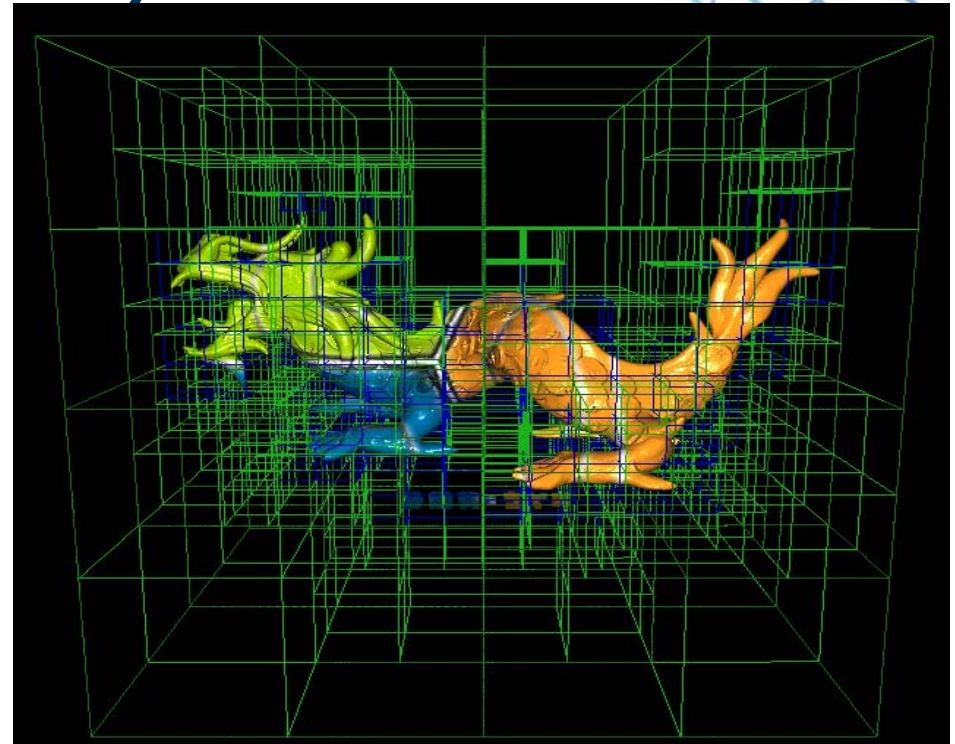
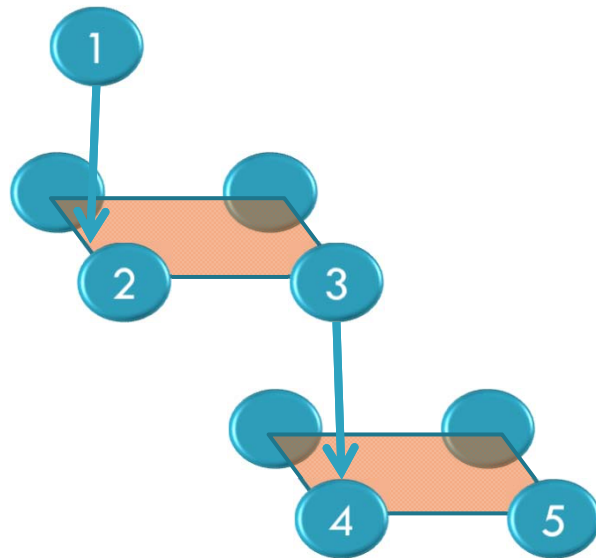


[Crassin, Lefebvre, Neyret, Eisemann - i3D 2009]  
[Crassin, Neyret, Lefebvre, Eisemann - GPUPro2010]

# GigaVoxel System



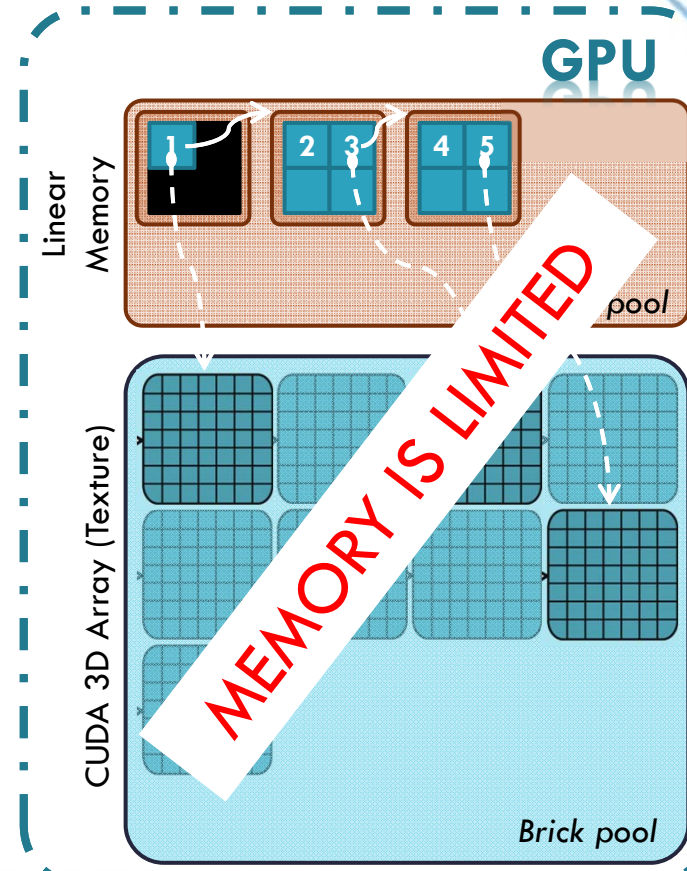
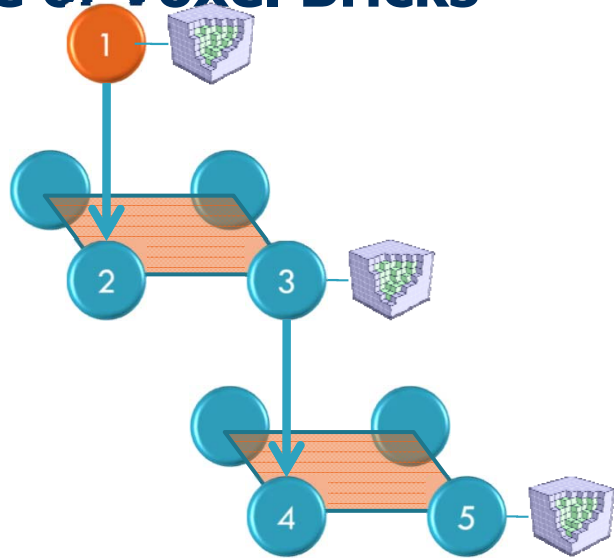
## Octree of Small Volumes (Bricks)



DATA  
SCIENCE

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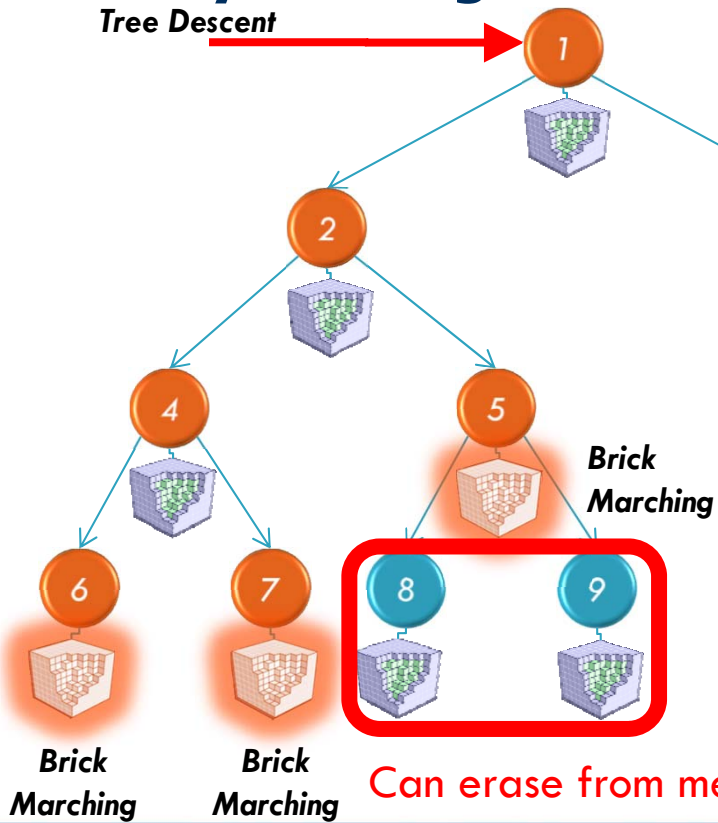
# Octree of Voxel Bricks



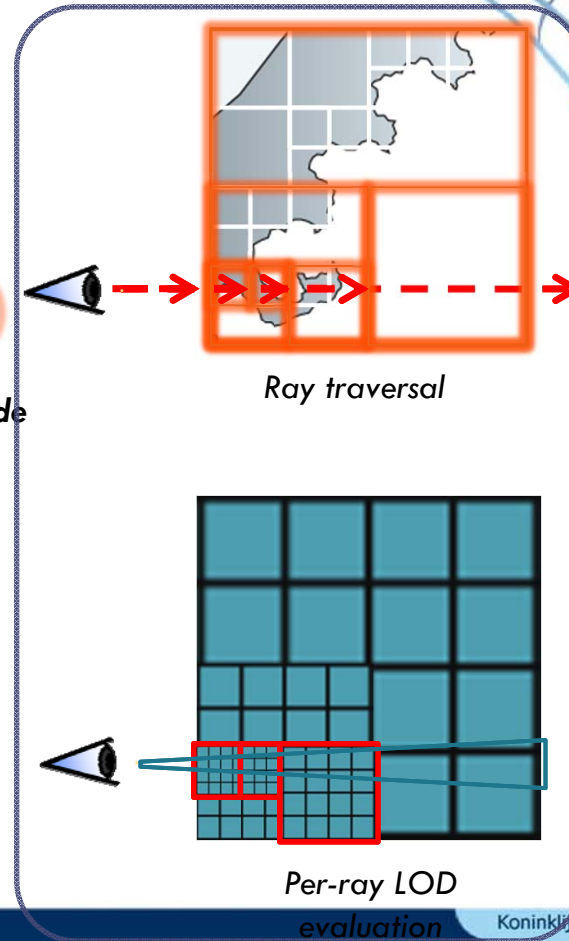


# Volume Ray-Casting

Tree Descent

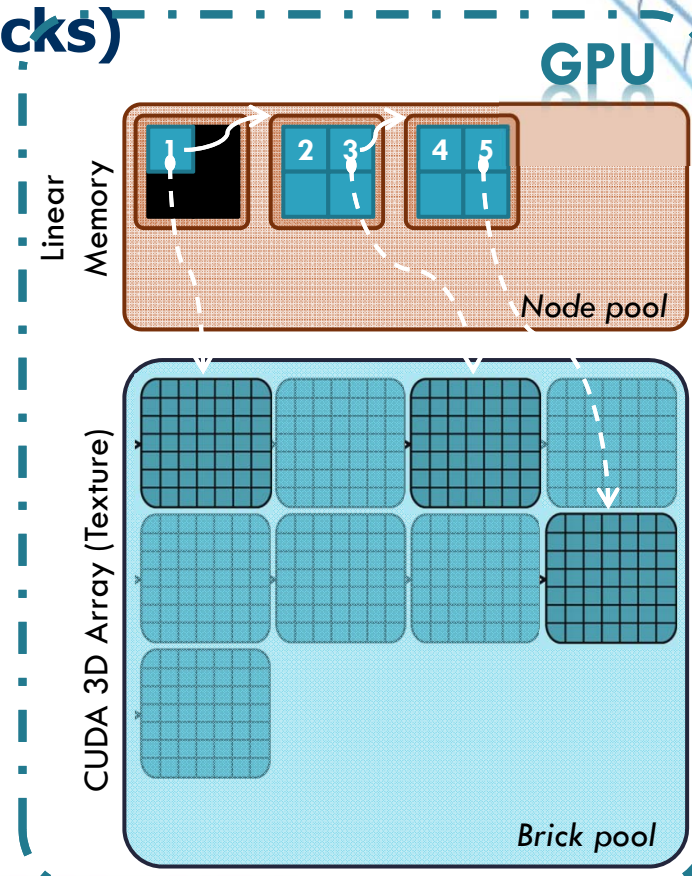


Skip Node



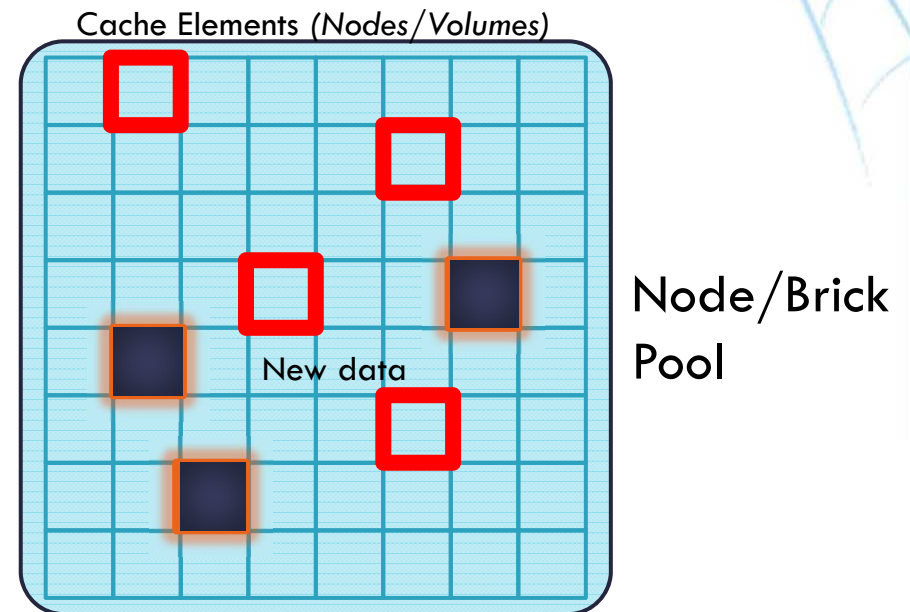
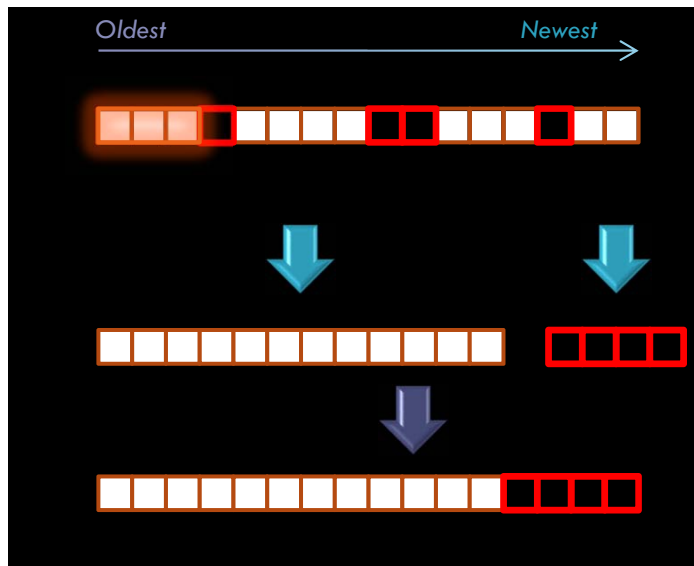
## Octree of Small Volumes (Bricks)

- All elements have the **same size** in memory!
- Makes exchanges easy

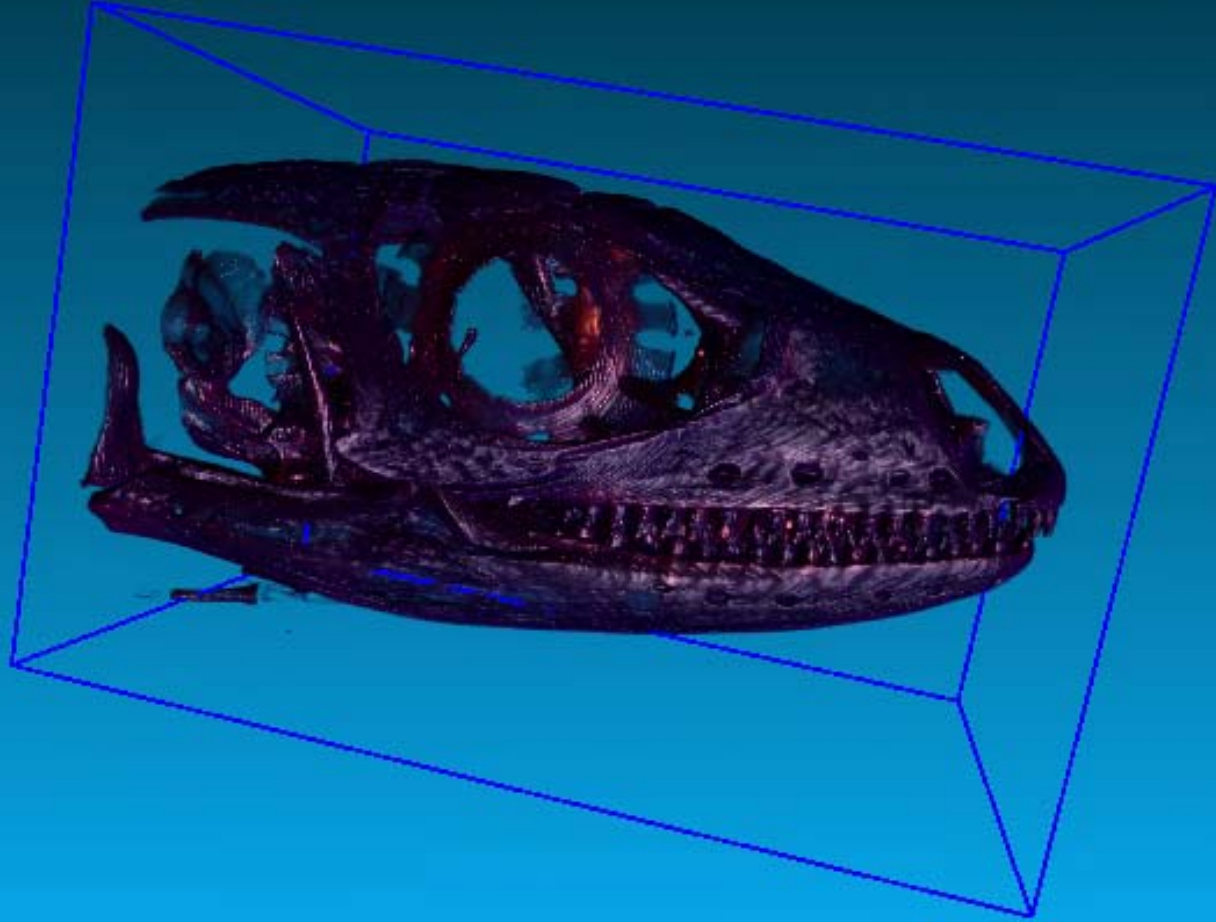


## “Rendering Queries” – Ray Queries

- GPU **Least-Recently-Used** Cache
  - Track element usage
  - **Maintain** list with least-used element in front



Projective



Front

[Crassin, Lefebvre, Neyret, Eisemann - i3D 2009]

[Crassin, Neyret, Lefebvre, Eisemann - GPUPro2010]

## GigaVoxels

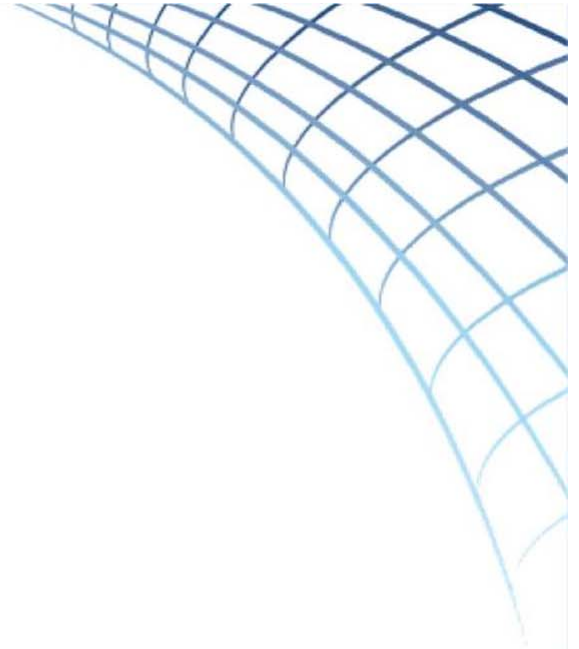
- Interactive Out-of-core Exploration of Volume Data
- Fully GPU-oriented
  - Rendering Algorithm
  - Data Representation

### Major remaining challenges:

- Bandwidth to GPU
- Storage (volumes grow quickly)



**Questions?**



## Large-Scale Voxels

Major remaining challenges for less performant systems:

- Bandwidth to GPU
- Storage (volumes grow quickly)



compression

[Dado, Kol, Thiery, Bauszat, Eisemann – Eurographics 2016]

$2^{51}$  voxels = 2,251,799,813,685,248 Voxels

## Colored DAGs



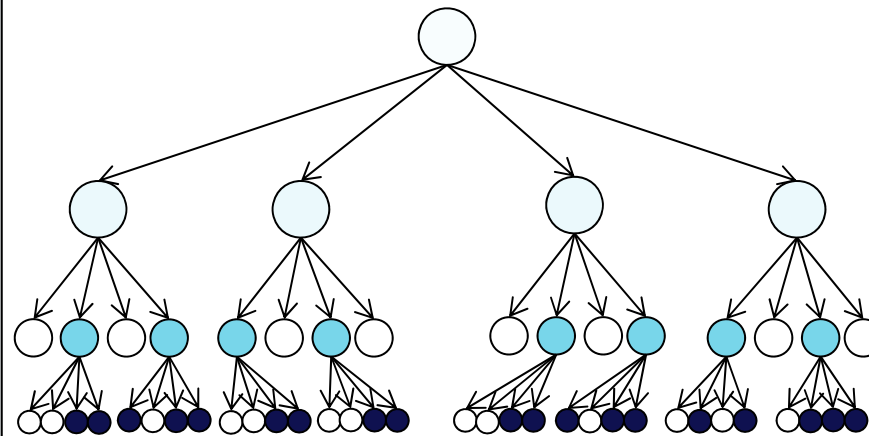
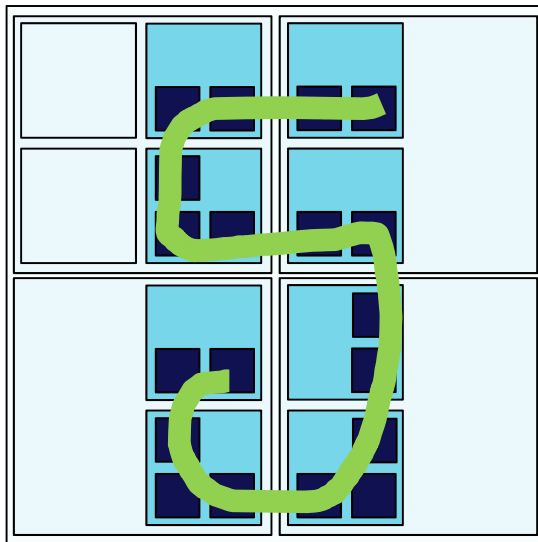
Koninklijk Instituut Van Ingenieurs



[Kaempe et al. – SIGGRAPH 2013]

# Sparse Voxel Directional Acyclic Graphs

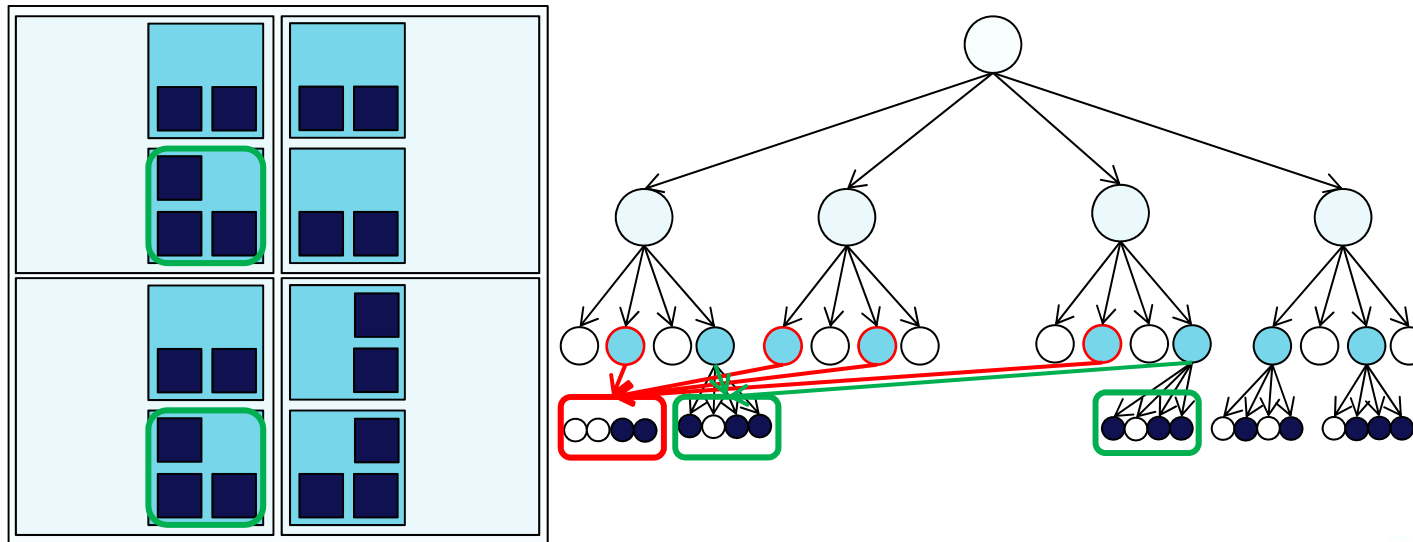
Binary Data Example





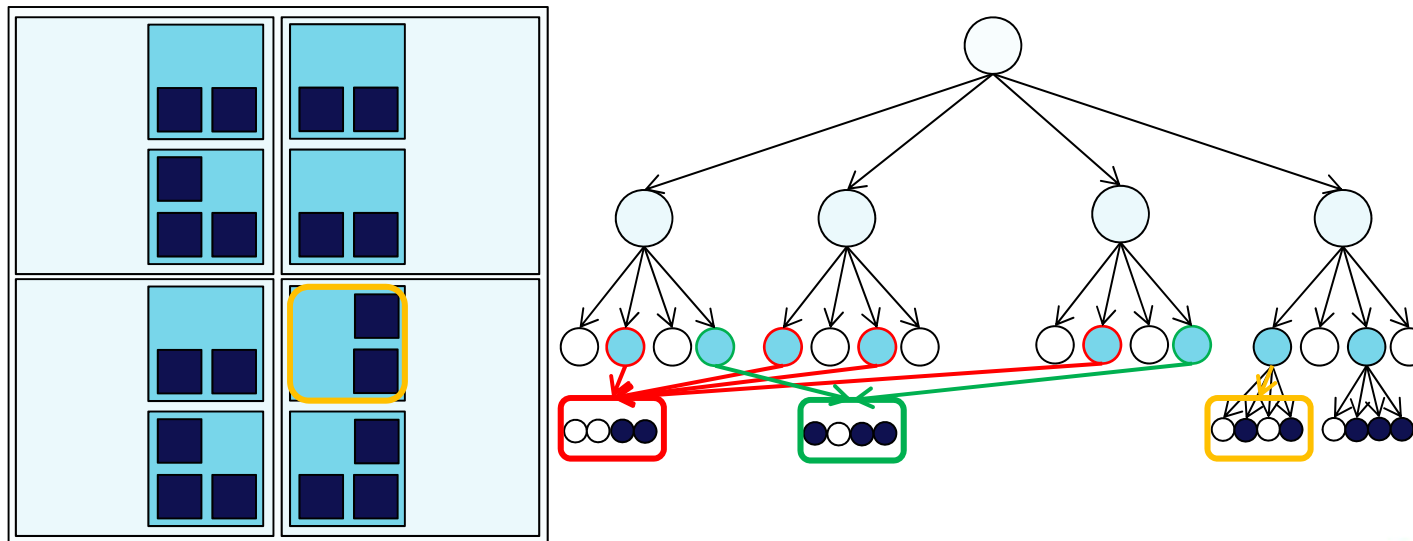
[Kaempe et al. – SIGGRAPH 2013]

## Sparse Voxel Directional Acyclic Graphs



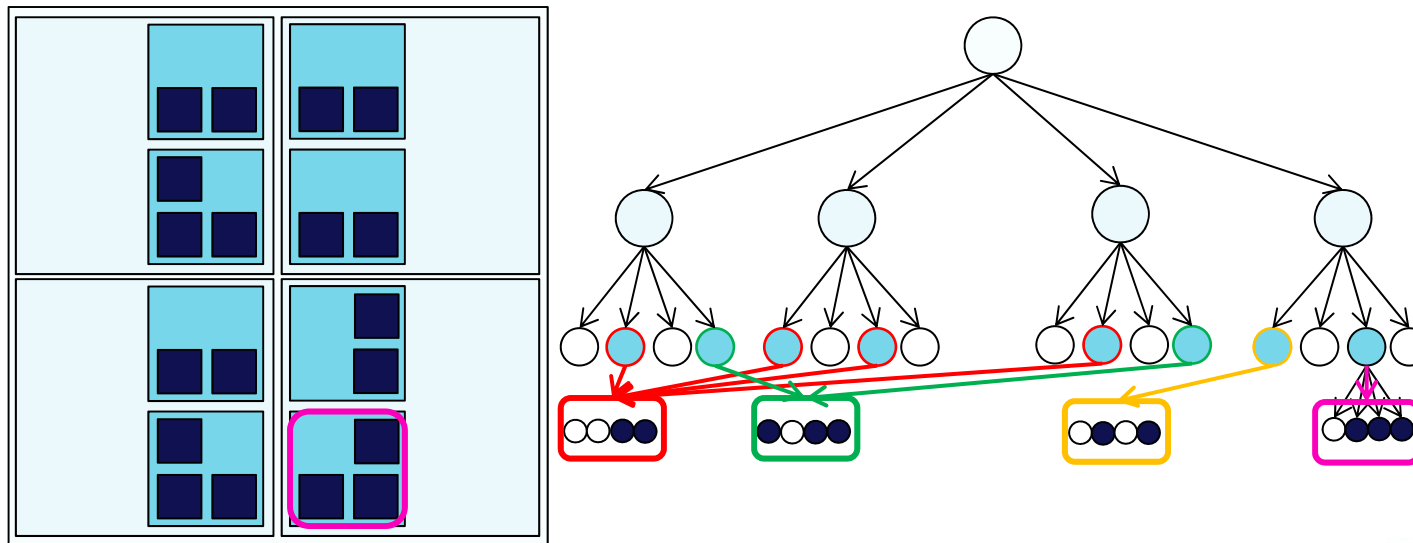
[Kaempe et al. – SIGGRAPH 2013]

## Sparse Voxel Directional Acyclic Graphs



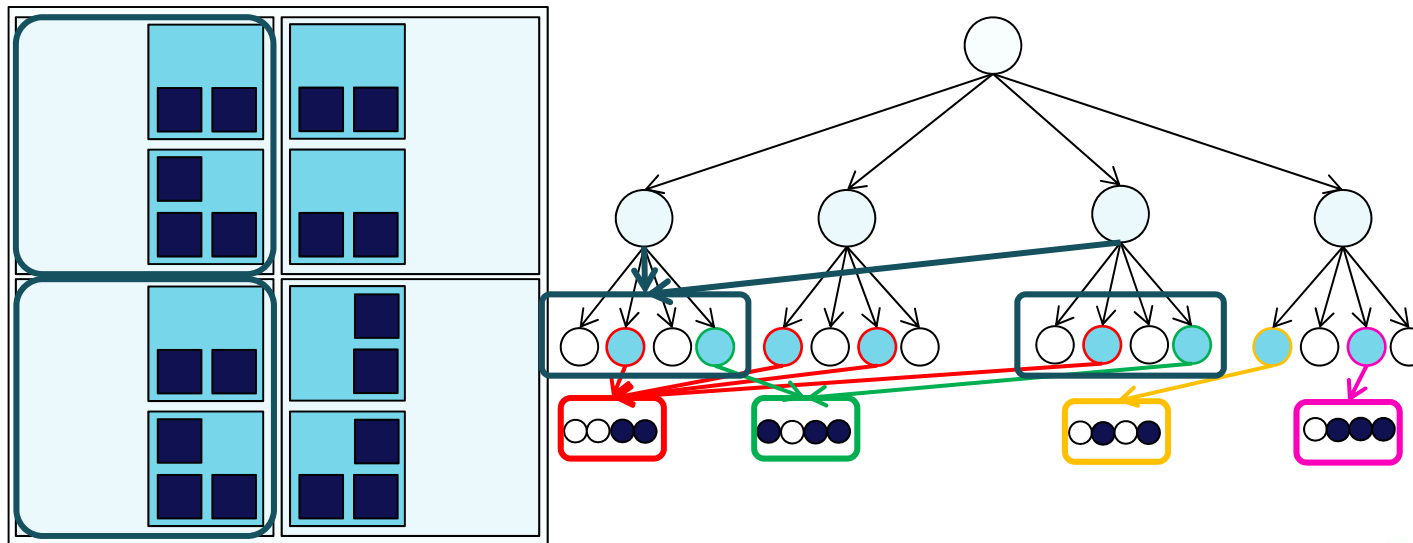
[Kaempe et al. – SIGGRAPH 2013]

## Sparse Voxel Directional Acyclic Graphs



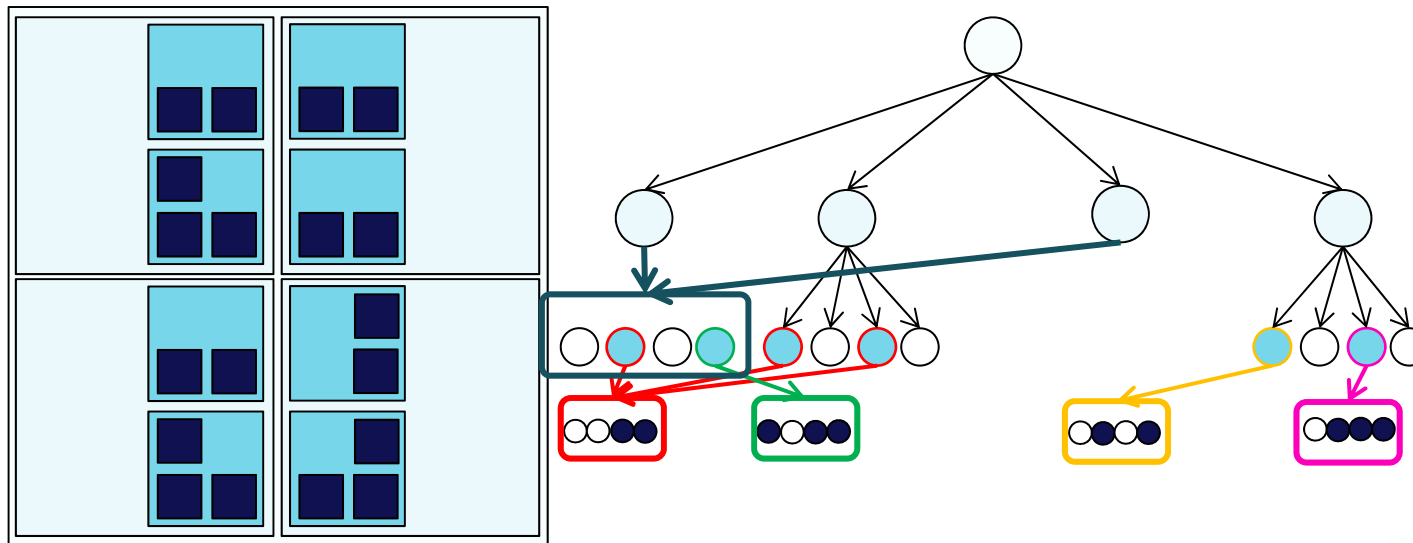
[Kaempe et al. – SIGGRAPH 2013]

## Sparse Voxel Directional Acyclic Graphs



[Dado, Kol, Thiery, Bauszat, Eisemann – Eurographics 2016]

## Sparse Voxel Directional Acyclic Graphs



Recent improvements:

More efficient compression  
Extension to voxel attributes



## San Miguel scene

64K<sup>3</sup>, 12-bit colors

15 billion filled voxels

Our size: 3.3 GB

Compression compared  
to sparse encoding: 11.5x



## Arena scene

64K<sup>3</sup>, 12-bit colors

3.3 billion filled voxels

Our size: 1.0 GB

Compression compared  
to sparse encoding: 9.3x

[Dado, Kol, Thiery, Bauszat, Eisemann – Eurographics 2016]

## Comparison

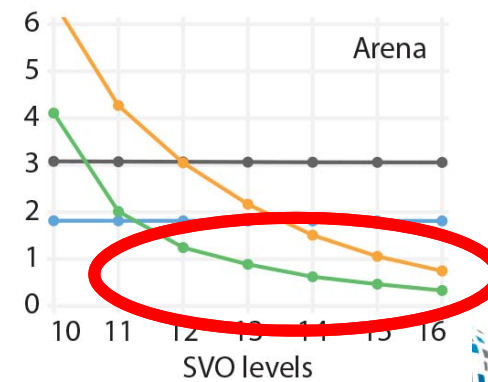
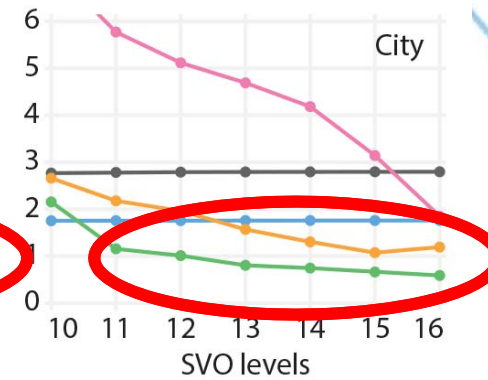
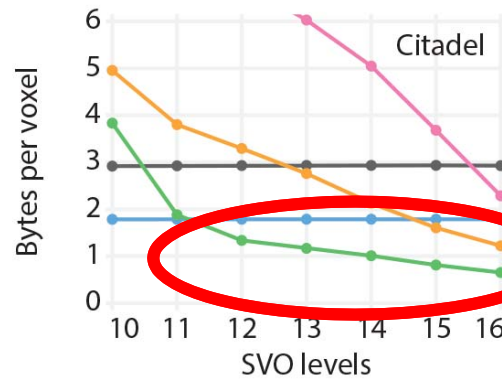
Cannot be displayed



- SVO
- PSVO
- ESVO
- CDAG
- Ours

PSVOs: [Schnabel and Klein 2006]

ESVOs: [Laine and Karras 2011]



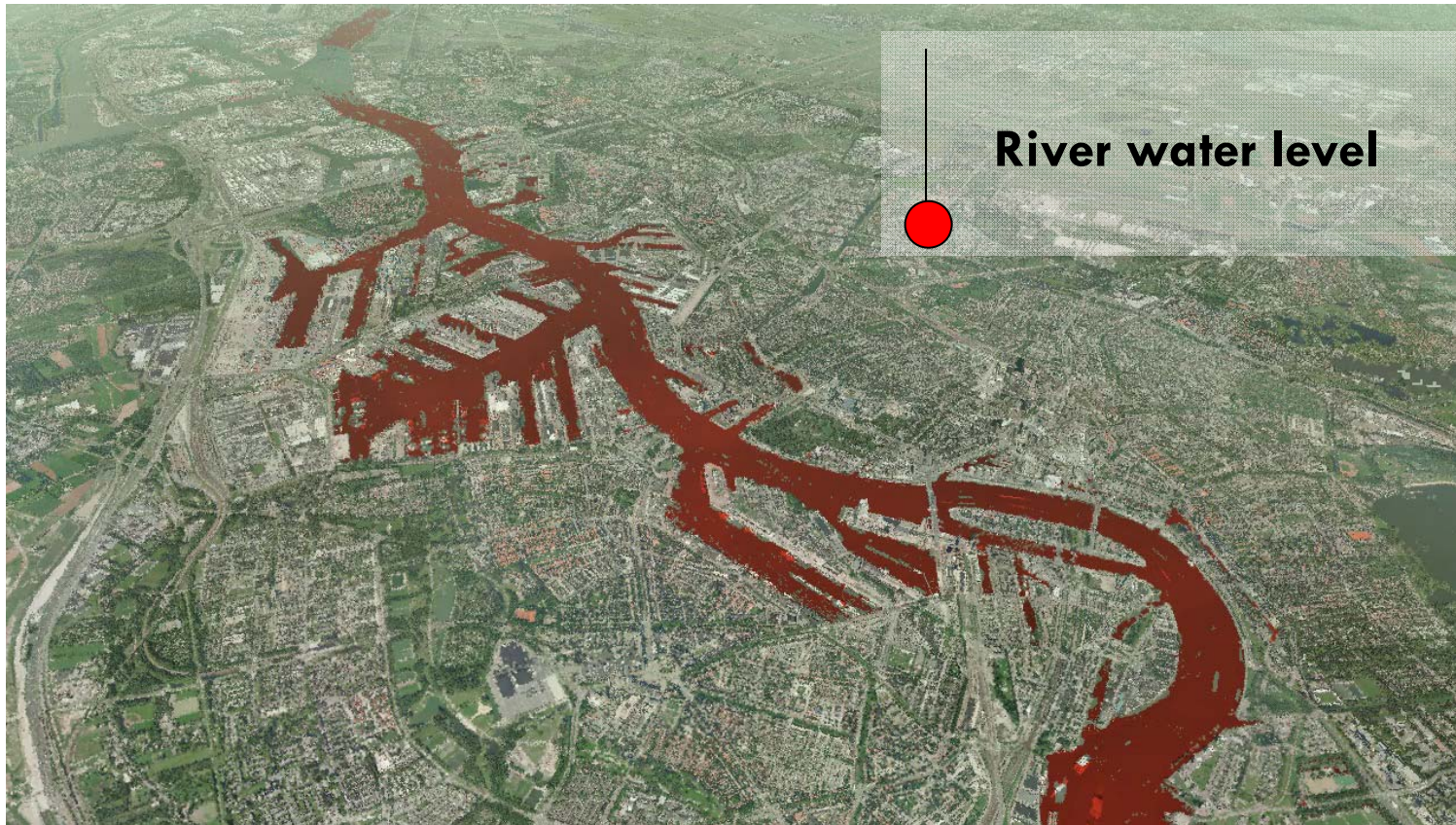
# Large-Scale Data Rendering



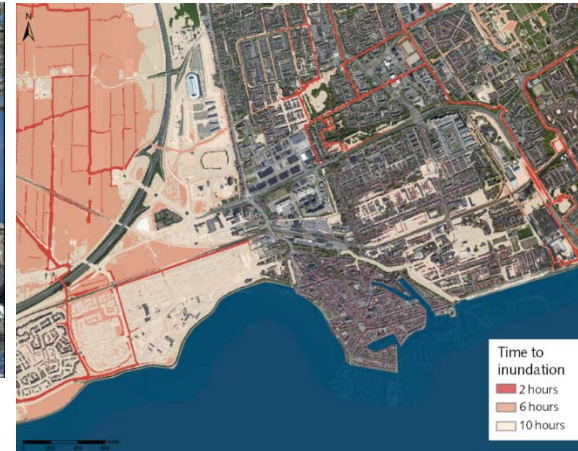
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# Flooding Scenario



## Evaluation of Evacuation Scenarios



- High benefit of visualizations  
> more and more equal discussion between parties



[Leskens, Kehl, Tuteneel, Kol, de Haan, Stelling, Eisemann  
– Science Env. Pol./Mit.Glob.Change 2015]

## Benefits of Realistic 3D Visualization



- Accessible to non-experts
- Useful for decision making
  - More involved discussions from all parties
  - Better estimation of damages/dangers
  - Better understanding of the context

## Exhibitions

- Reproduction of 1953 flooding exhibited in the
  - Noodwatermuseum Zeeland
  - Delft Science Center



## Large-Scale Rendering

- Ray Tracing
- Graphics Pipeline
- Specialized Methods for Different Data Types
  - Height-Field Data, Voxel Data, Data Management, Compression



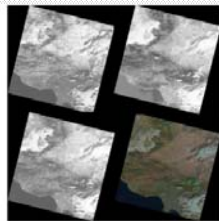
# Effective Data Visualization Requires



- **Large-Scale Rendering**



- **Visualization and Perception**



- **Data Analysis**

**Questions?**



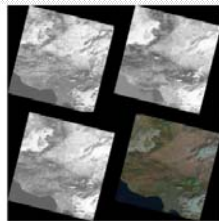
# Effective Data Visualization Requires



- **Large-Scale Rendering**



- **Visualization and Perception**



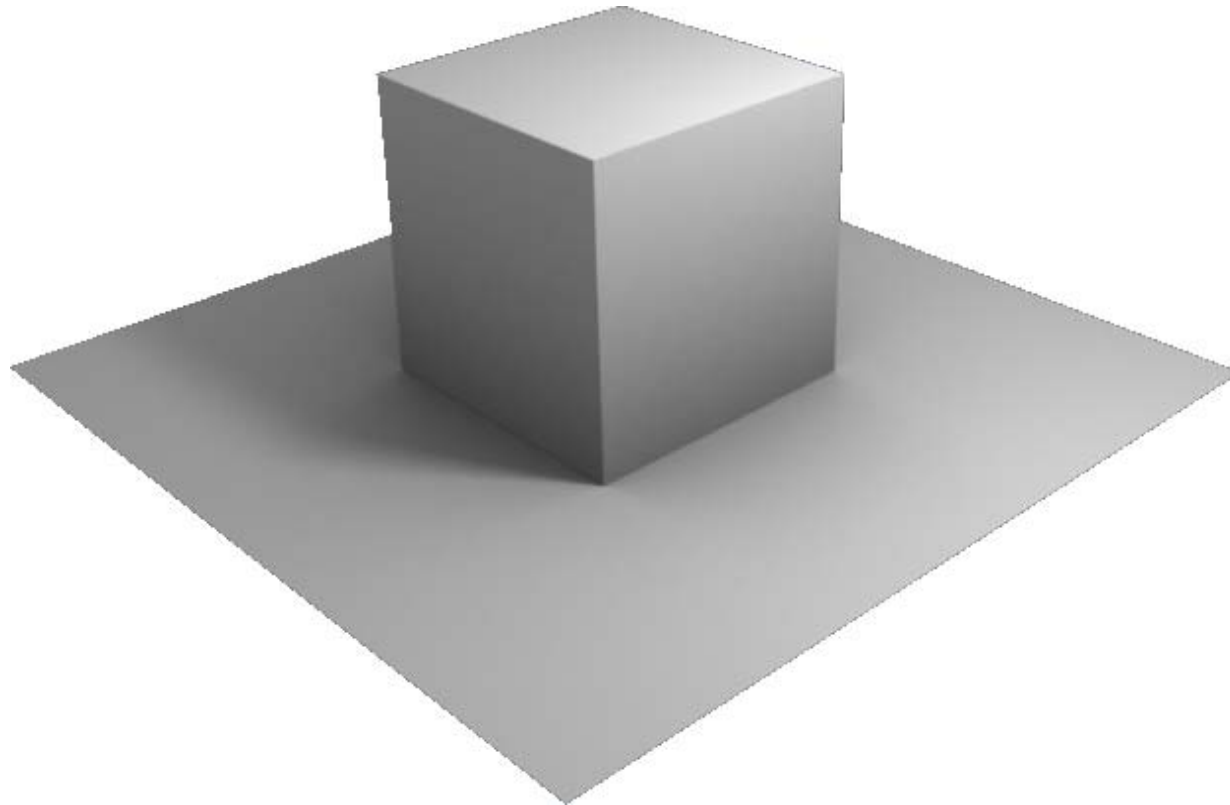
- **Data Analysis**

# Visualization and Perception

- Realistic Rendering
- Perceptual Methods
- Visualization



# Physically-Based Rendering





[Eisemann&Decoret - CGF 2008]

[Holländer, Ritschel, Eisemann, Boubekur - EGSR 2011]

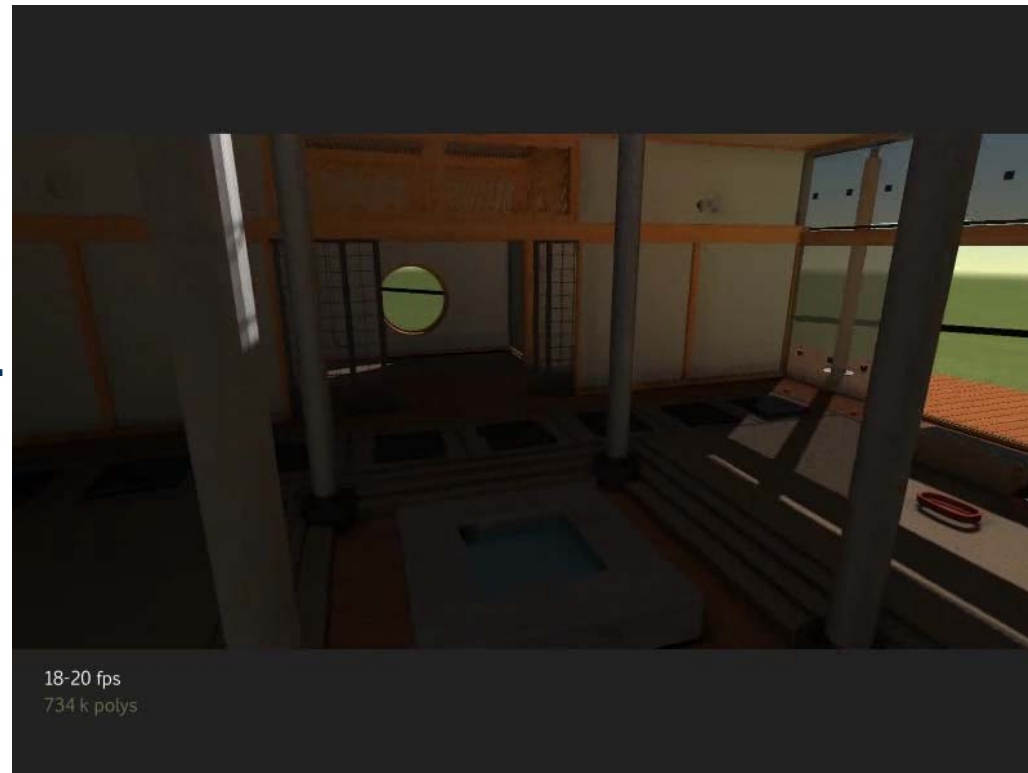
[Ritschel, Eisemann, Ha, Kim, Seidel - CGF 2011]

[Baboud, Eisemann, Seidel, TVCG 2012]

## Light Physics are Complex

- Reflections
- Refractions
- Caustics
- Transparency
- Global Illumin.

...



[Lee, Eisemann, Seidel – SIGGRAPH Asia'09] [Lee, Eisemann – EGSR'13]

[Lee, Eisemann, Seidel – SIGGRAPH'10] [Kurz, Ritschel, Eisemann, Thormählen, Seidel JVRB14]

[Hullin, Lee, Eisemann, Seidel – SIGGRAPH'11] [Joo, Kwon, Lee, Eisemann, Lee – EGSR16]

## Improving Camera Model

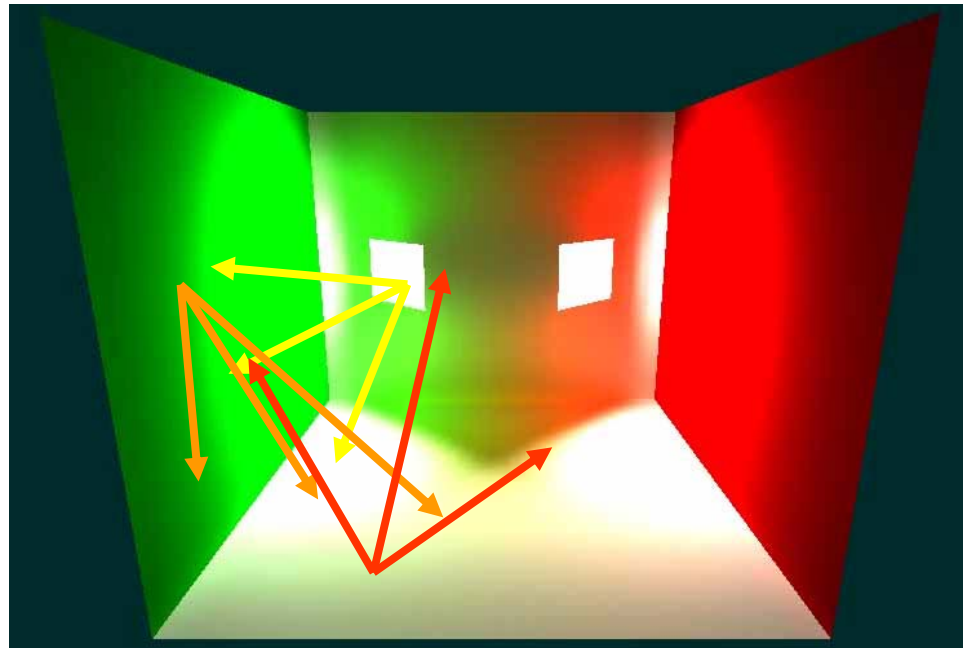
- Depth of Field
- Lens Blur
- Lens Flares
- ...



DELFT  
DATA  
SCIENCE



# Global Illumination



In 2002...  
More than 4 hours  
8 triangles



## Rendering Equation

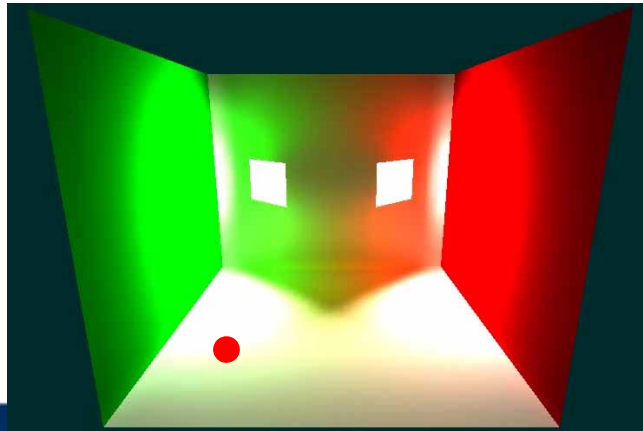
$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$

observed light = emitted light + reflected light

## Rendering Equation

- Position

$$L(\mathbf{x}, \theta_0, \varphi_0) = L_e(\mathbf{x}, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(\mathbf{x}, \theta_0, \varphi_0, \theta, \varphi) L_i(\mathbf{x}, \theta, \varphi) \cos \theta d\omega$$

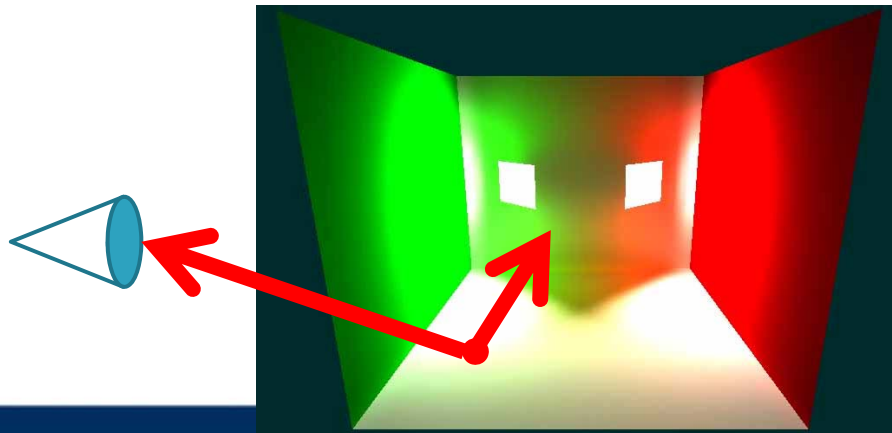


## Rendering Equation

- Orientation

$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$

Angular domain

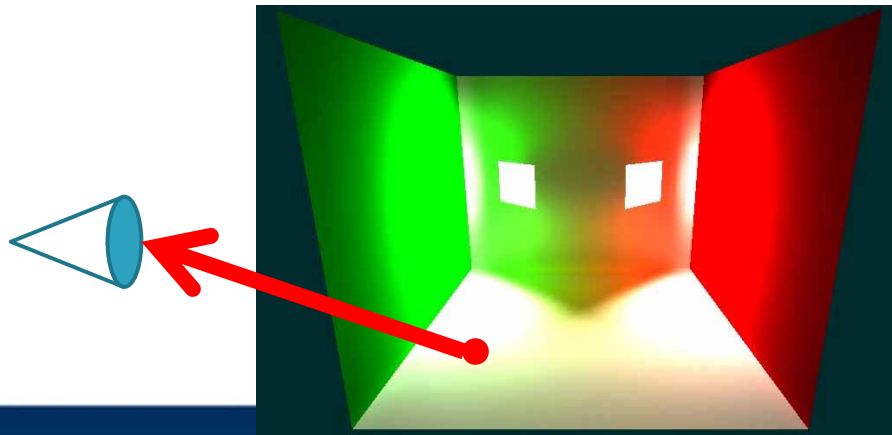


## Rendering Equation

- Radiance

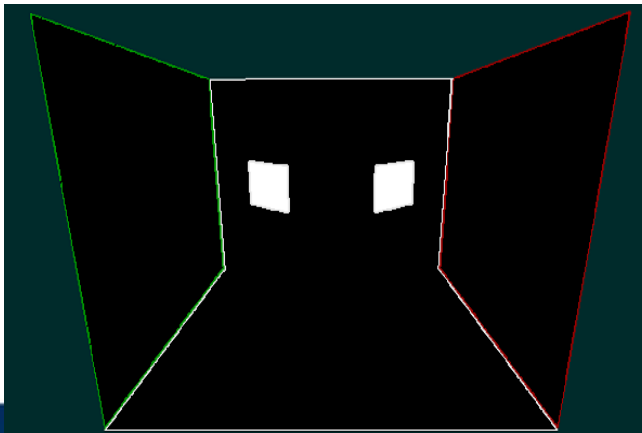
$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) +$$

$$\int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$



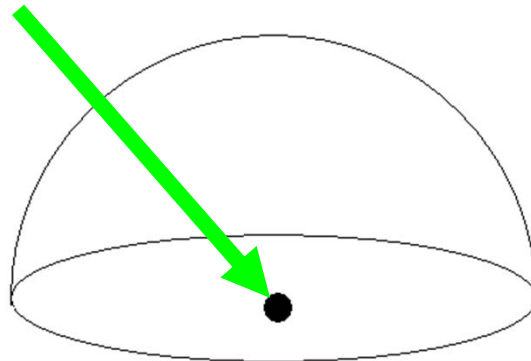
## Rendering Equation

$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$



## Rendering Equation

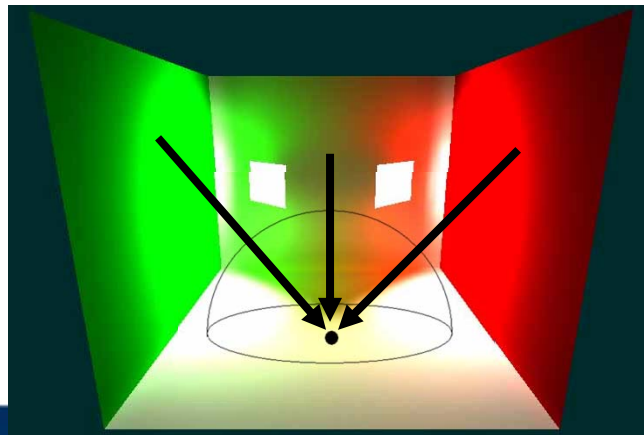
$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$



## Rendering Equation

$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) +$$

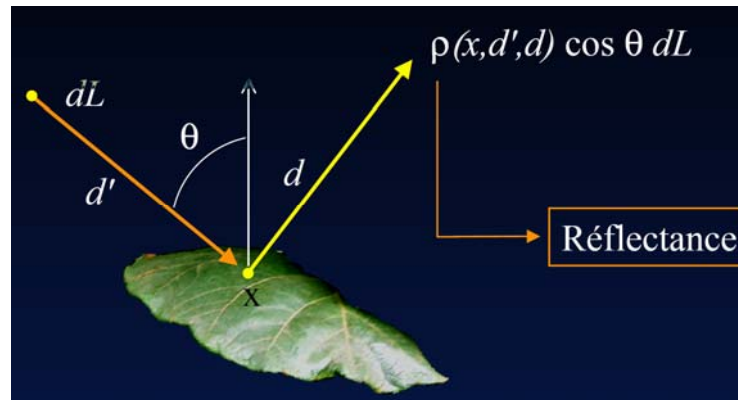
$$\int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$





## Rendering Equation

$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$



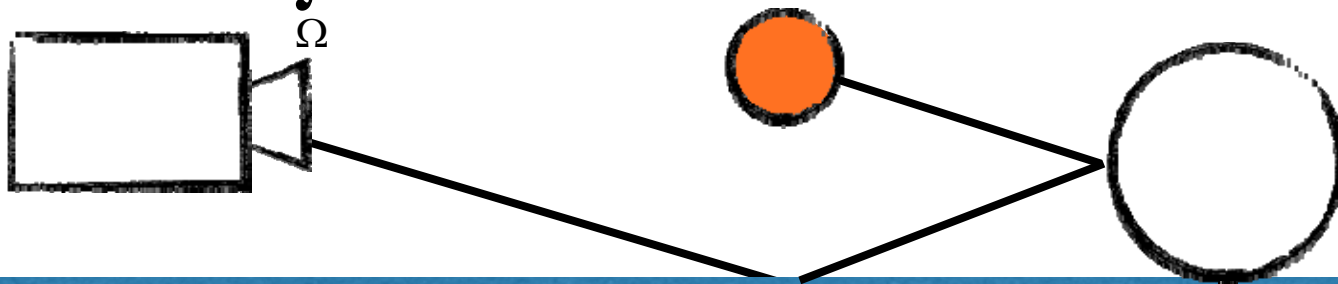
## Rendering Equation

$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) + \int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$

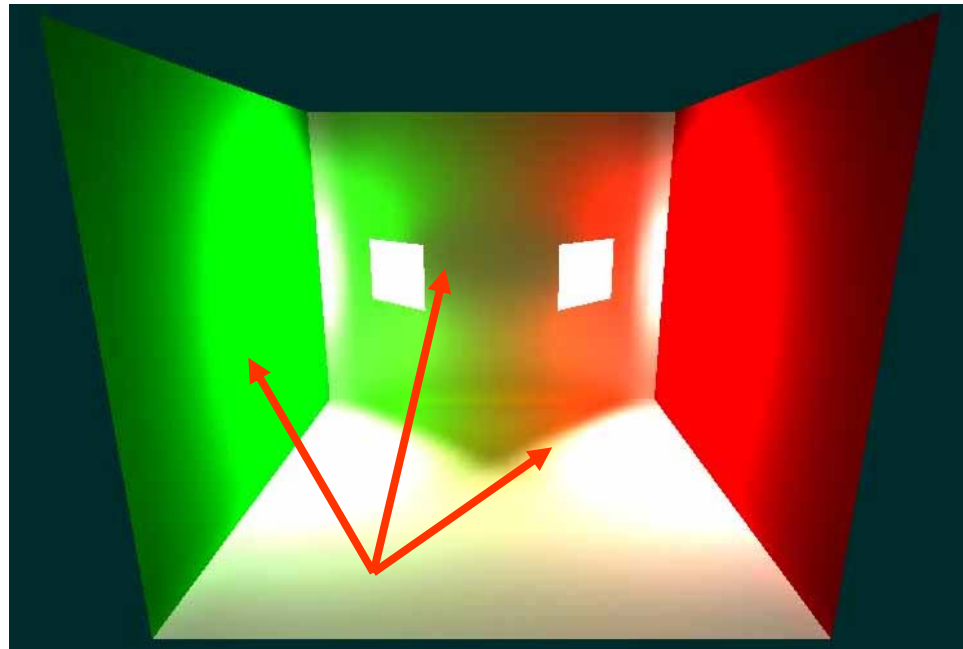
## Rendering Equation

$$L(x, \theta_0, \varphi_0) = L_e(x, \theta_0, \varphi_0) +$$

$$\int_{\Omega} \rho_{bd}(x, \theta_0, \varphi_0, \theta, \varphi) L_i(x, \theta, \varphi) \cos \theta d\omega$$



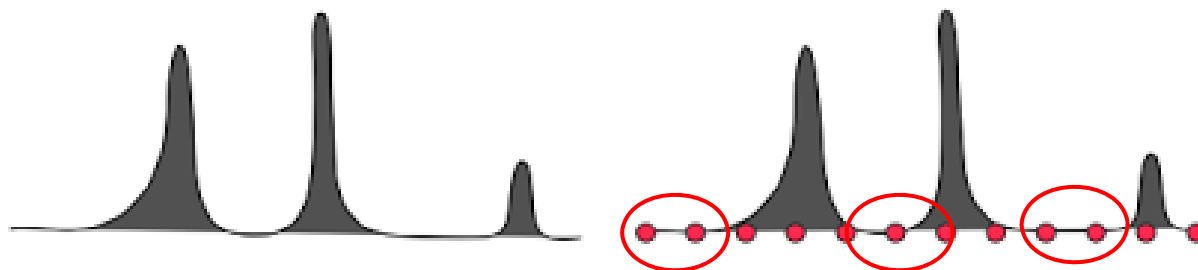
# Importance Sampling



“Shoot in the right direction”

## Importance Sampling

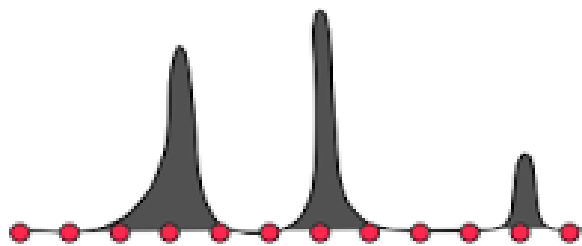
- Uniform sampling of a function?



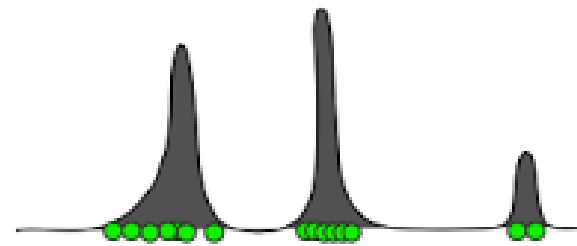
Uniform  
distribution

## Importance Sampling

- Uniform sampling of a function?

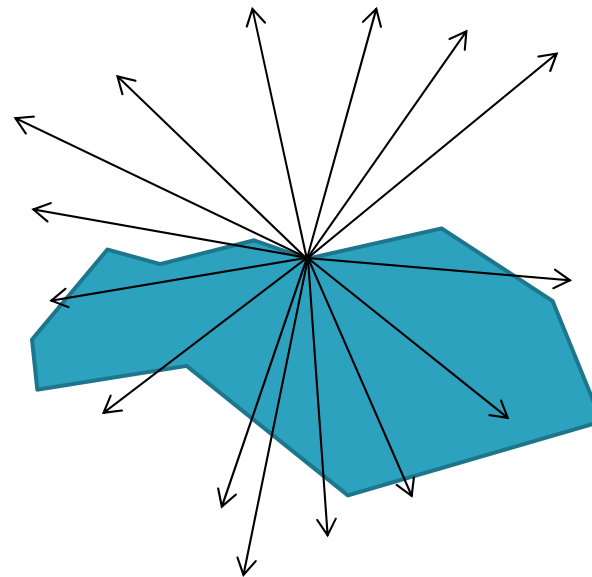


Uniform  
distribution



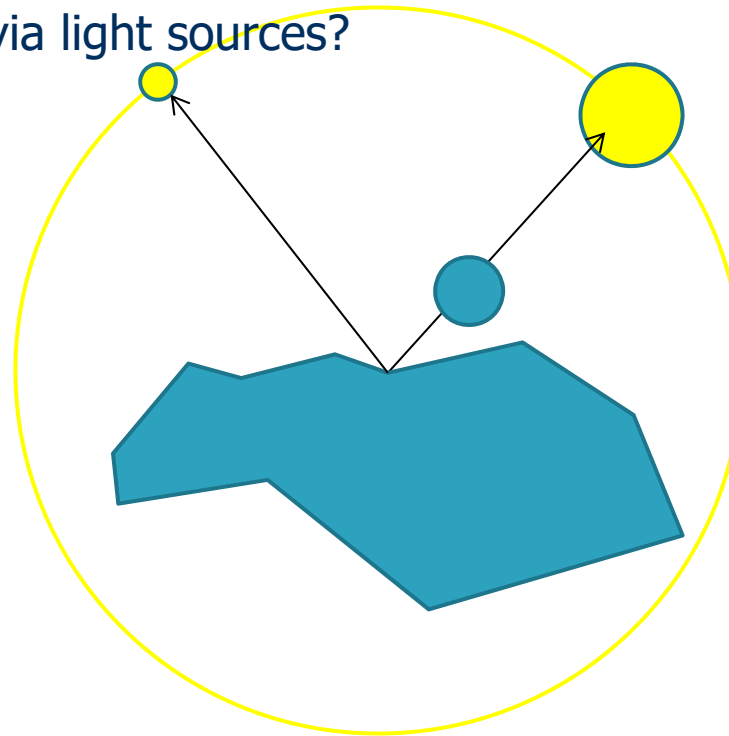
Importance  
sampling

# Importance Sampling



## Importance Sampling

- Steer sampling via light sources?

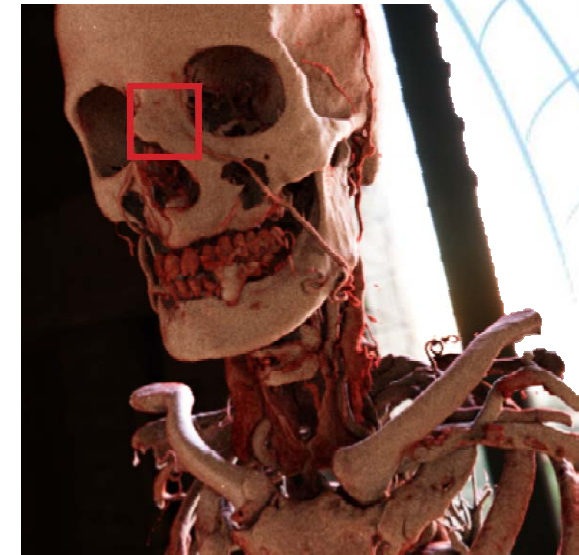




[Kroes, Eisemannx2 - GI2015] , Sweeney Award Winner  
[v. Radziewski, Kroes, Eisemannx2 - TVCG 2016]

## Importance Sampling

- Same amount of rays



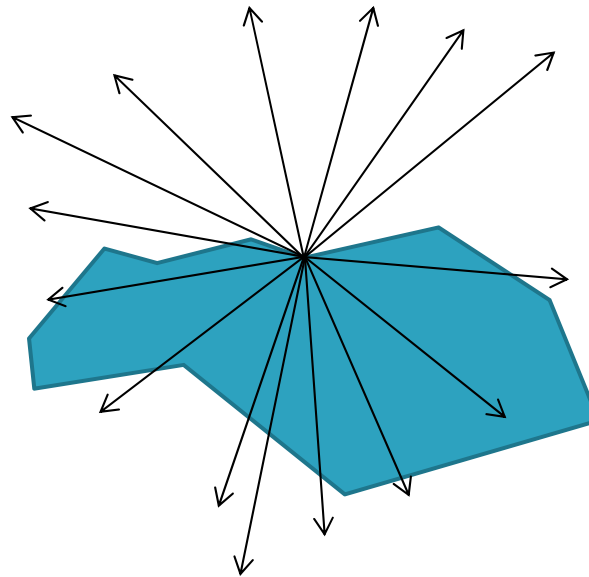
Two-step= Light and Visibility together are used for sampling



[Kroes, Eisemannx2 - GI2015] , Sweeney Award Winner  
[v. Radziewski, Kroes, Eisemannx2 - TVCG 2016]

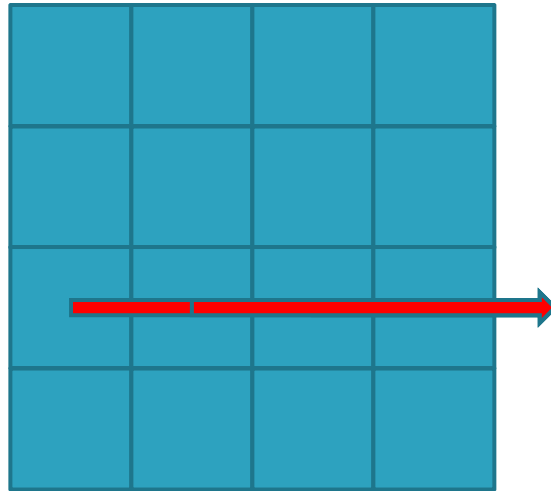
## How to determine visibility?

- Shooting rays from every point is too expensive



## Sweeping Solution

- Fix a random direction:

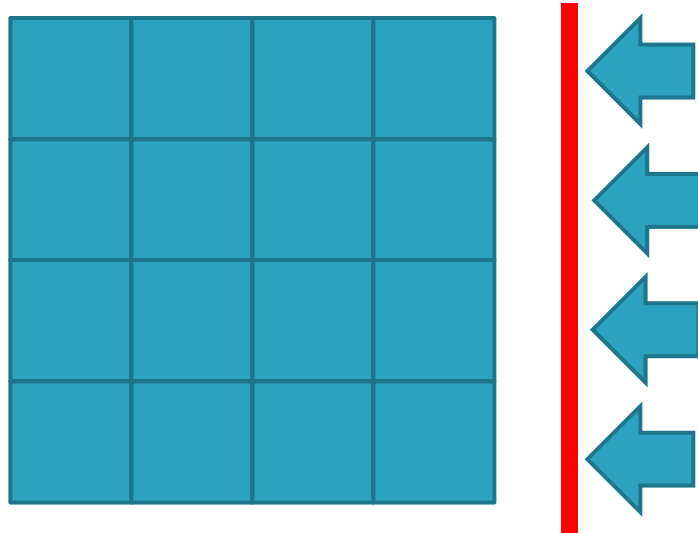


[Kroes, Eisemannx2 - GI2015]

[v. Radziewski, Kroes, Eisemannx2 - TVCG 2016]

## Sweeping Solution

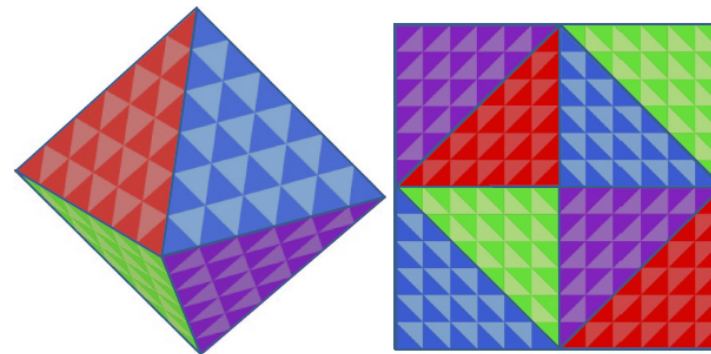
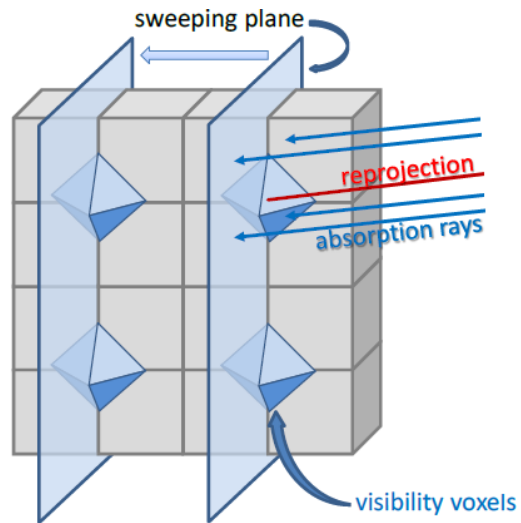
- Accumulate visibility in a single sweep for all voxels



[Kroes, Eisemannx2 - GI2015]

[v. Radziewski, Kroes, Eisemannx2 - TVCG 2016]

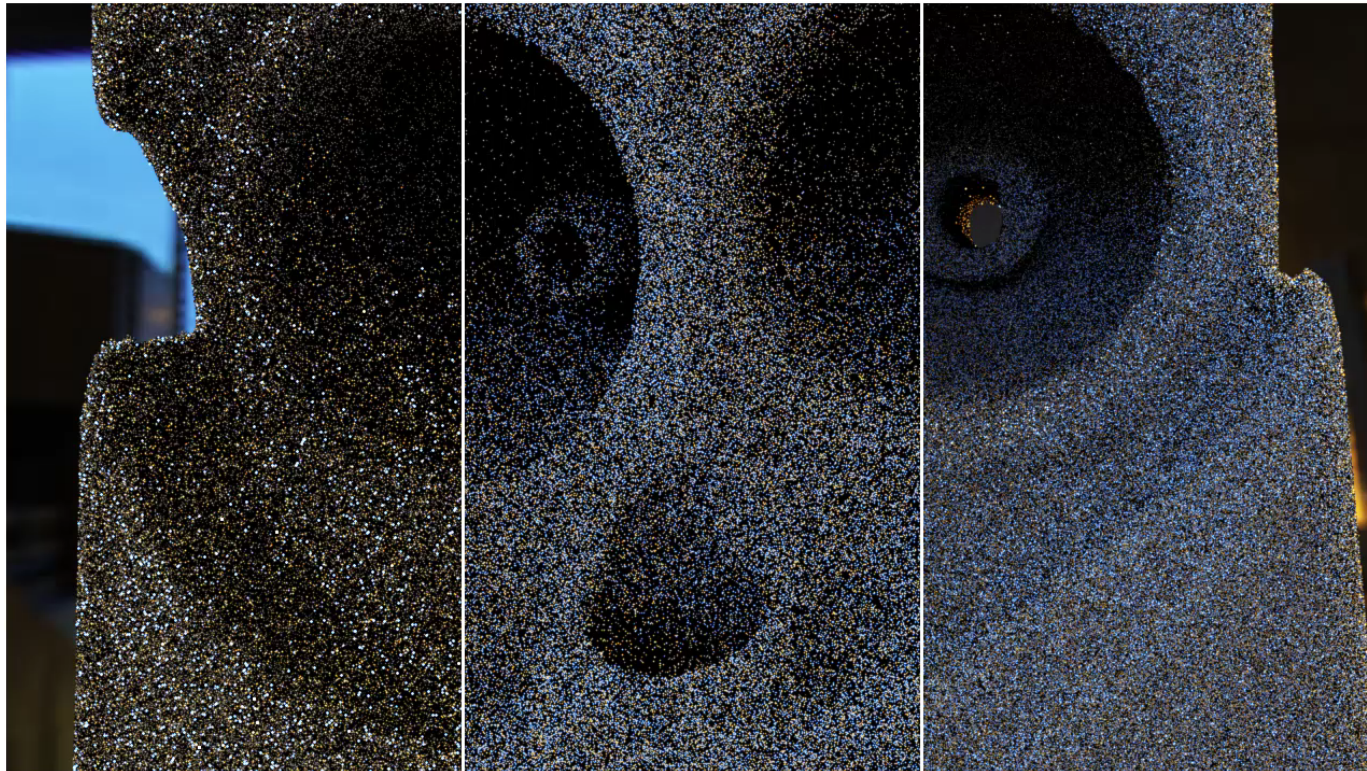
## Store Visibility



- Fast parallelized scheme for image-based visibility information



## Convergence with our importance sampling



[Bauszat, Eisemannx2, Magnor – Eurographics 2015]

## Light Reconstruction

10 mins:



2 mins:

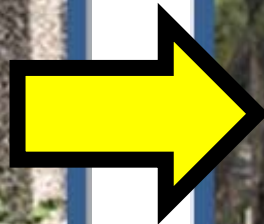


“What signal is likely, given my observations?”



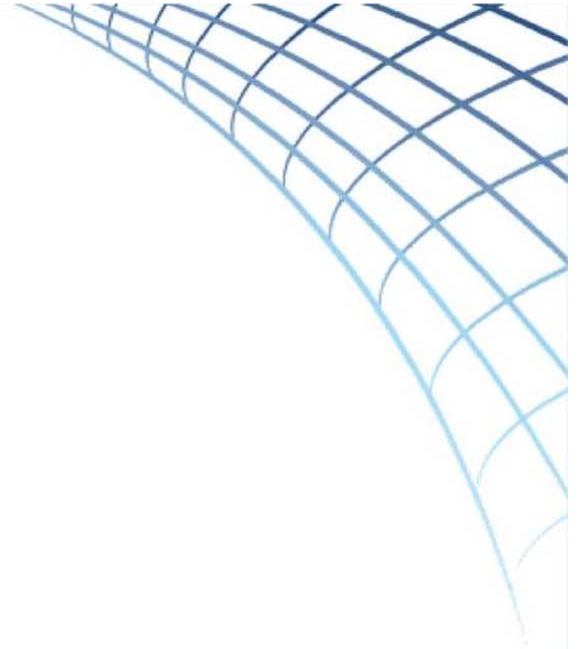
[Bauszat, Eisemannx2, Magnor – Eurographics 2015]

## Light Reconstruction



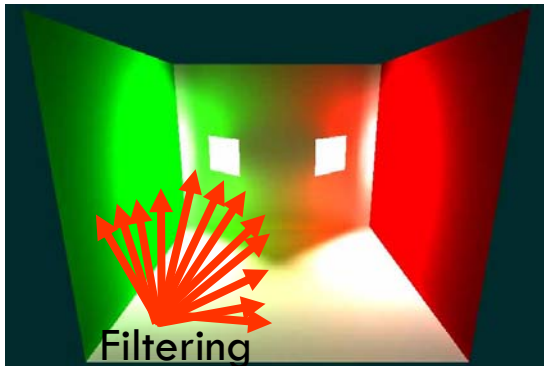


# How can we go real-time?

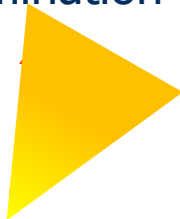


[Crassin, Neyret, Sainz, Green, Eisemann, PG 2012 ]

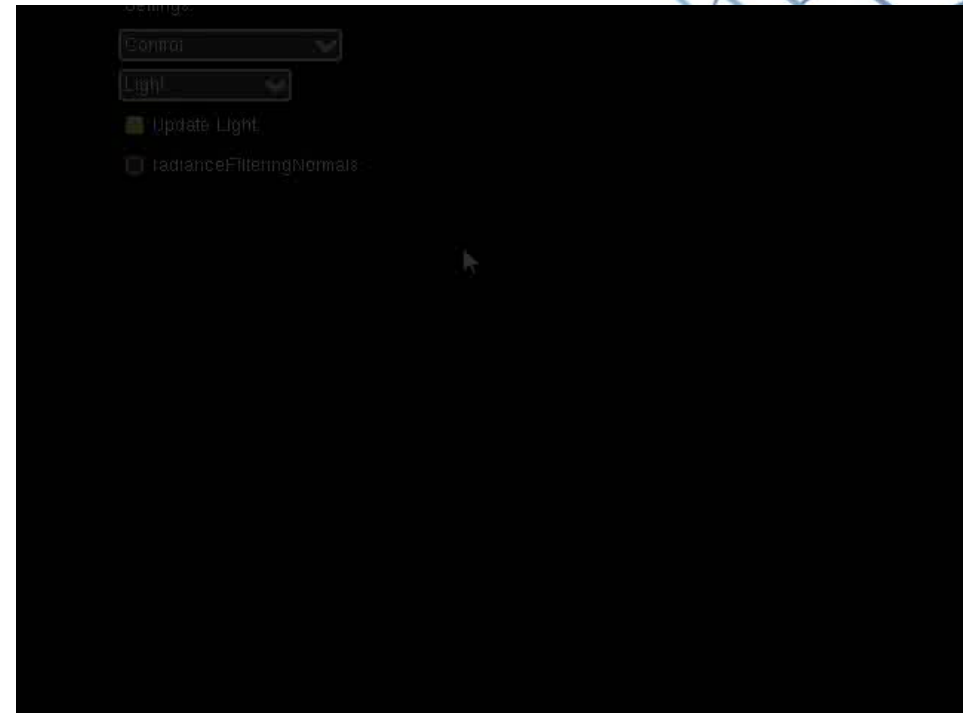
## Voxel-Cone Tracing



- Illumination Filtering



Filtering as approximation of many rays



Basis for GI in Unreal Engine 4 & NVIDIA VXGI



Based on:

[Crassin, Neyret, Sainz, Green, Eisemann, PG 2012 ]

## Global Illumination

Unreal Engine 4 / Cry Engine 2015

NVIDIA VXGI 2015 and VXAO 2016

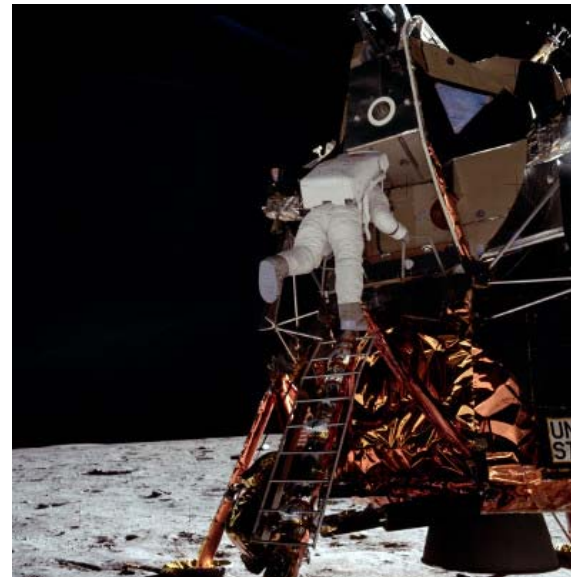


Fig 6. Rise of the Tomb Raider rendered with VXAO and HBAO+



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# NVIDIA Debunks the Moon Landing...



Copyright NVIDIA



Koninklijk Instituut Van Ingenieurs

## NVIDIA Debunks the Moon Landing...



Copyright NVIDIA



Koninklijk Instituut Van Ingenieurs

## Exposure Render

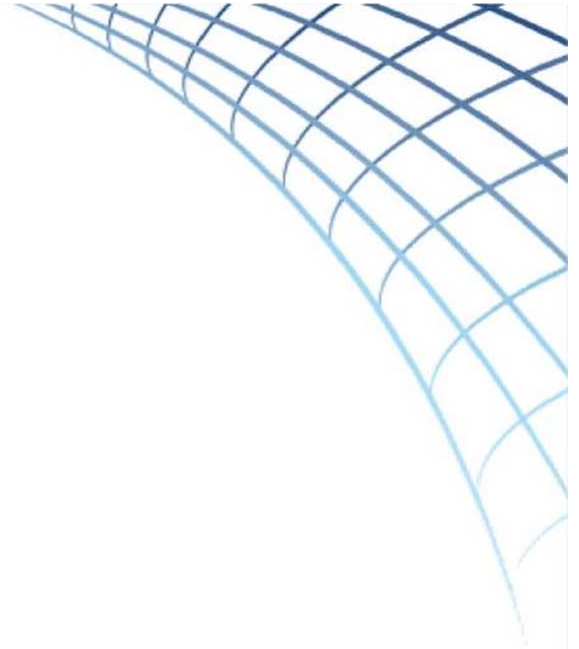
- Integrates similar methods for volume rendering



**How many images per second do we need?**



**Questions?**

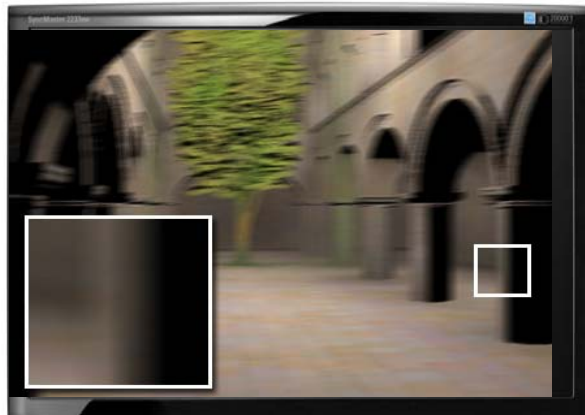




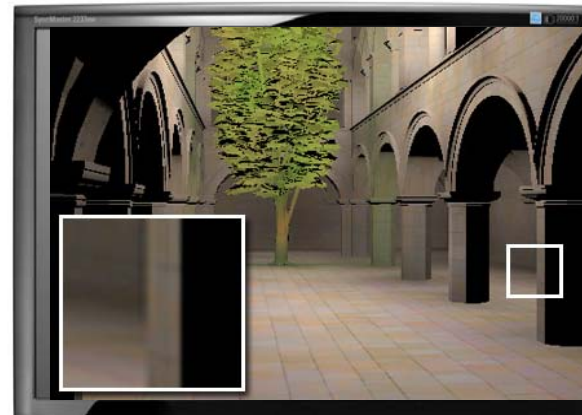
## How many images per second do we need?

- More images:
  - Increased detail perception / Blur reduction
  - Increased task performance

40 Hz

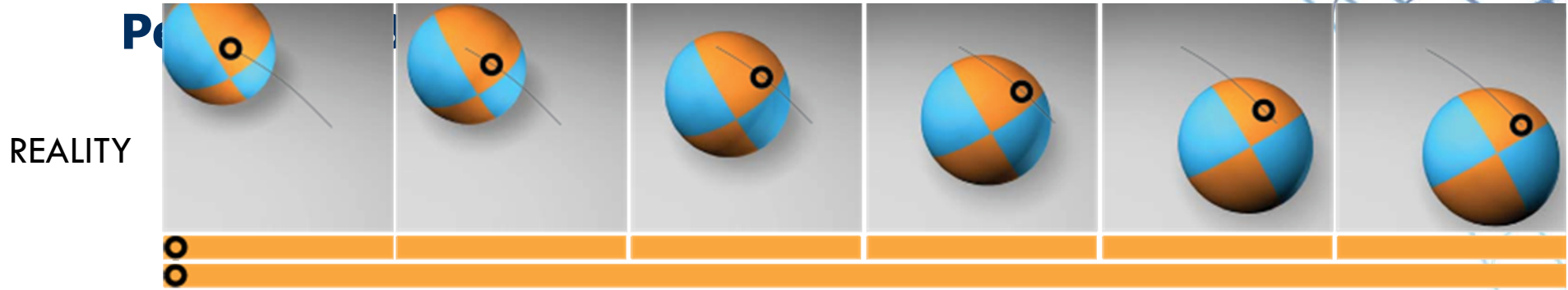


120 Hz



[Stengel, Bauszat, Eisemann x2, Magnor – TVCG2015]

[Didyk, Eisemann, Ritschel, Myszkowski, Seidel – Eurographics 2010]



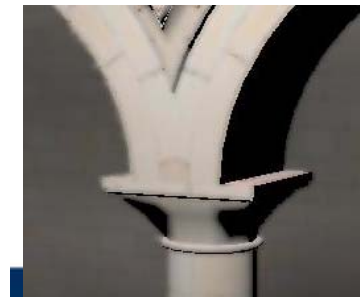
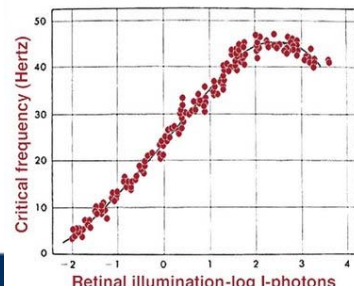
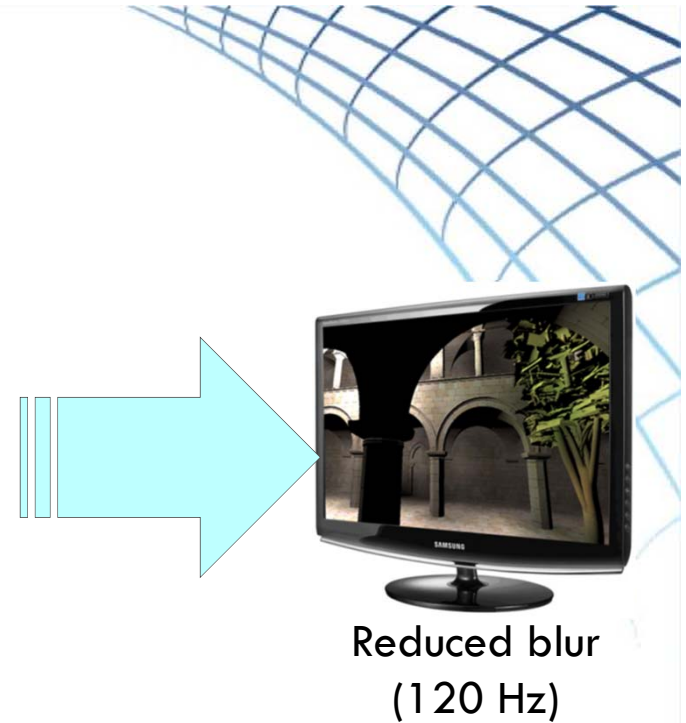
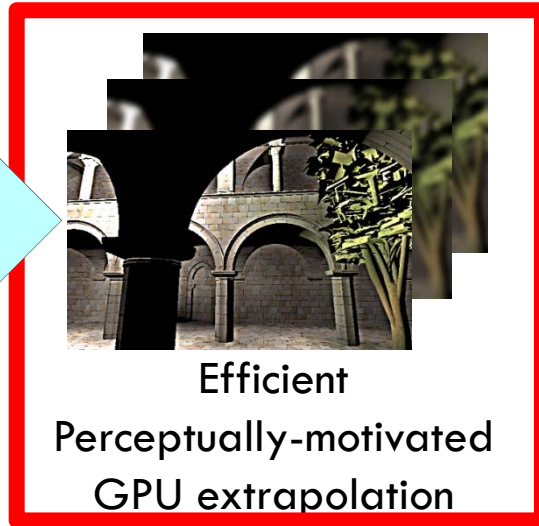
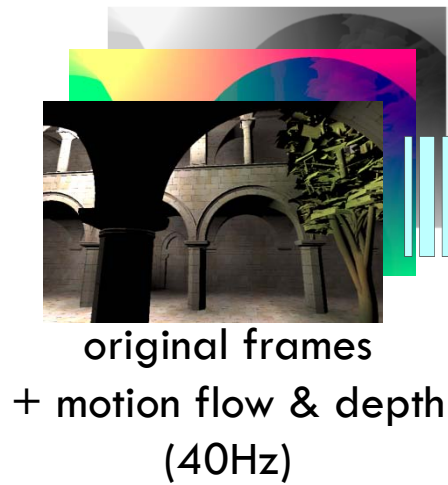
**“Simple” solution: Produce more frames...**



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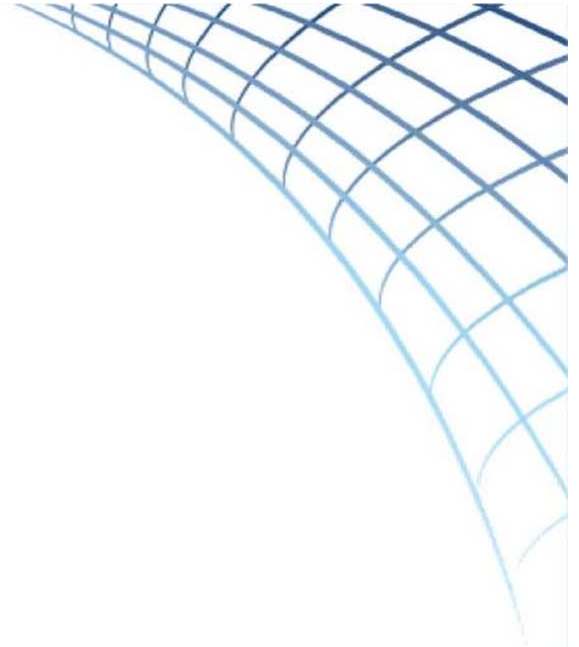
[Didyk, Eisemann, Ritschel, Myszkowski, Seidel – Eurographics 2010]

## Perceptual Upsampling



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# Image Decomposition



## Combine high-frequency information

Frame 0



Frame 1



Frame 2



- At 120 Hz indistinguishable from original

## Combine high-frequency information

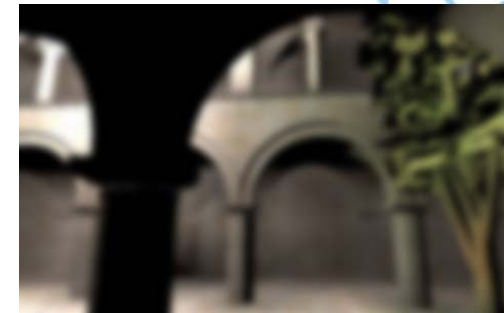
Frame 0



Frame 1



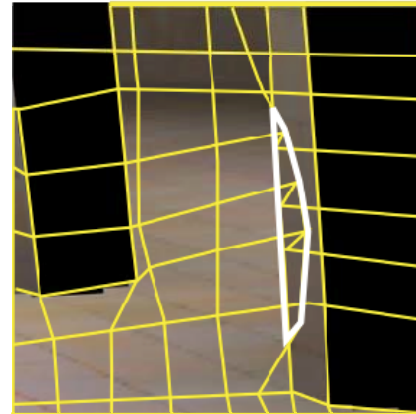
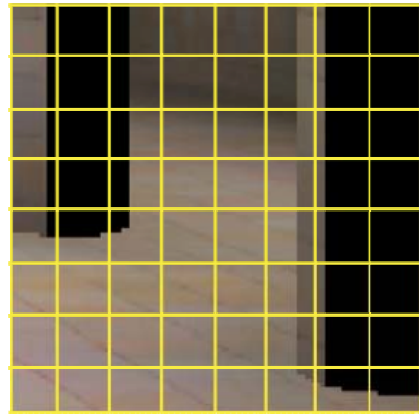
Frame 2



- Our idea: Turn the principle around

## Produce frames via simple warping

- Transform grid via motion flow (respect depth)

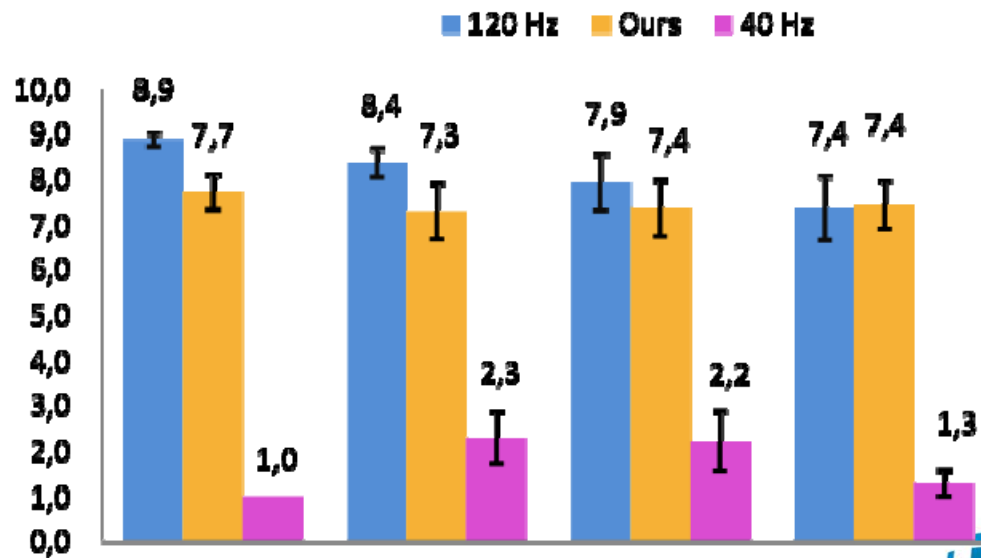
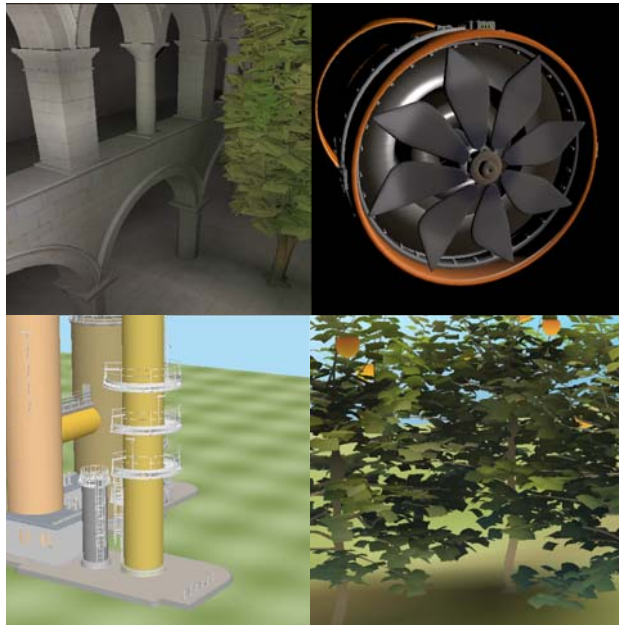


~1 ms in full HD



# Perceptual Upsampling

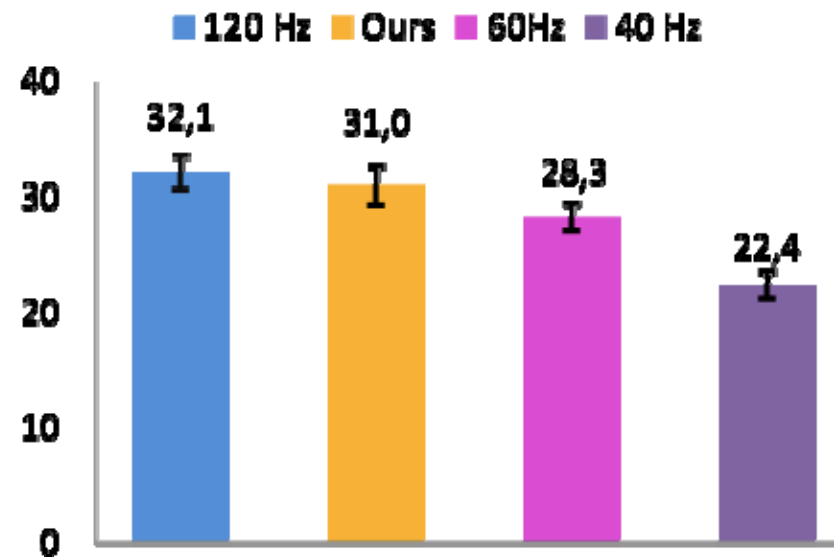
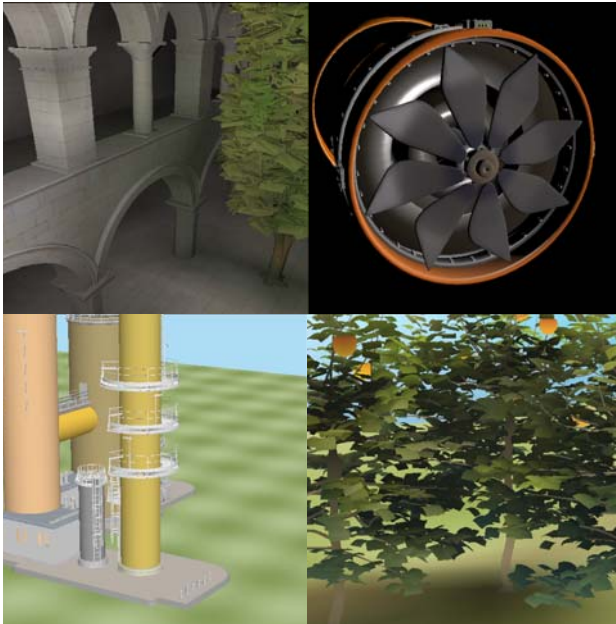
- Task Performance





## Perceptual Upsampling

- Task Performance



[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

## Ghosting in HFR Videos

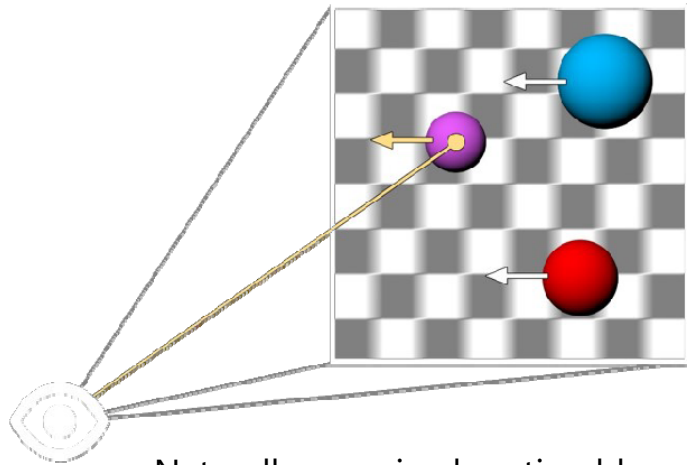


60  
fps

**DELFT  
DATA  
SCIENCE**

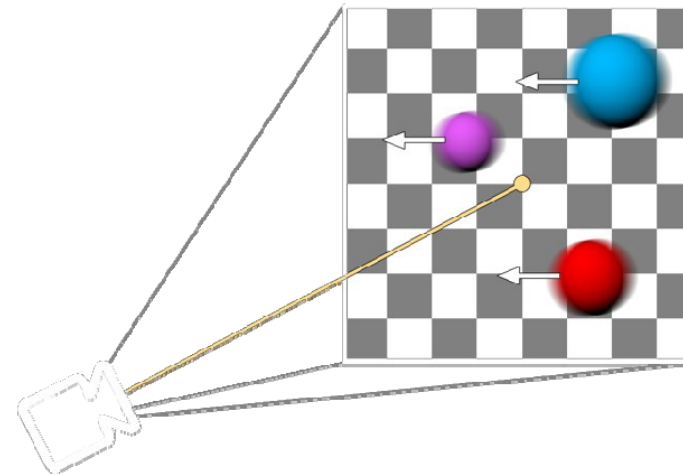
[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

## Blur mismatch between Camera and Eye



Naturally perceived motion blur

- eye tracking → high-detail
- static background is blurred
- which leads to ghosting for 'sharp' backgrounds over duration of a frame



Captured Motion Blur

- static camera
- moving objects

[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

## Blur mismatch between Camera and Eye

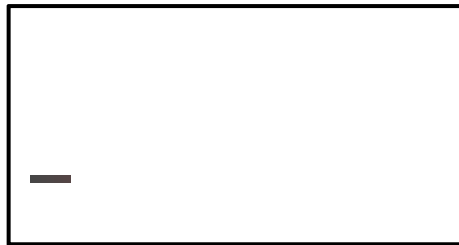
Stimulus



[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

## Blur mismatch between Camera and Eye

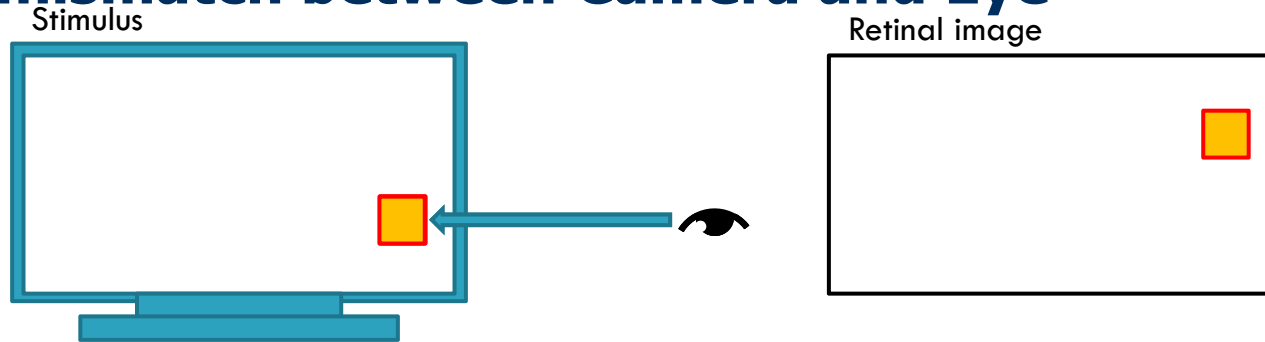
Stimulus



Motion blur recorded  
by camera

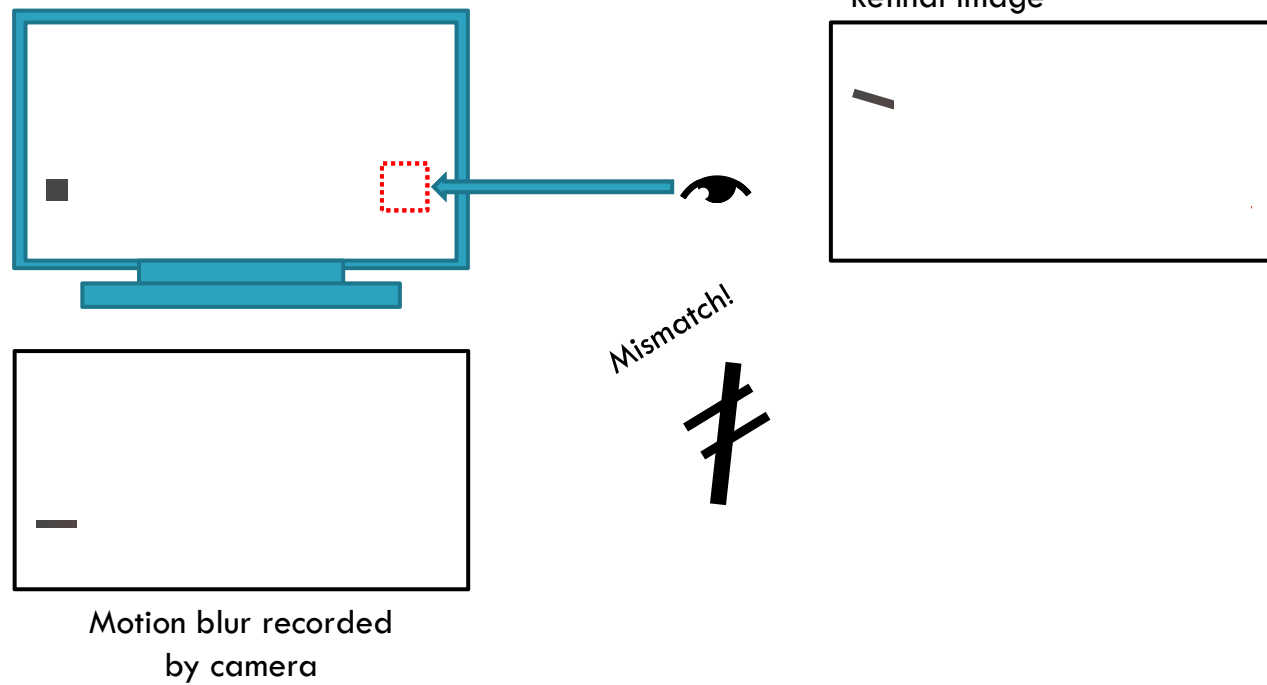
[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

## Blur mismatch between Camera and Eye



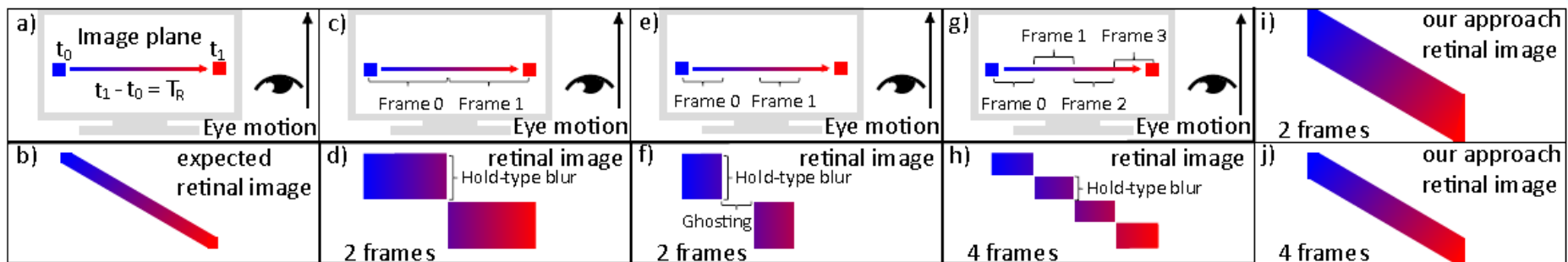
[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

## Blur mismatch between Camera and Eye



[Stengel, Bauszat, Eisemannx2, Magnor TVCG2015]

# Blur mismatch between Camera and Eye





**Please follow the face of the statue in the following videos.**



Short exposure / 60 fps



Long exposure / 60 fps



Perceptual filter / 60 fps



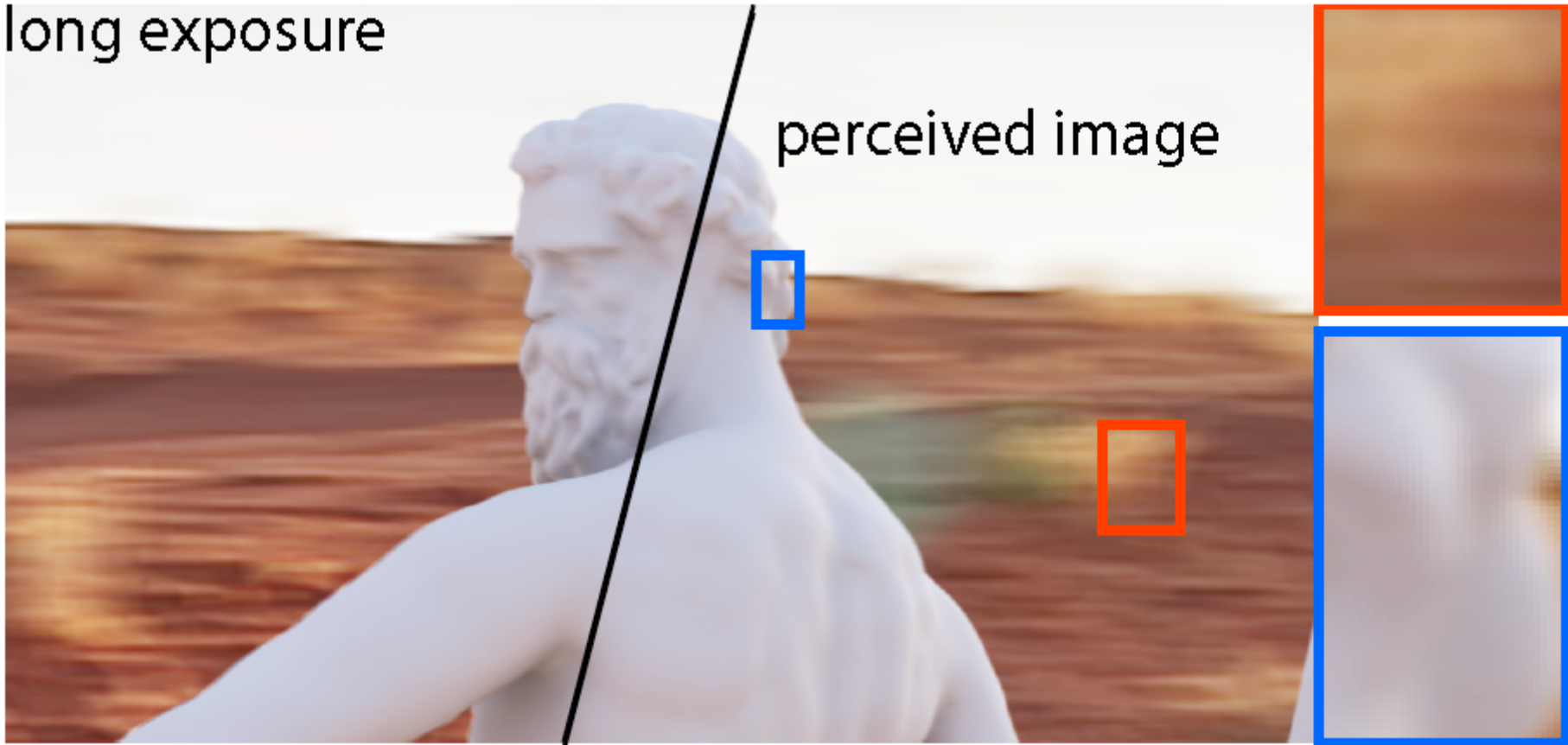
short exposure

perceived image



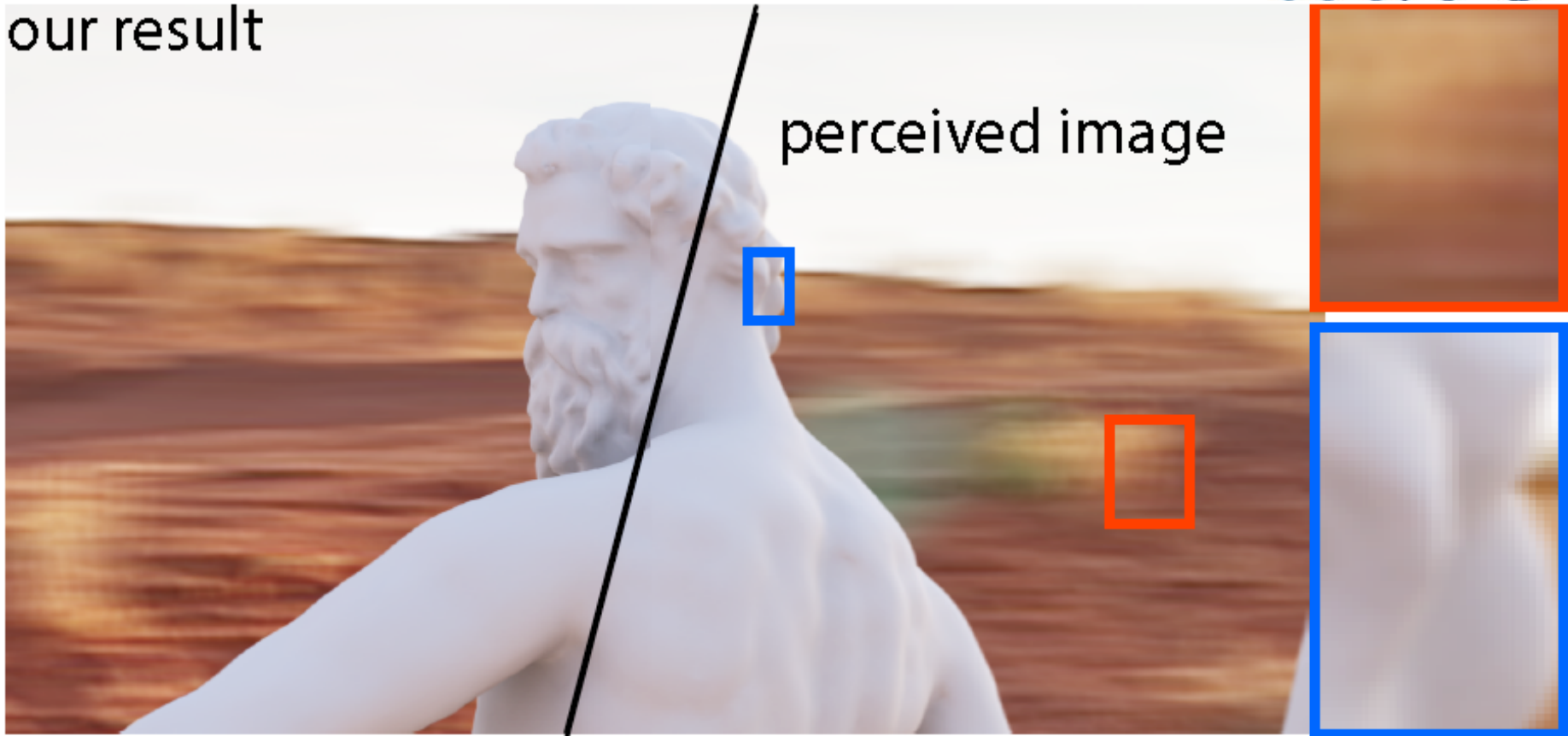
long exposure

perceived image



our result

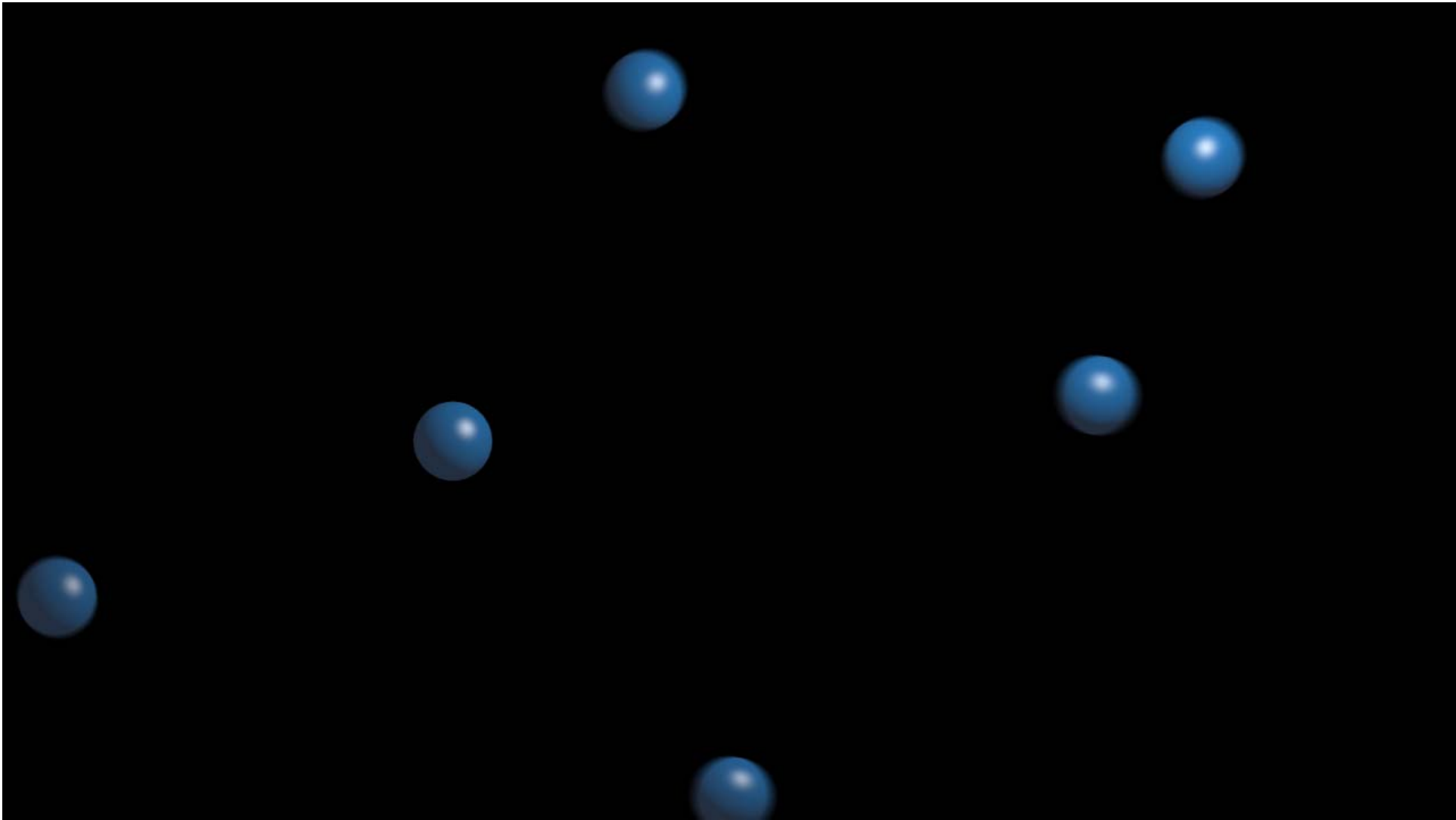
perceived image

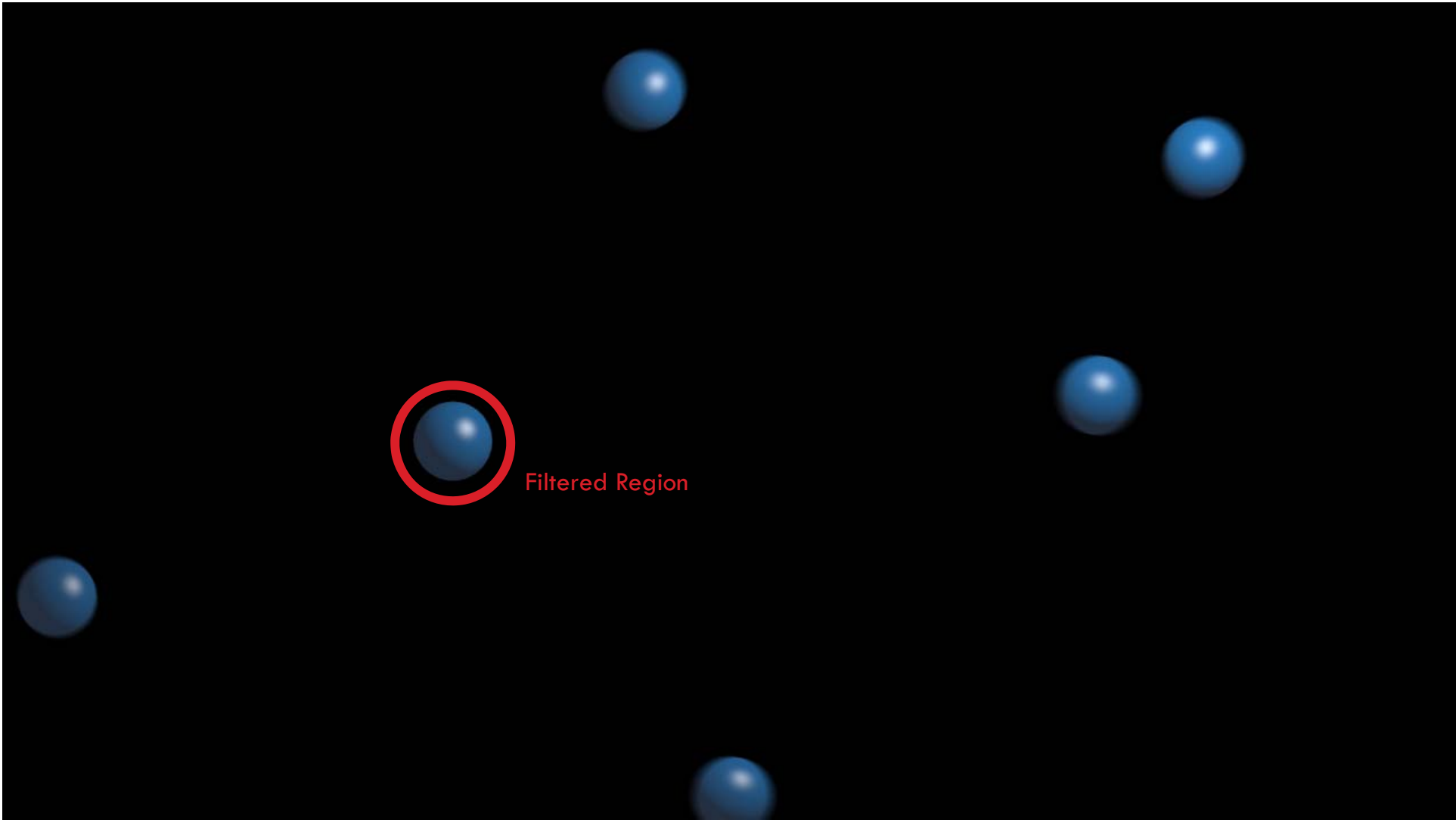


**Can we use our perceptual filter to influence eye motion?**

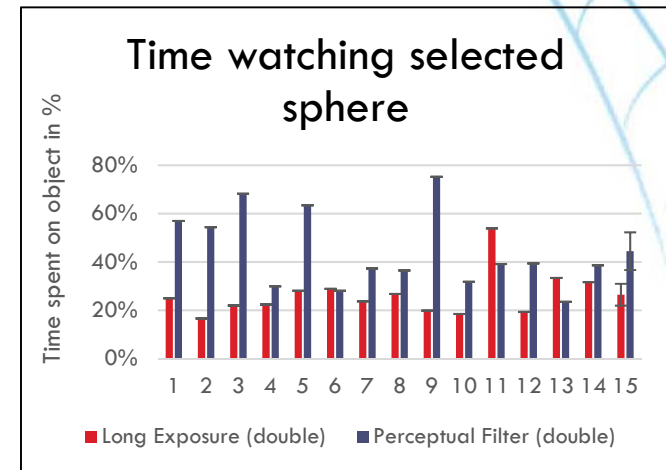
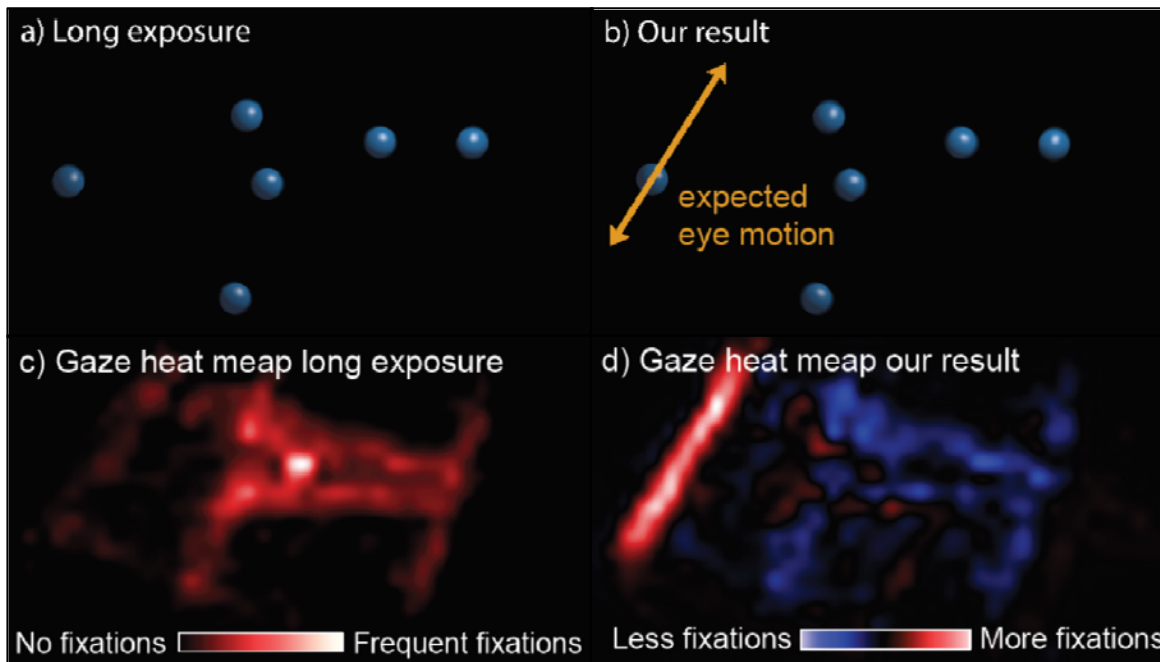








# Subtle Gaze Guidance







- We can influence where you look!
- Can we influence what you see?



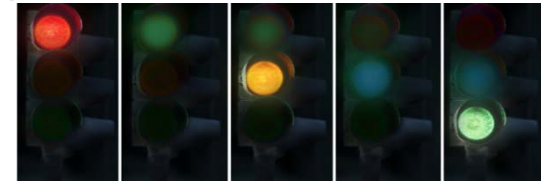
## Overcoming Physical Limitations

- Apparent Resolution Enhancement  
[Didyk, Eisemann, Ritschel, Myszkowski, Seidel – SIGGRAPH 2010]  
[Templin, Didyk, Ritschel, Eisemann, Myszkowski, Seidel - SCCG 2011]

Resolution

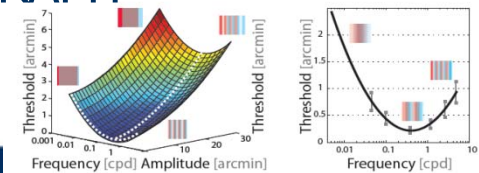
- A Computational Model of Afterimages  
[Ritschel & Eisemann - Eurographics'12]

Brightness

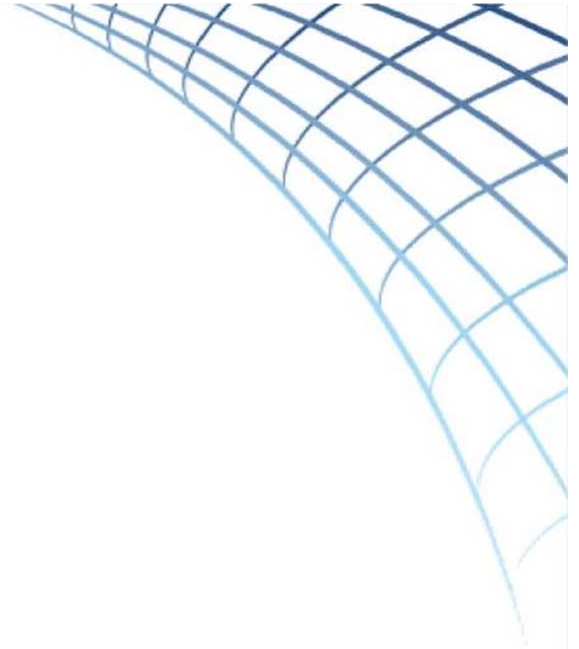


- A Perceptual Model for Disparity  
[Didyk, Ritschel, Eisemann, Myszkowski, Seidel - SIGGRAPH 2011/SIGAsia2012]

Stereo illusion



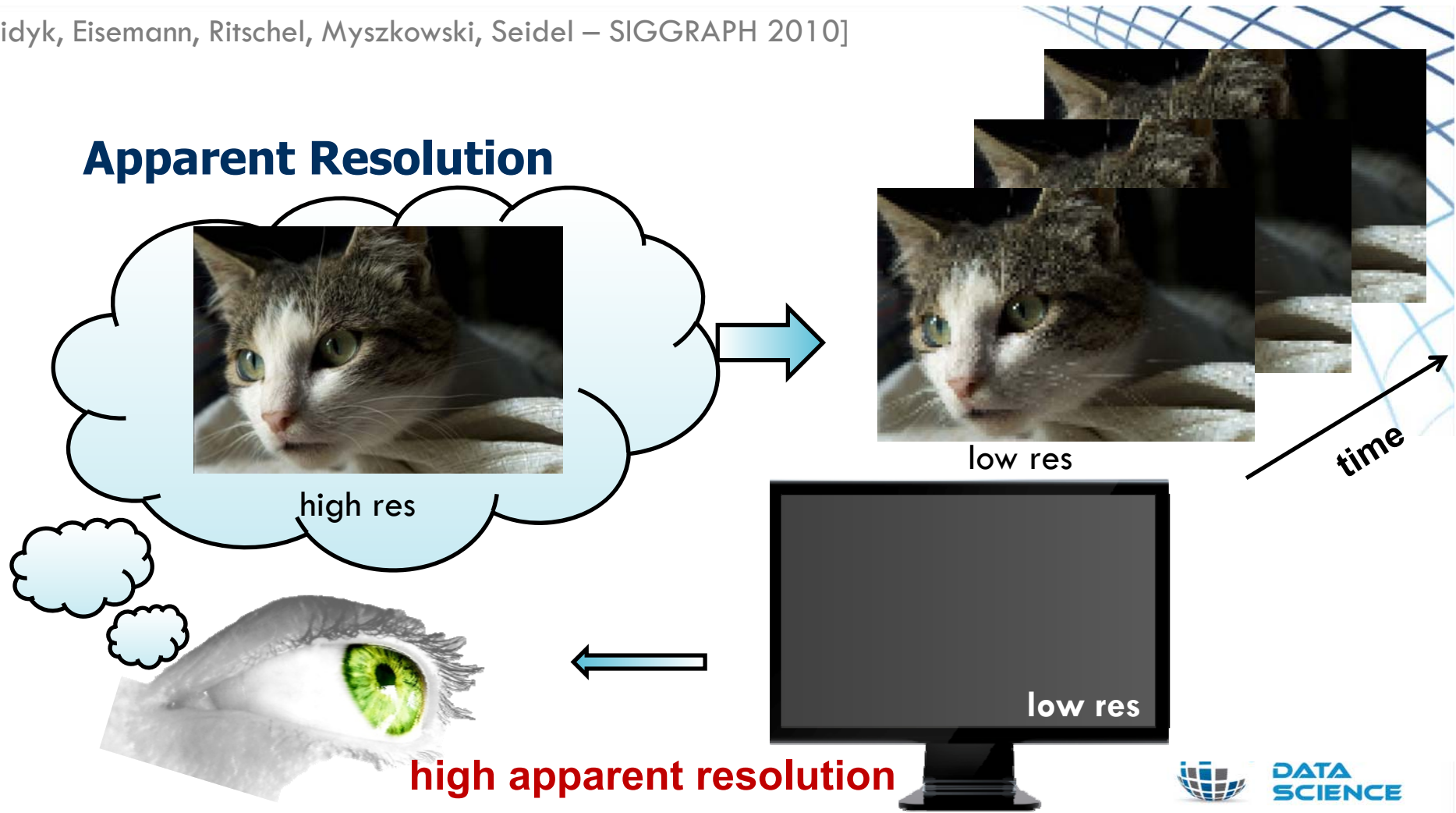
**Questions?**



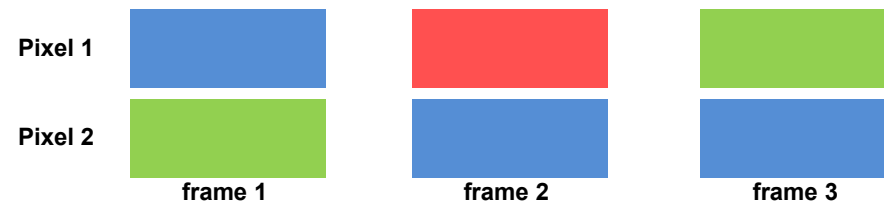
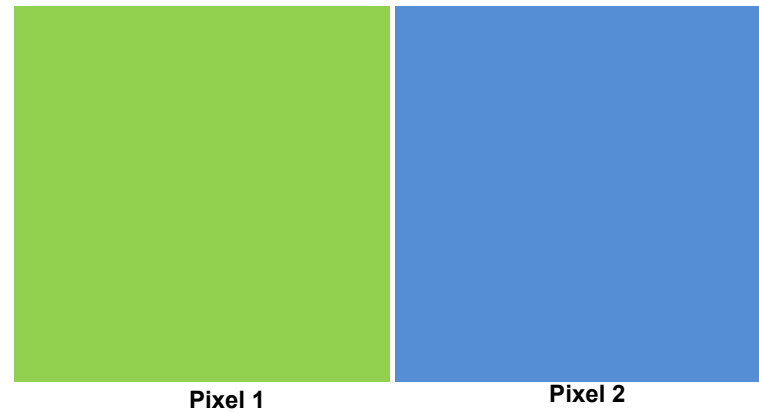


[Didyk, Eisemann, Ritschel, Myszkowski, Seidel – SIGGRAPH 2010]

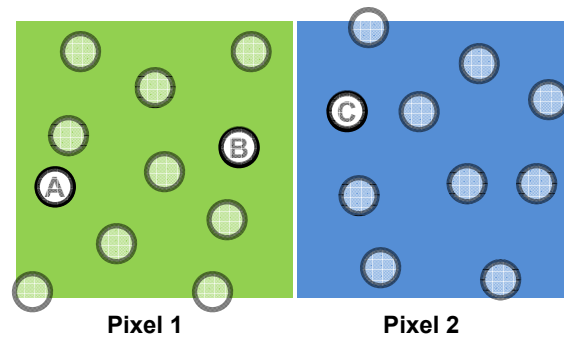
## Apparent Resolution



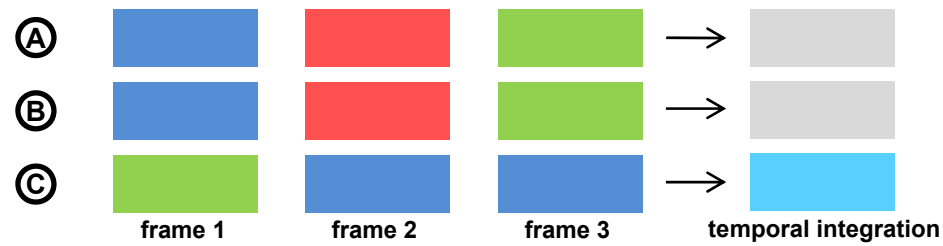
# Temporal Domain



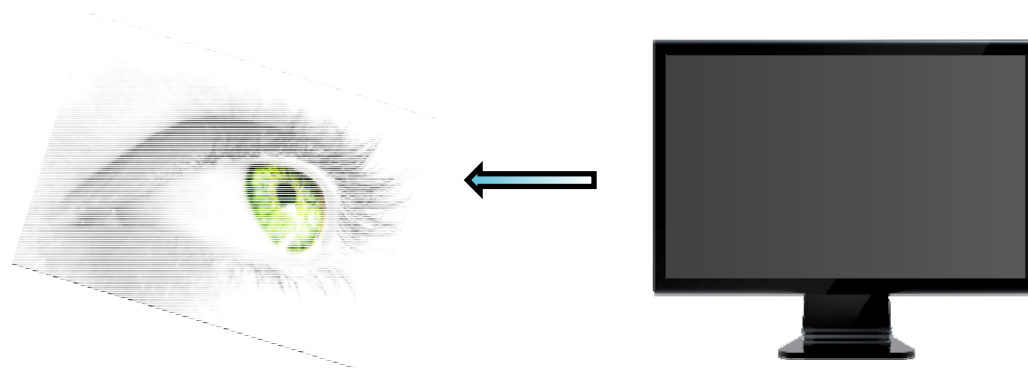
# Temporal Domain – static case



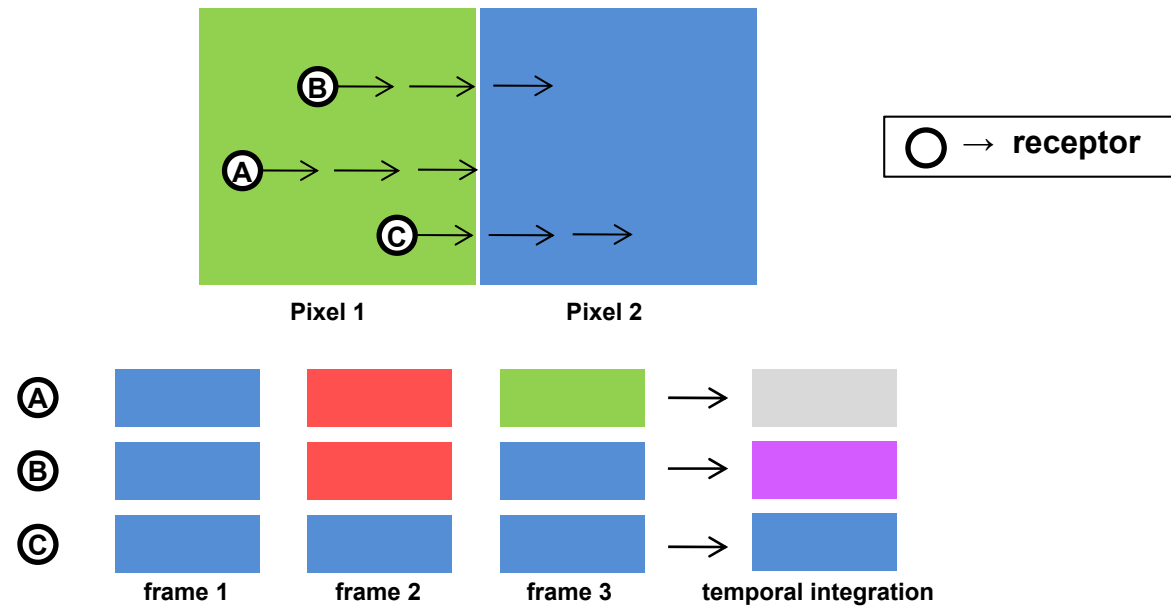
○ → receptor



## Temporal Domain – dynamic case

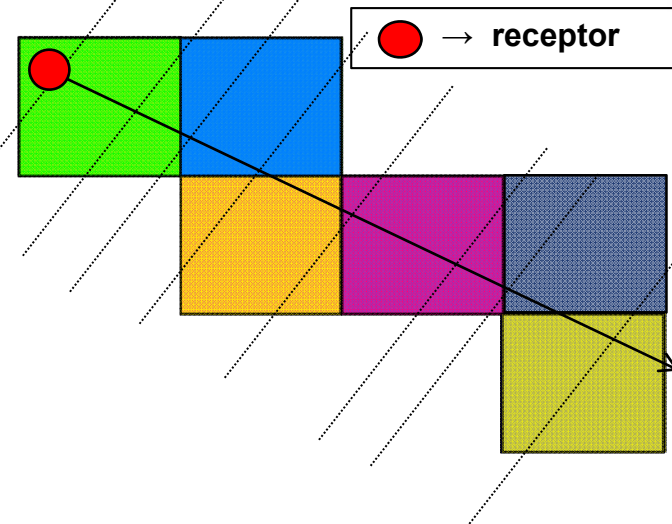


# Temporal Domain – dynamic case



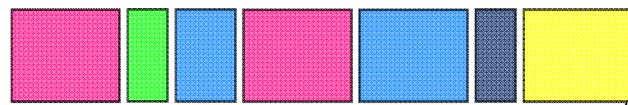
# Temporal Integration Model

Receptor signal:



# Temporal Integration Model

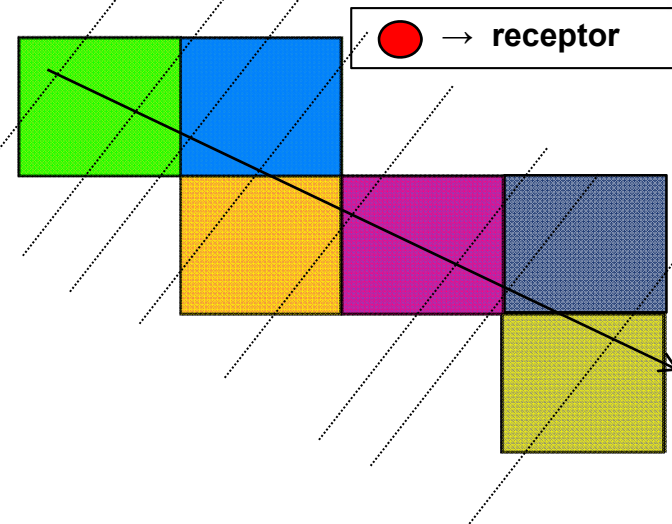
Receptor signal:



$$\sum_{i=0}^N w_i I(p(i), i)$$

segment
time  
 $N$  length
segment

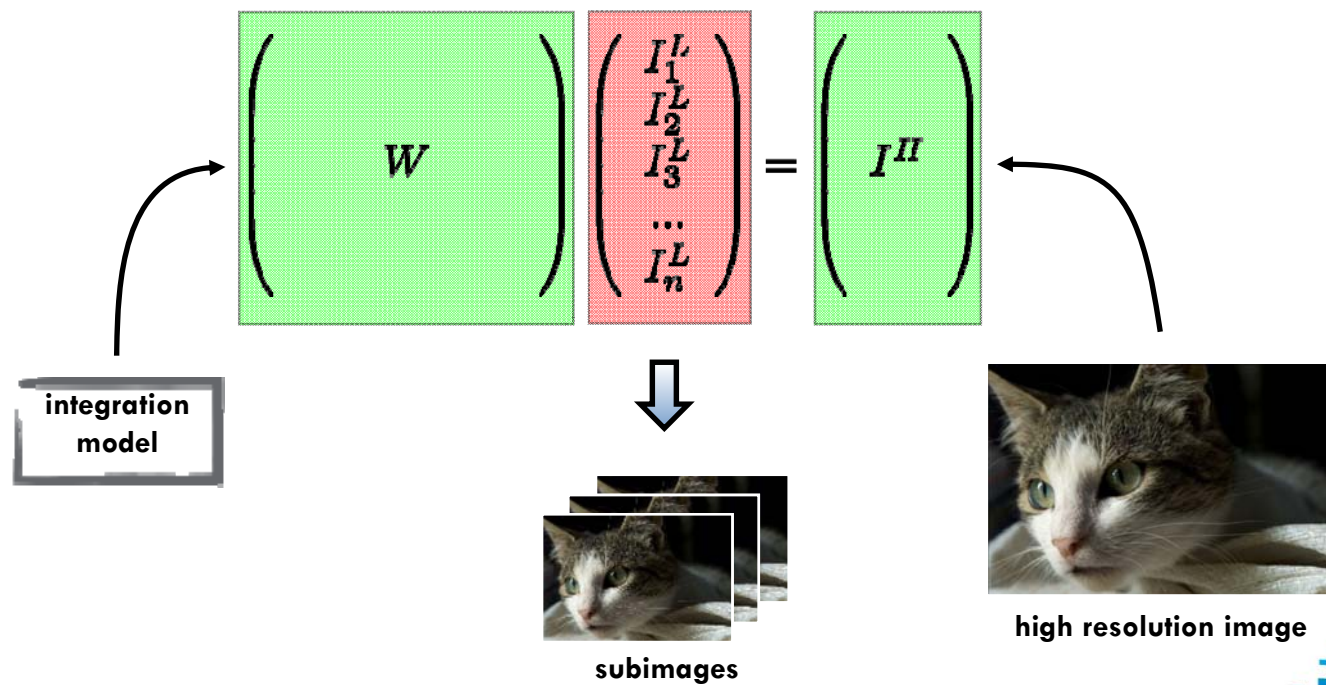
Observed  
color for  
segment  $i$



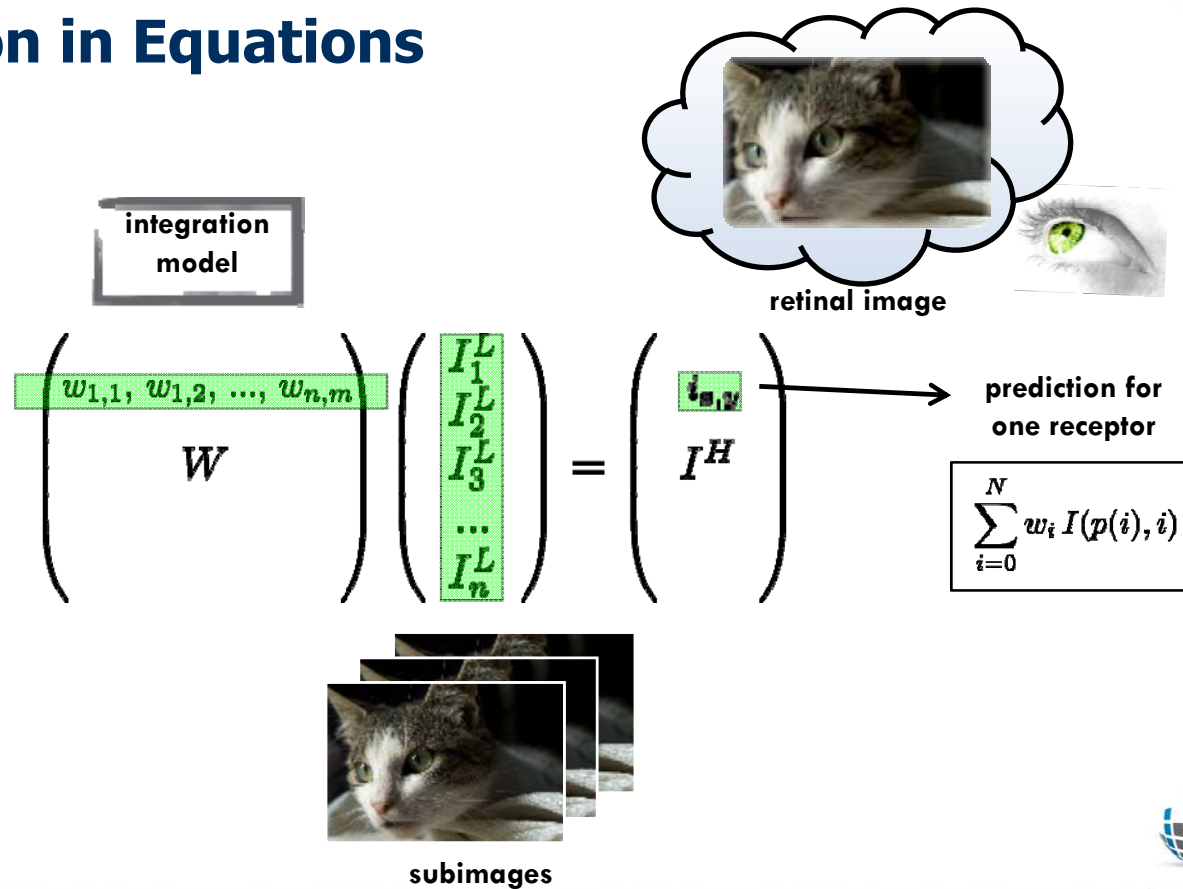




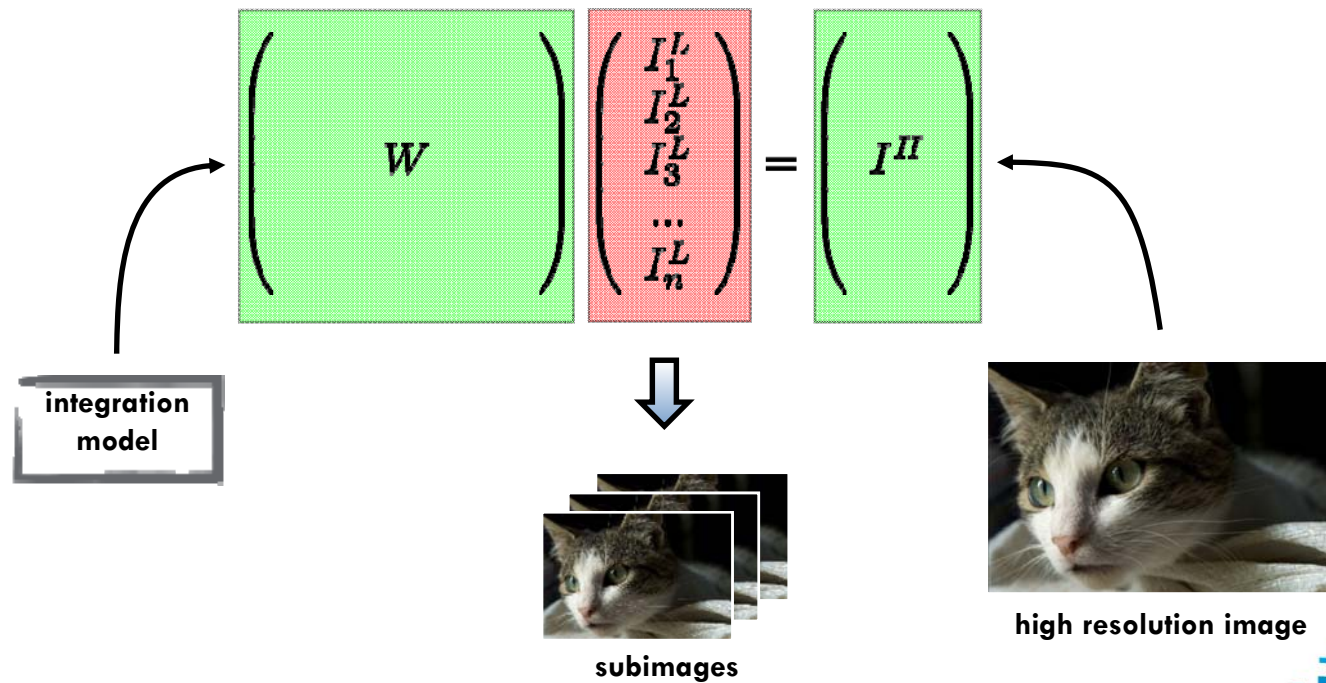
# Optimization Problem



# Prediction in Equations



# Optimization Problem



# Fusion Frequency

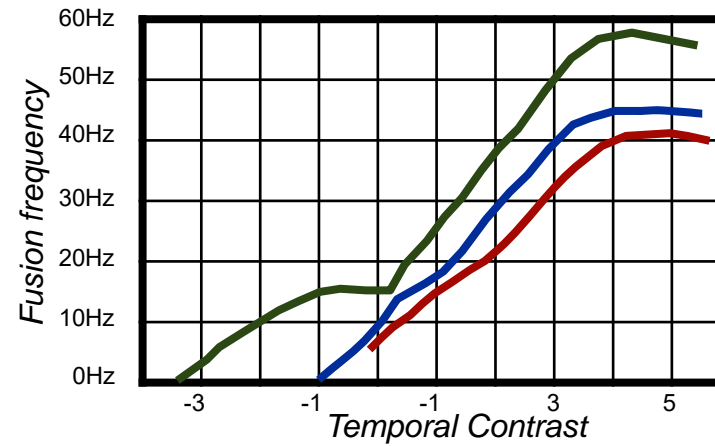
- Depends on
  - temporal contrast
  - spatial extent

● 19 deg

● 2 deg

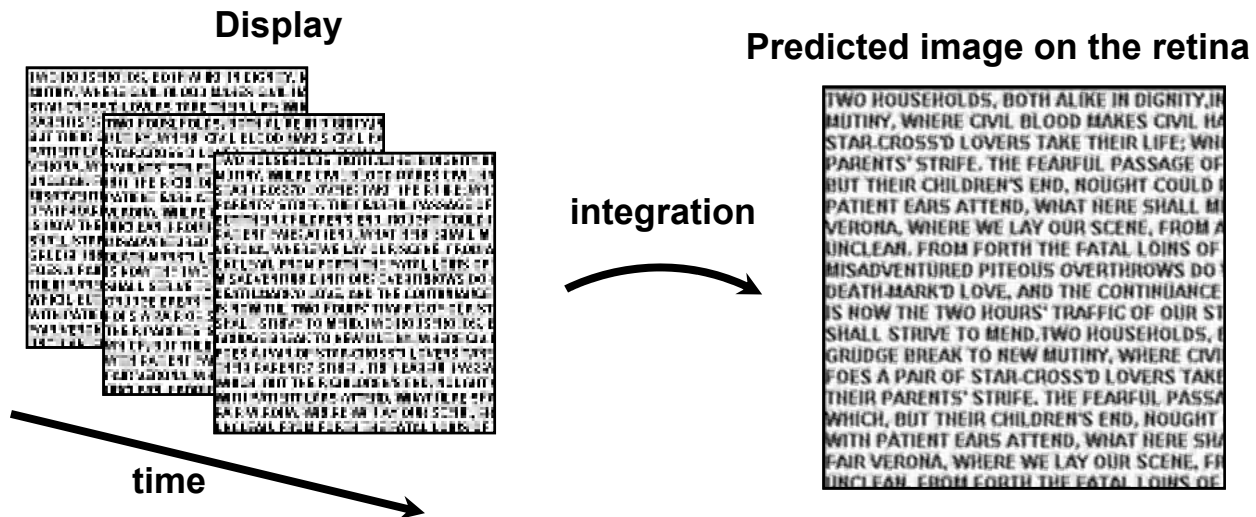
● 0.3 deg

⇒ 40Hz

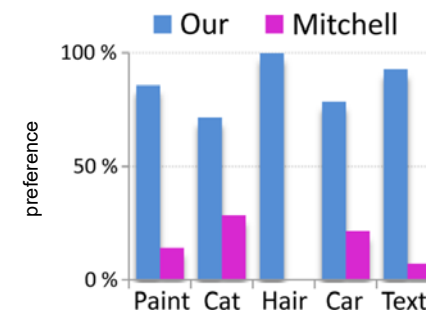
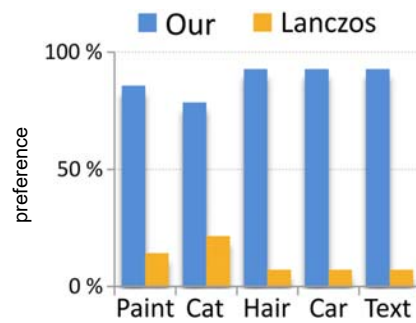


Critical Flicker Frequency - Hecht and Smith's data from Brown J. L. *Flicker and Intermittent Simulation*

# Optimization Result



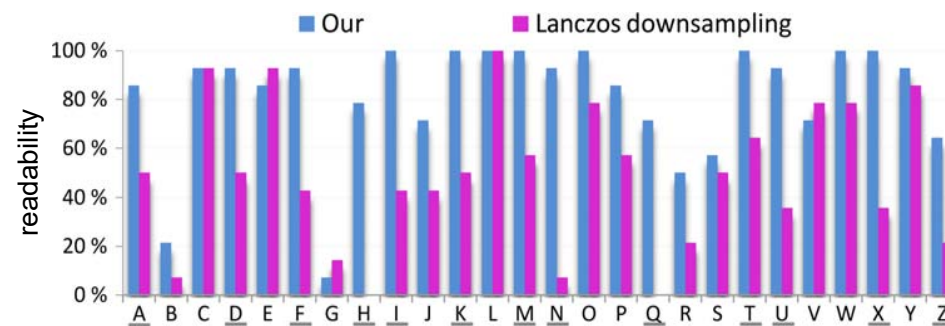
## Our vs. Previous Downsampling Techniques



## Example: Alphabet

**A B C D E F G H I J K L M N O P Q R S T U V W X Y Z**

Size: 2 x 3 pixels



- Applications:
  - scrolling text or maps on low resolution devices
  - stock tickers, news headlines

## Overcoming Physical Limitations

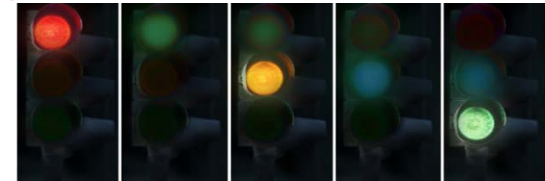
- Apparent Resolution Enhancement  
[Didyk, Eisemann, Ritschel, Myszkowski, Seidel – SIGGRAPH 2010]  
[Templin, Didyk, Ritschel, Eisemann, Myszkowski, Seidel - SCCG 2011]

Resolution

- A Computational Model of Afterimages

[Ritschel & Eisemann - Eurographics'12]

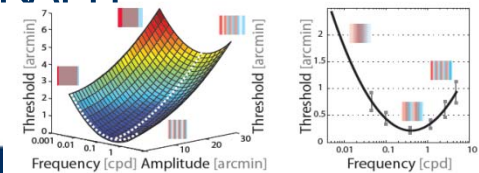
Brightness



- A Perceptual Model for Disparity

[Didyk, Ritschel, Eisemann, Myszkowski, Seidel - SIGGRAPH 2011/SIGAsia2012]

Stereo illusion





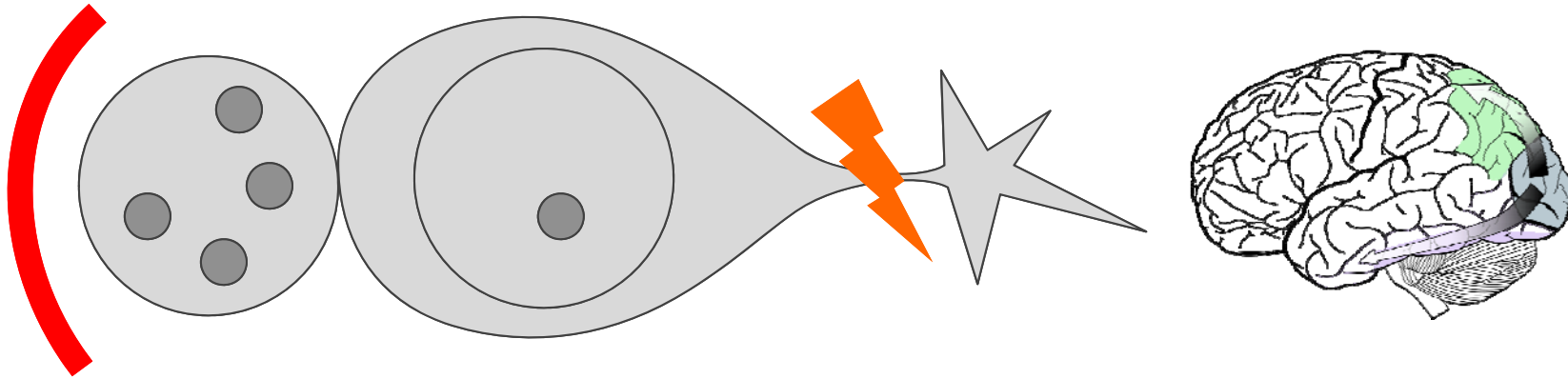
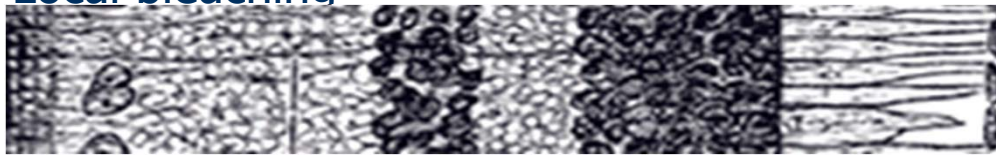
## Example

- Focus on the dark spot...



## Chromatic Adaptation

- Local bleaching



Adaptation state relates to the bleaching in the retinal cells

[Ritschel and Eisemann - Eurographics2012]



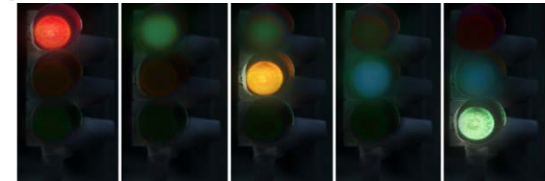
## Overcoming Physical Limitations

- Apparent Resolution Enhancement  
[Didyk, Eisemann, Ritschel, Myszkowski, Seidel – SIGGRAPH 2010]  
[Templin, Didyk, Ritschel, Eisemann, Myszkowski, Seidel - SCCG 2011]

Resolution

- A Computational Model of Afterimages  
[Ritschel & Eisemann - Eurographics'12]

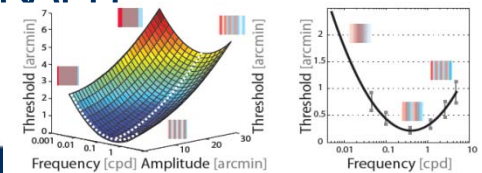
Brightness



- A Perceptual Model for Disparity

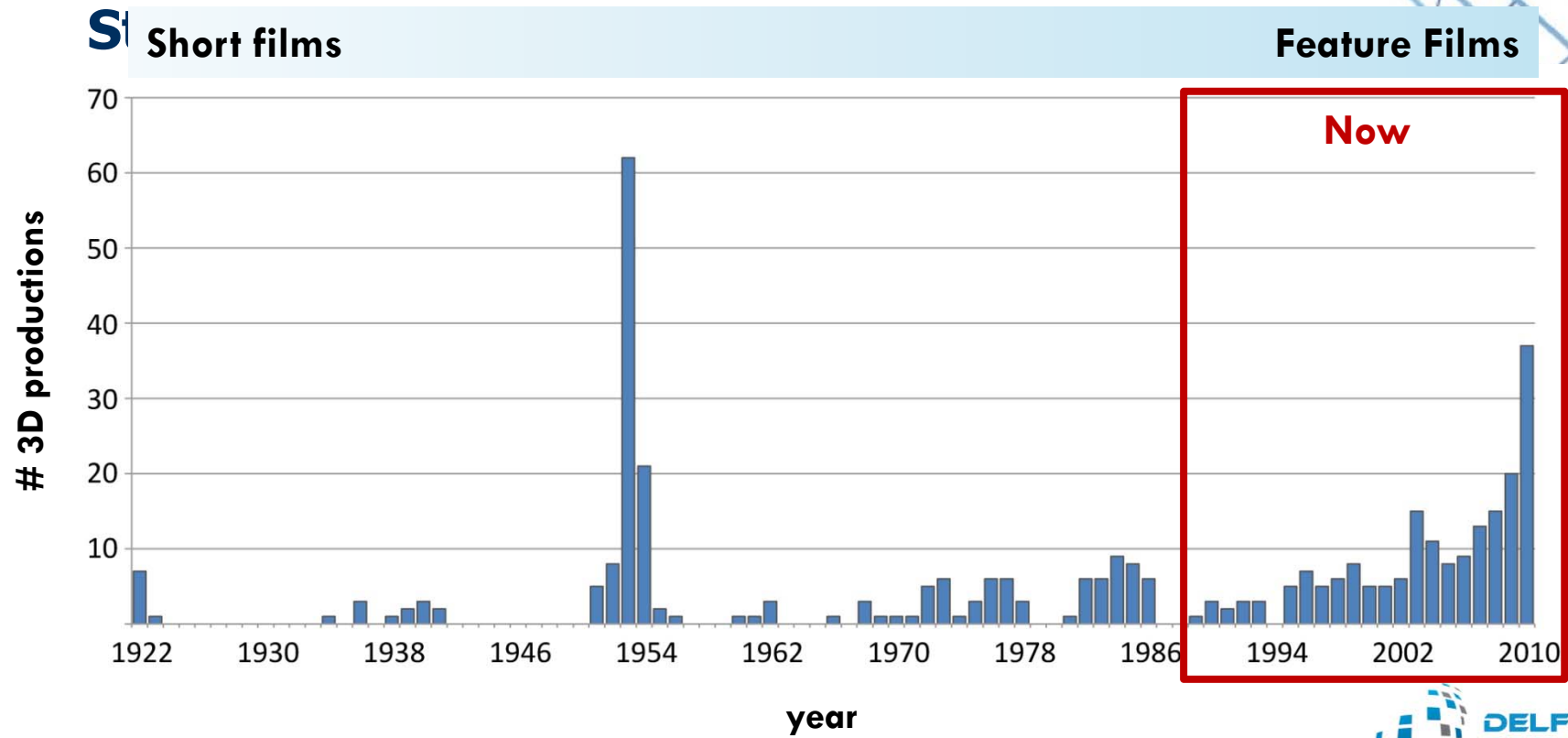
[Didyk, Ritschel, Eisemann, Myszkowski, Seidel - SIGGRAPH 2011/SIGAsia2012]

Stereo illusion

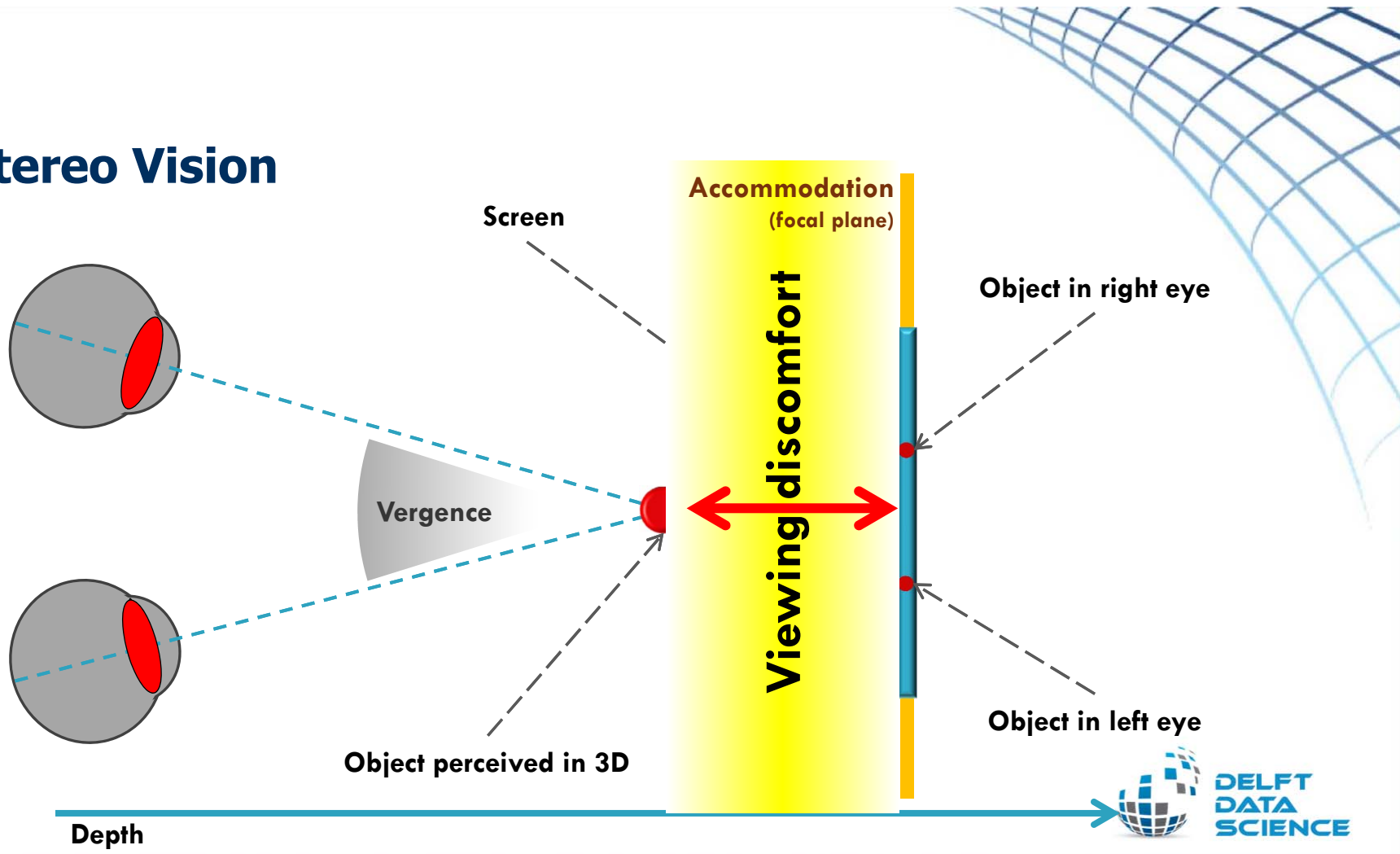


## Rebirth of Stereo

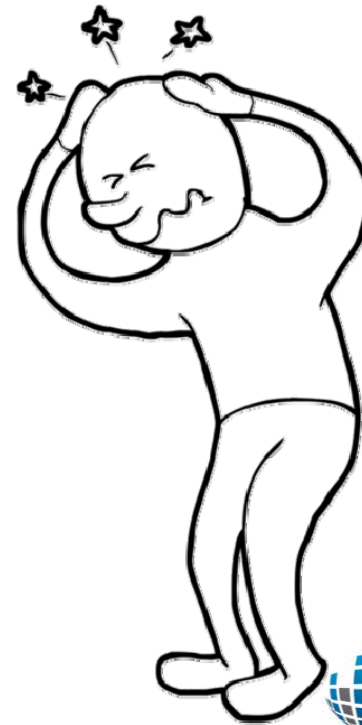




# Stereo Vision

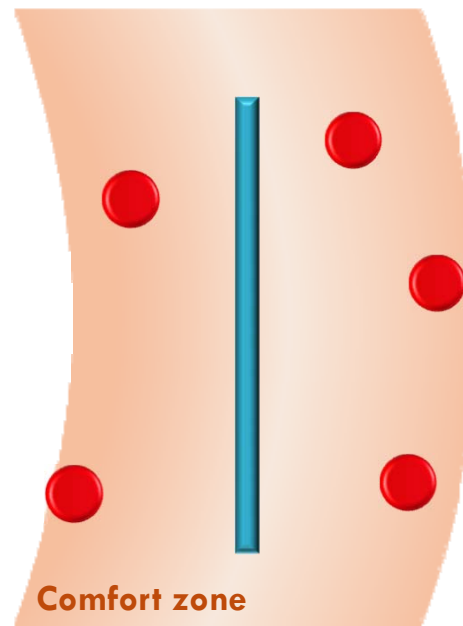
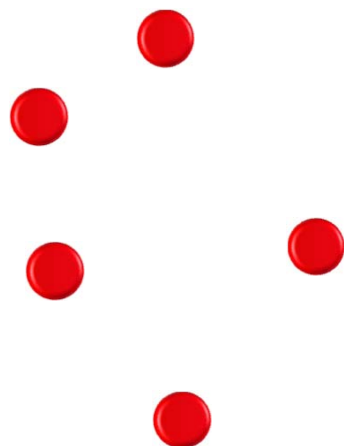
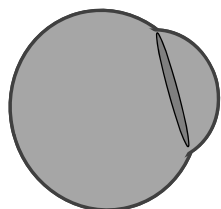
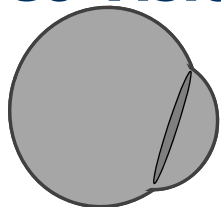


## Stereo Vision





## Stereo Vision



Scene manipulation  
~~Viewing discomfort~~ → Viewing comfort



[Didyk, Ritschel, Eisemann, Myszkowski, Seidel – SIGGRAPH 2011]  
[Didyk, Ritschel, Eisemann, Myszkowski, Seidel – SIGGRAPH Asia 2012]

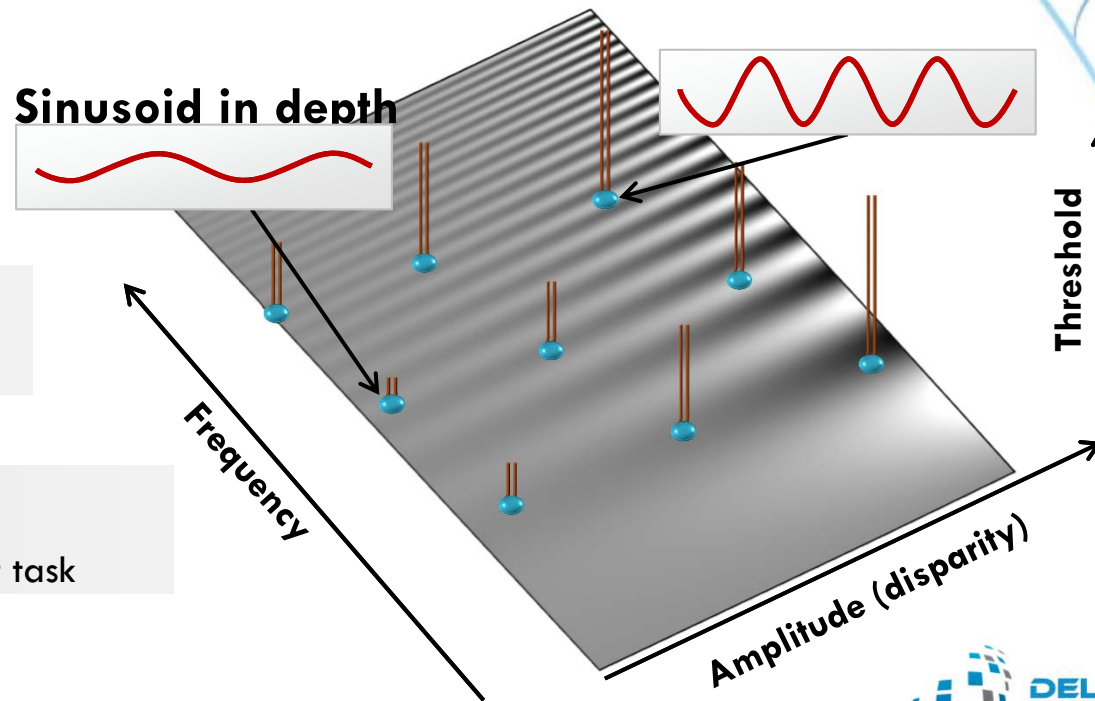
# Perception Model

Parameter space:

Sample the space

Measure thresholds

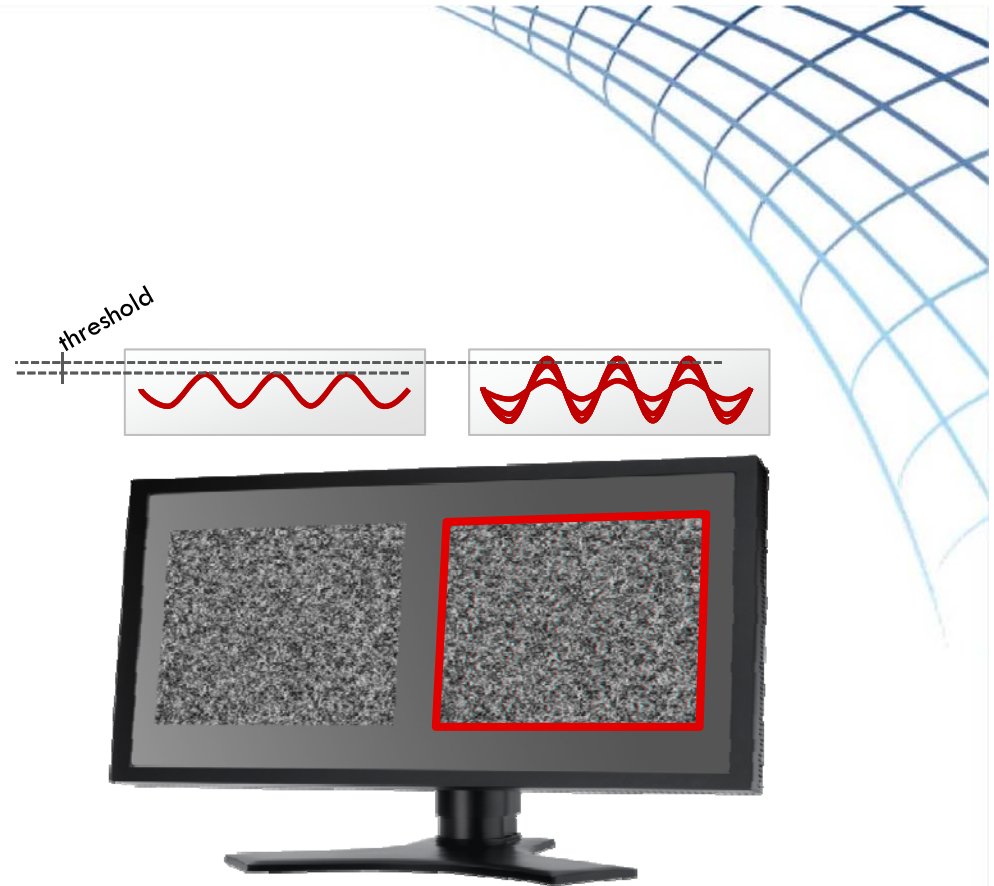
- Experiment with adjustment task



# Measurements

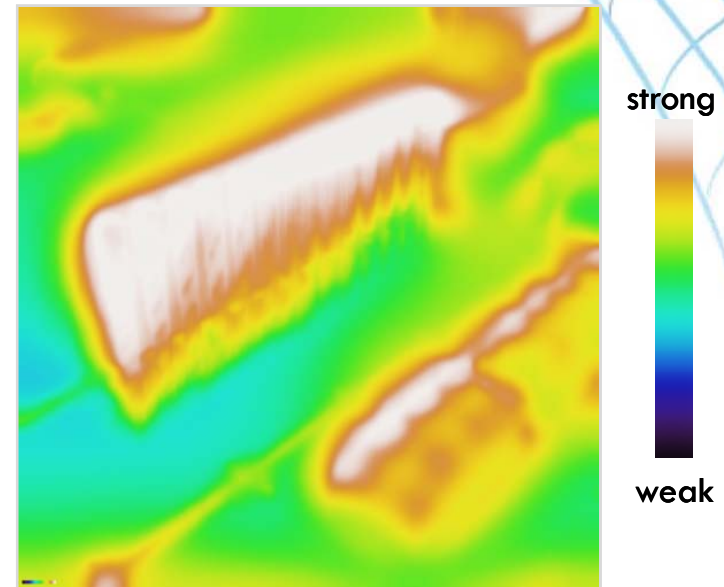
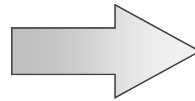
## Thresholds measurement:

- Two sinusoidal corrugations
- Which one has more depth? (left/right)
- Amplitude adjustment (PEST with 2AFC)



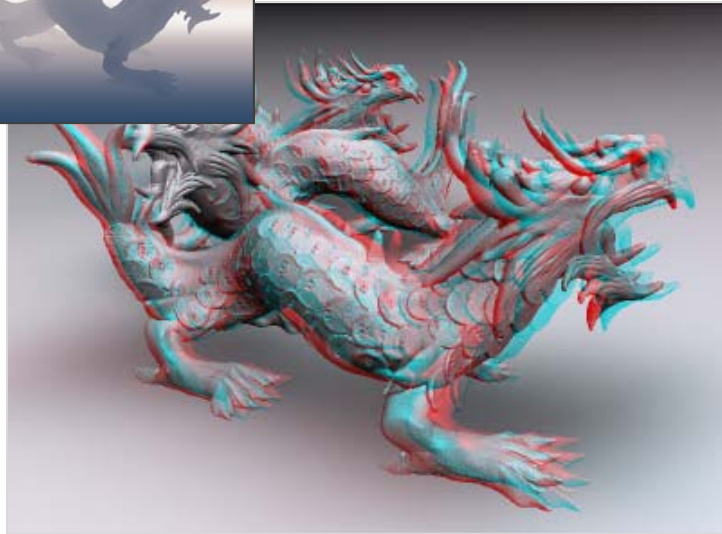
[Didyk, Ritschel, Eisemann, Myszkowski, Seidel – SIGGRAPH 2011]  
[Didyk, Ritschel, Eisemann, Myszkowski, Seidel – SIGGRAPH Asia 2012]

## Stereo Vision – Metric



[Didyk, Ritschel, Eisemann, Myszkowski, Seidel – SIGGRAPH 2011]  
[Didyk, Ritschel, Eisemann, Myszkowski, Seidel – SIGGRAPH Asia 2012]

## Stereo Vision – Metric



Standard stereo



Backward-compatible stereo

# Perceptual Rendering

Taking perception into account

- can reduce computational cost
- can increase quality/comfort
- is advantageous even on modern displays

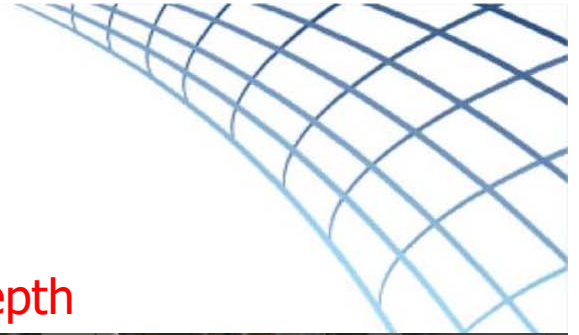


[Pajak, Herzog, Eisemann, Myszkowski, Seidel - EG 2014]

## Streaming of Rendered Content with Depth Compression

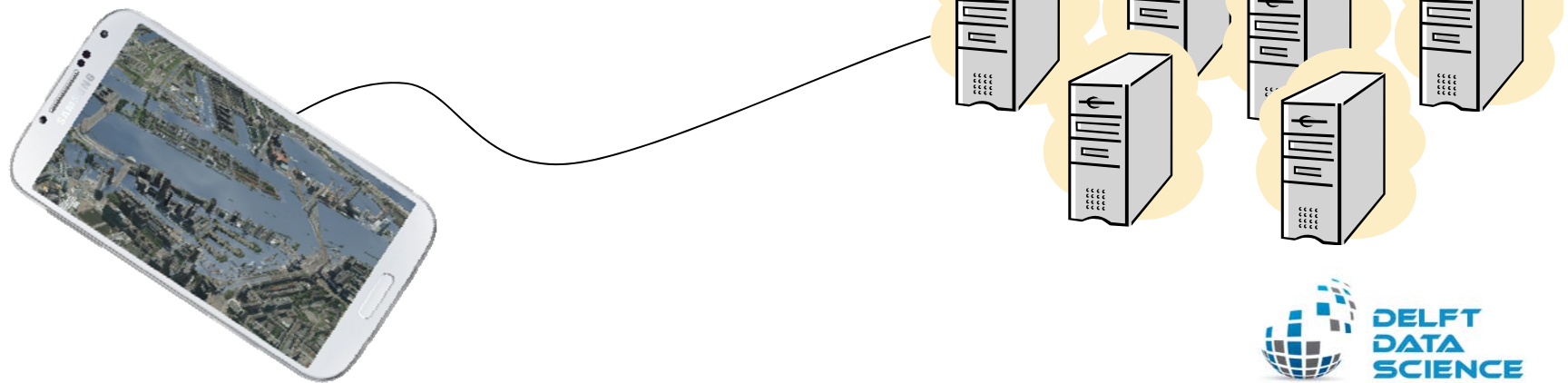
H264

Our solution + depth



[Pajak, Herzog, Eisemann, Myszkowski, Seidel - EG 2014]

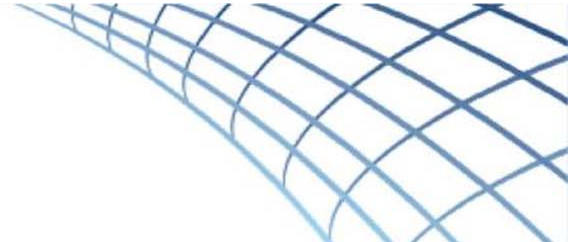
## Remote Computing



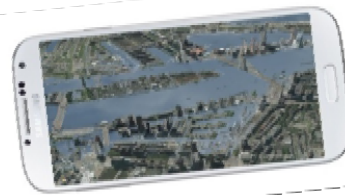


Enlighten your Research  
SurfSara

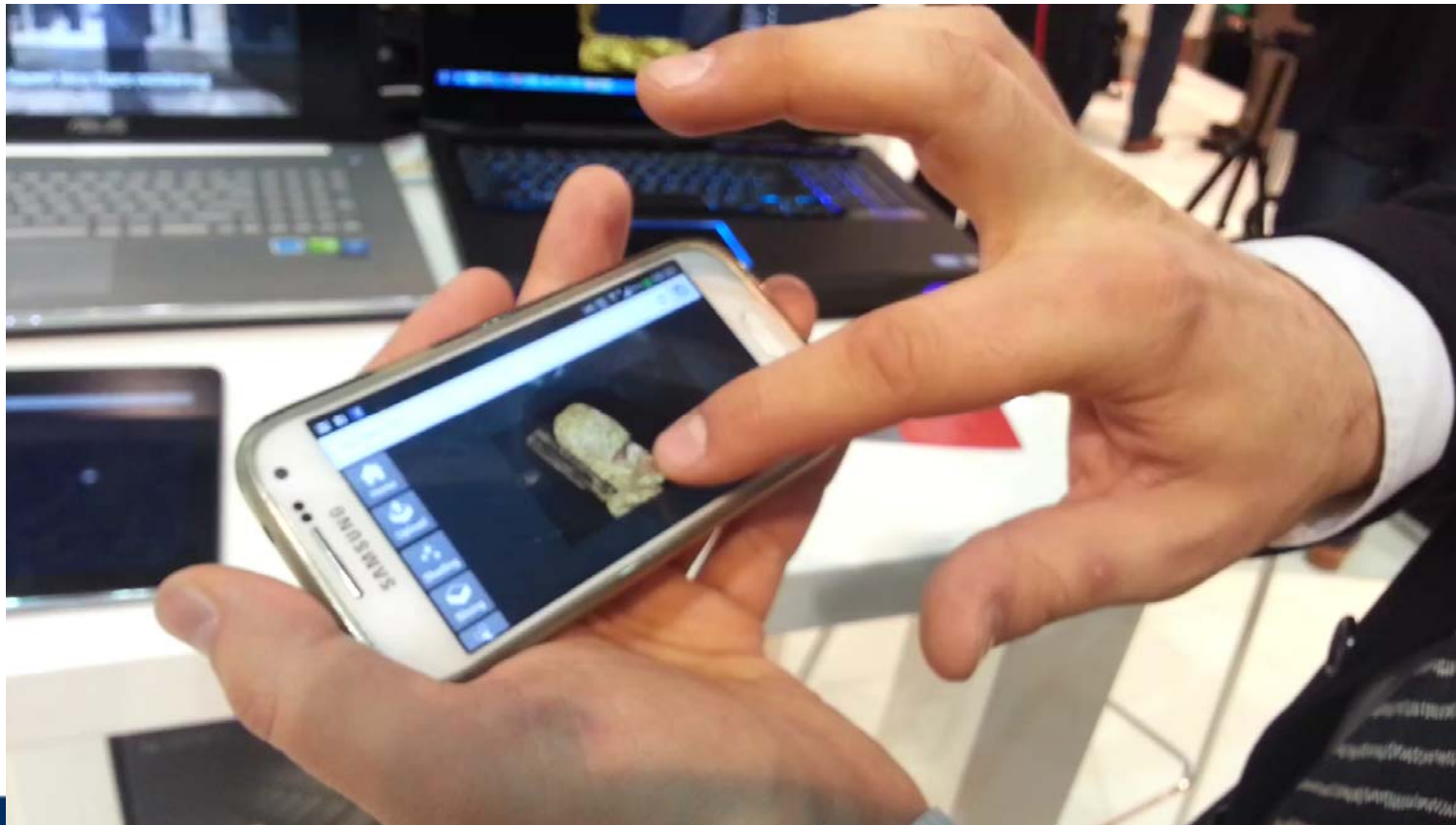
## Remote Computing



General Image  
Synthesis Solution

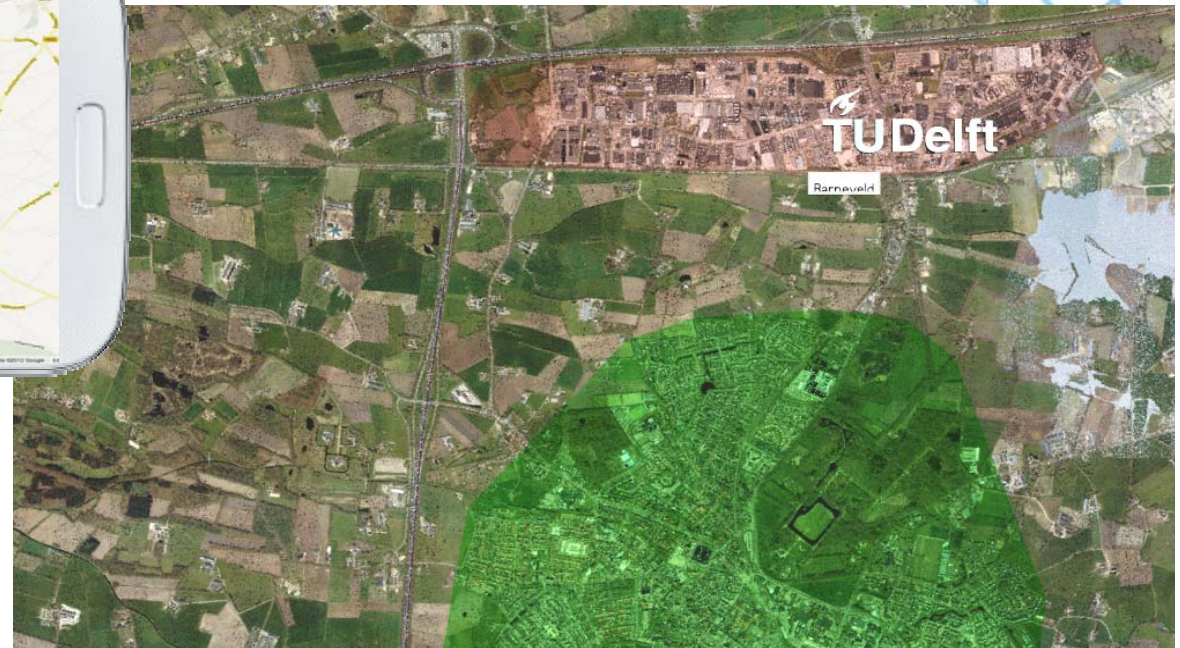
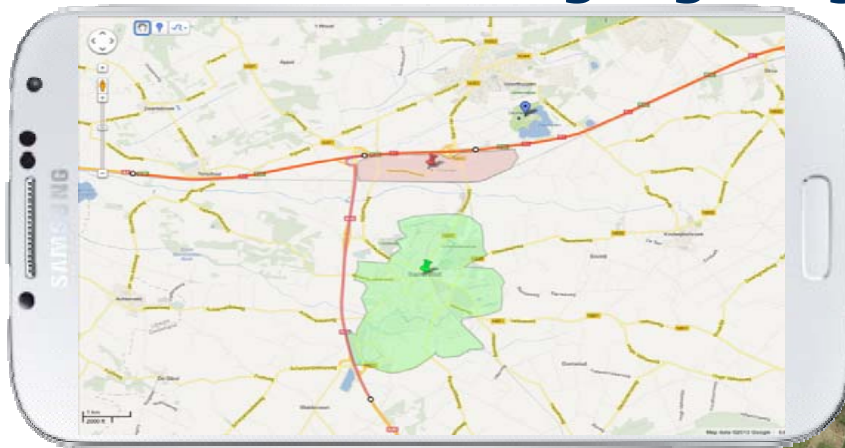


## Remote Computing

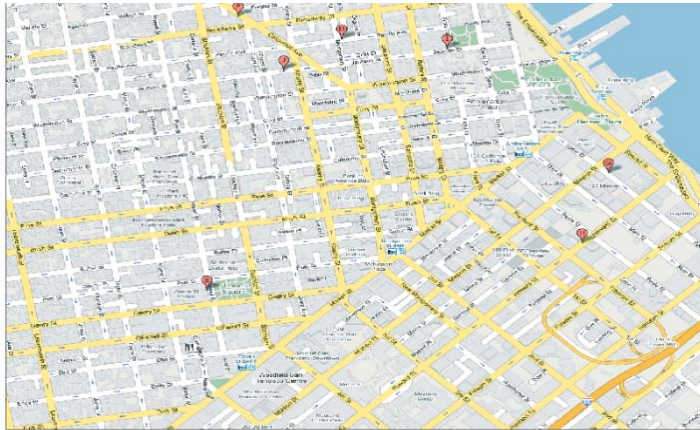


[Tutenel et al. GeoWorldForum 2013]

## Interaction: Highlighting and Markup



## Example: Improved Navigation



- Simplified representation for recognition
- Visual Context for orientation

Grabler et al. 2008

## Example: Improved Navigation – Existing solutions



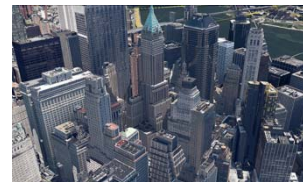
Top-down



Street-level



Bird's eye



3D



Combined

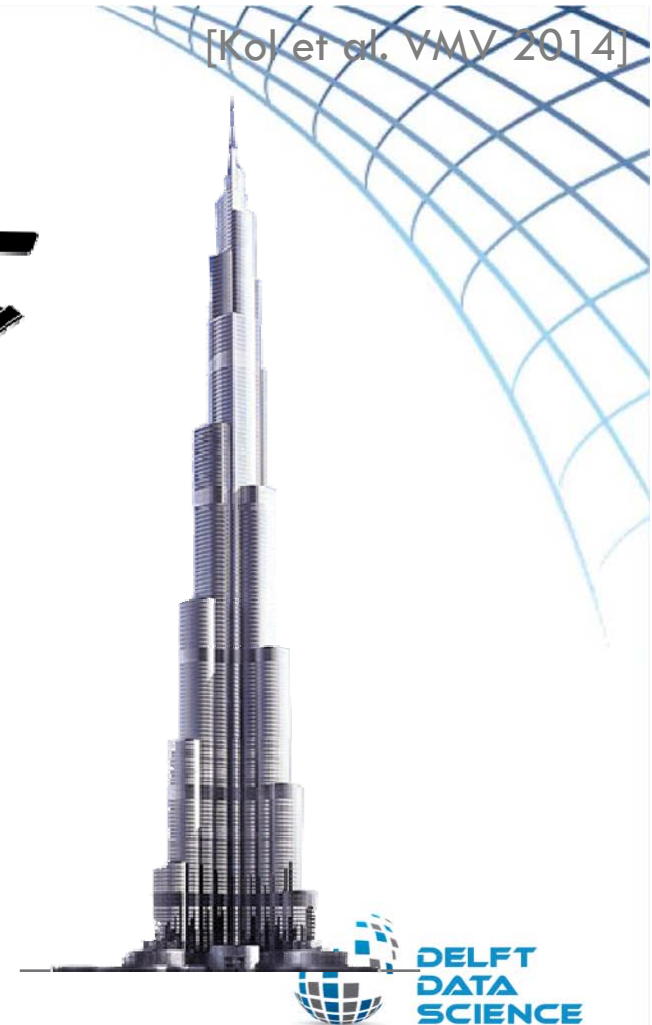
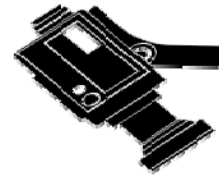


**DELFT  
DATA  
SCIENCE**

[Kol et al. VMM 2014]

## Example: Improved Navigation

- Give a Context
- Optimize for building recognition
  - Canonical View
  - Real-time constraints





Regular



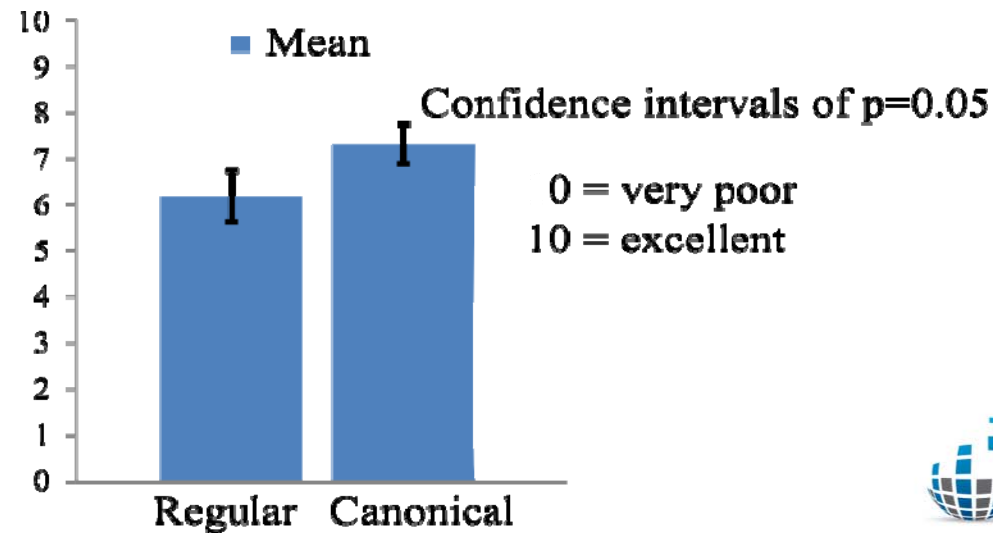
Canonical



## Example: Improved Navigation

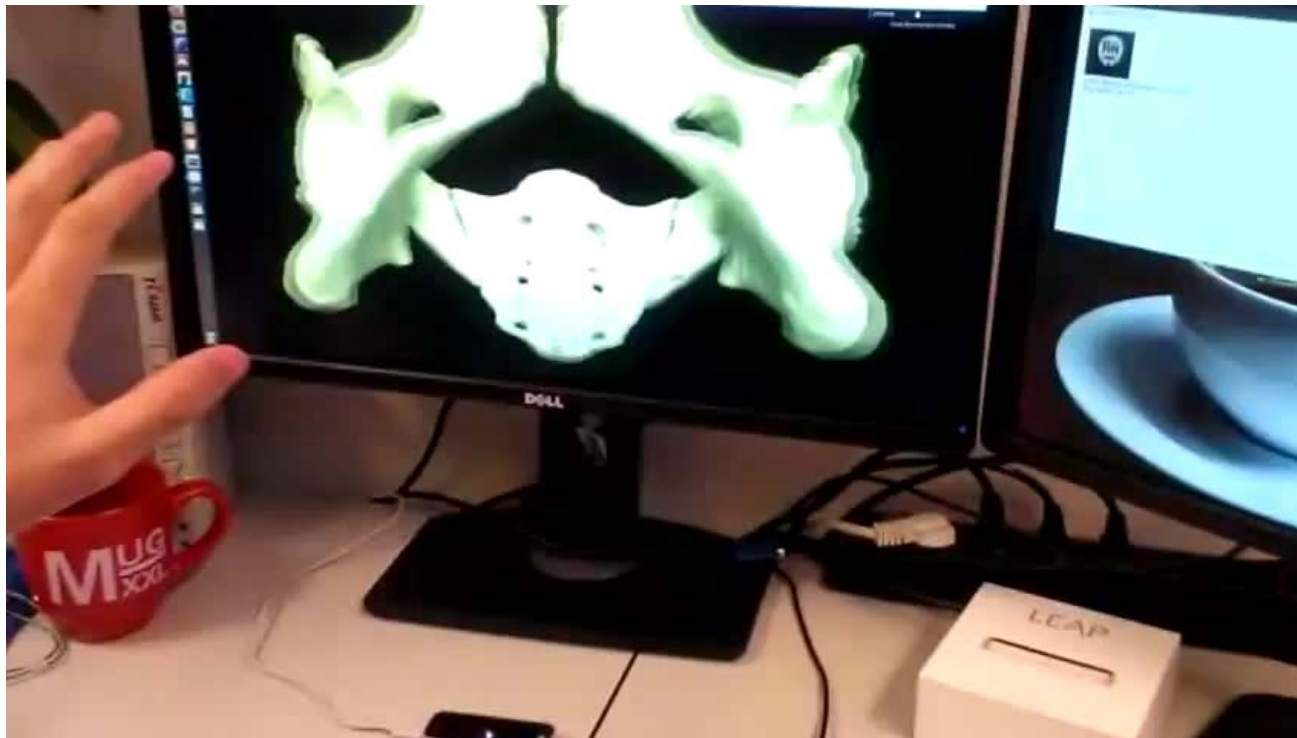
- Number of wrong turns in navigation tasks:

Canonical View	Street-level View	Top-down View
2/12	3/12	6/12





## Novel Interaction Possibilities

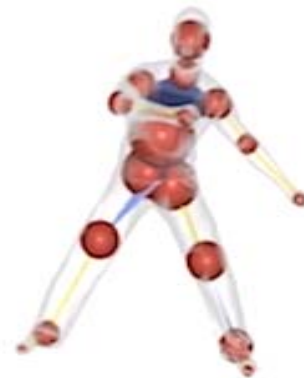


[Thiery, Guy, Boubekur, Eisemann – TOG2016]

## Encode Motion Efficiently - Animated Sphere Meshes



input mesh



sphere-mesh

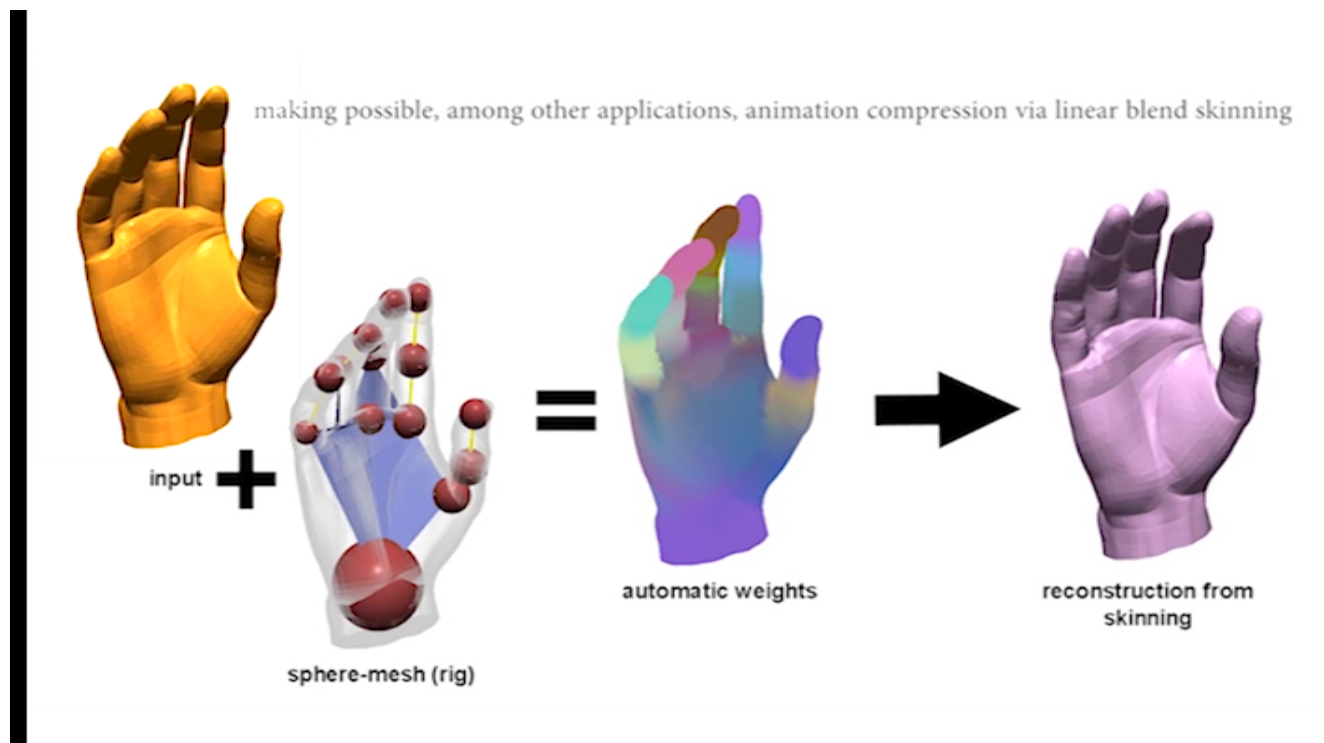


interpolated  
sphere-mesh



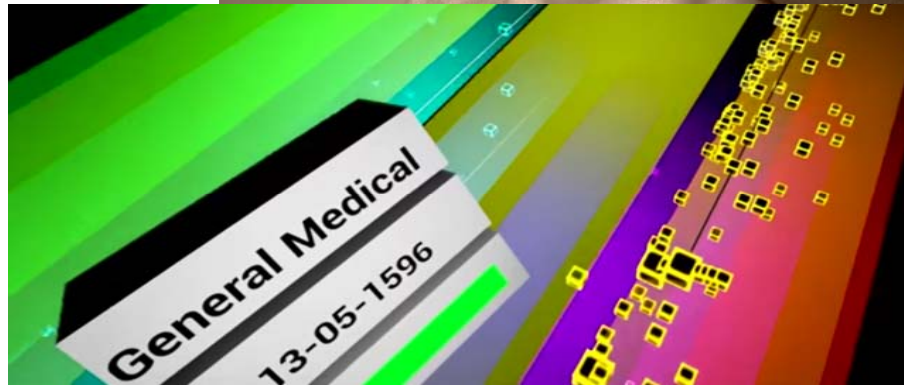
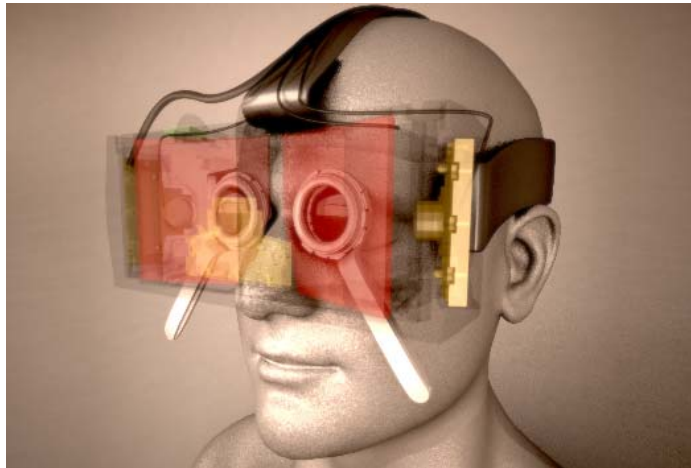
[Thiery, Guy, Boubekur, Eisemann – TOG2016]

## Encode Motion Efficiently - Animated Sphere Meshes



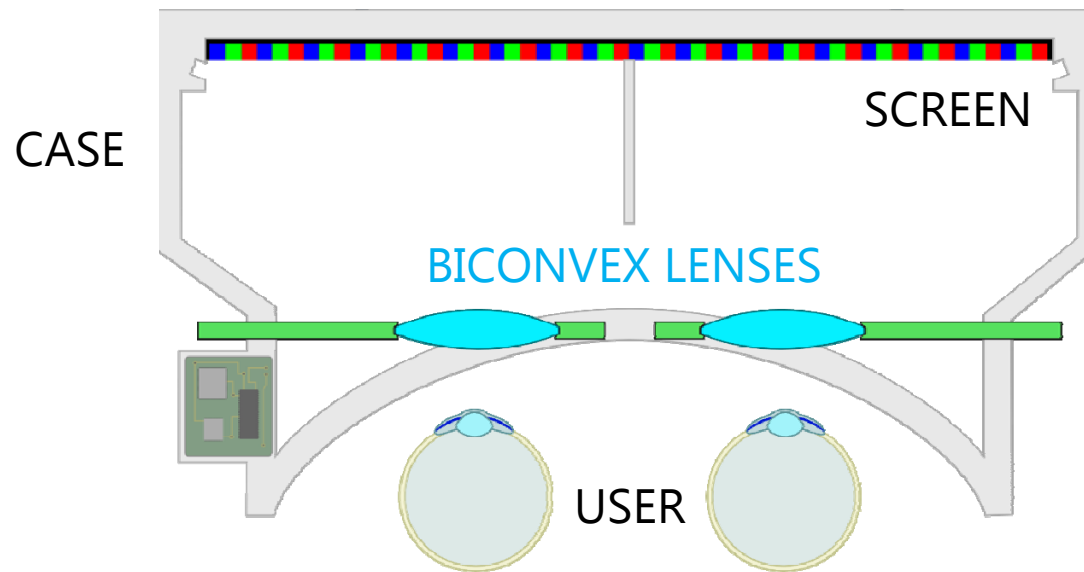
[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

## Novel Display Devices



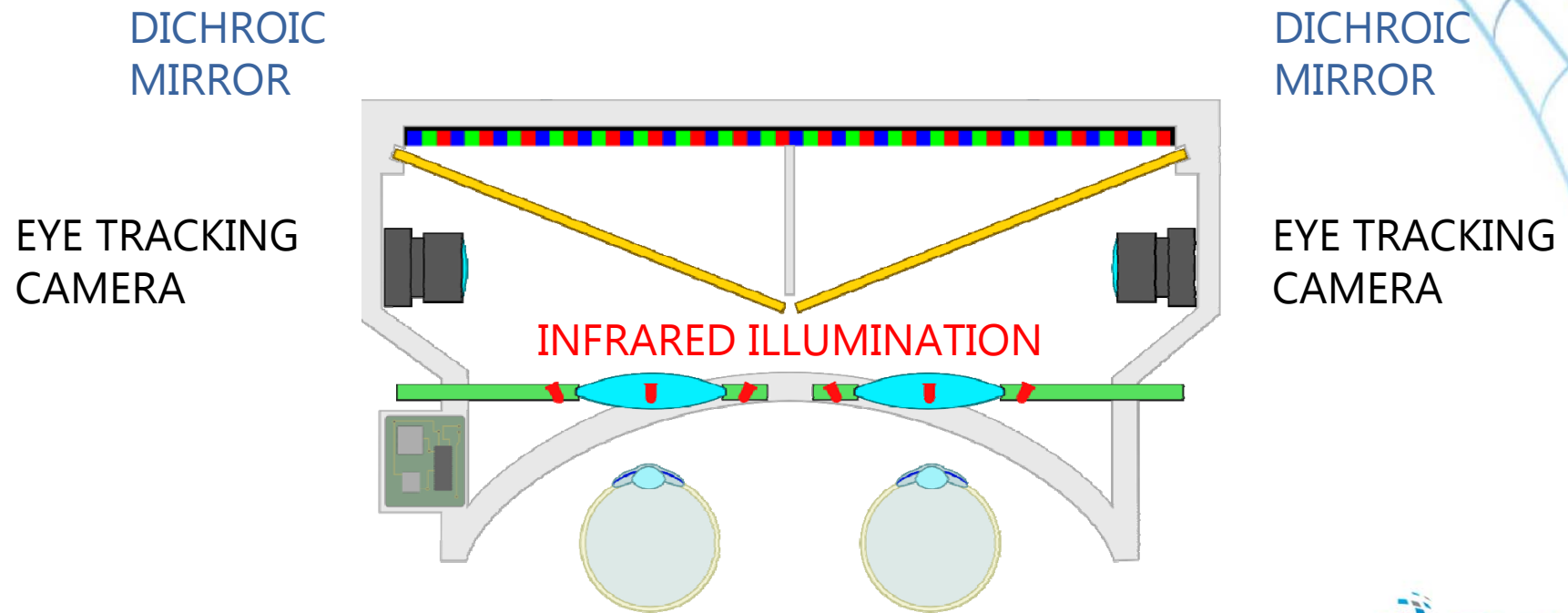
[Stengel, Grogorick, Eisemann2, Magnor – ACM MM 2015]

## Novel Display Devices



[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

## Novel Display Devices



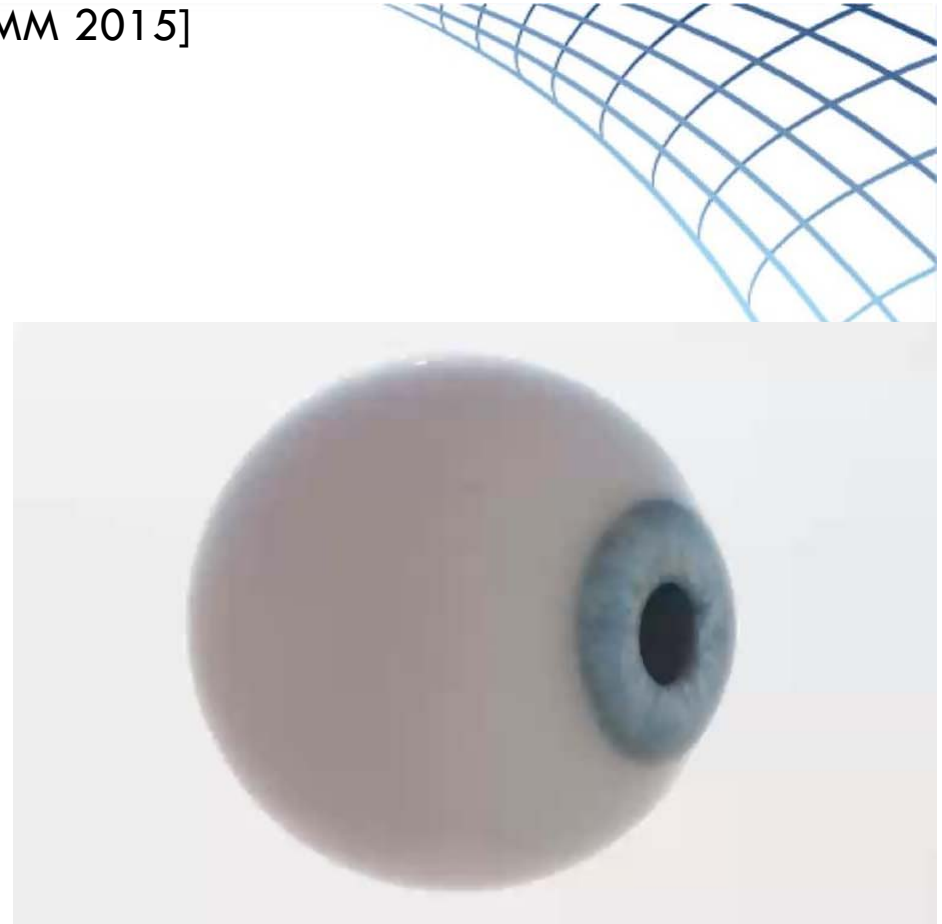
[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

## CALIBRATION / USER

- Calibration via Inverse Rendering

A photon accurate model of the human eye [Deering'05]

The Physiology of the Eye [Adler et al., '08]

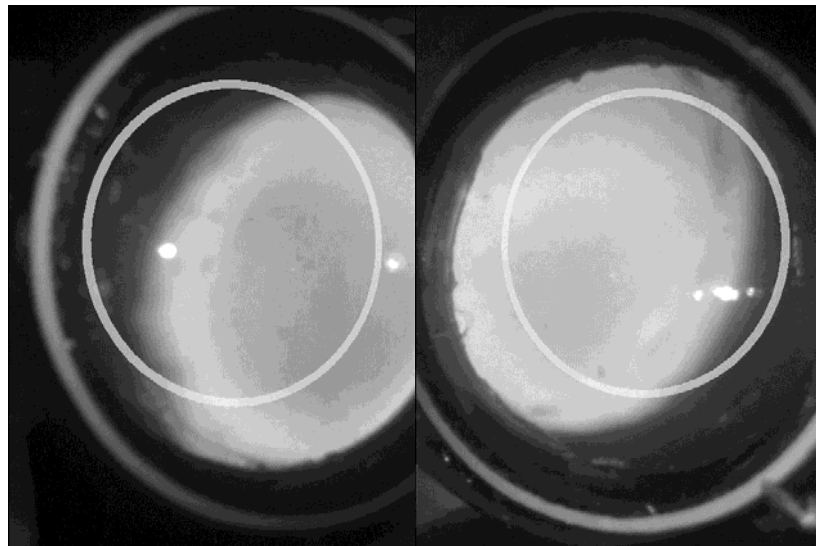


PHYSICAL EYE MODEL  
DELFT  
SCIENCE

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[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

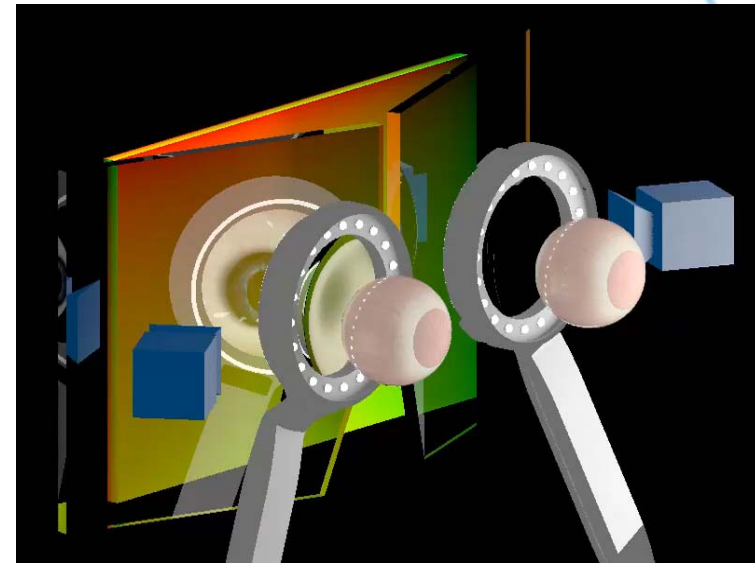
## CALIBRATION / LENS LOCATION



LEFT EYE

RIGHT EYE

CAMERA CAPTURE



SIMULATED MODEL

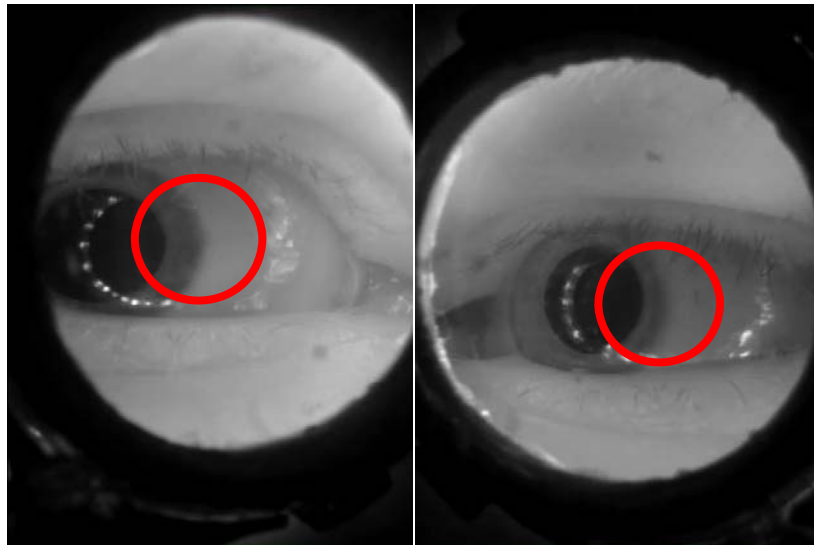


Koninklijk Instituut Van Ingenieurs



[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

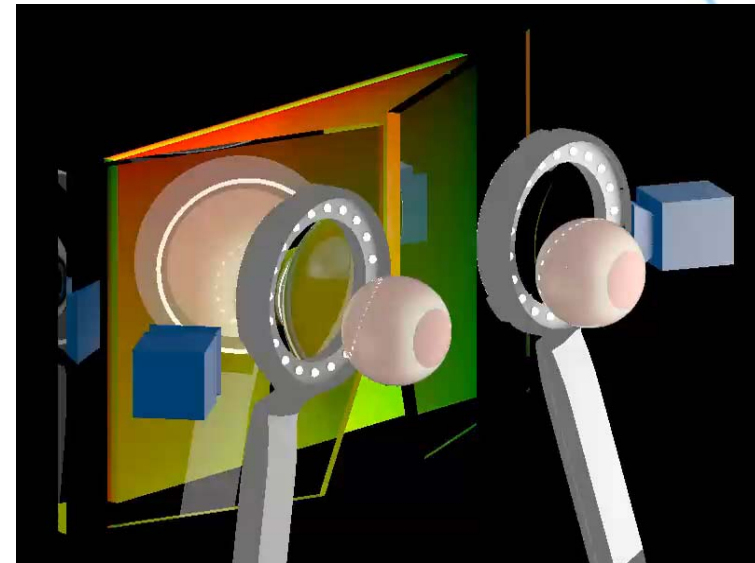
## CALIBRATION / EYE BALL LOCATION



LEFT EYE

RIGHT EYE

CAMERA CAPTURE

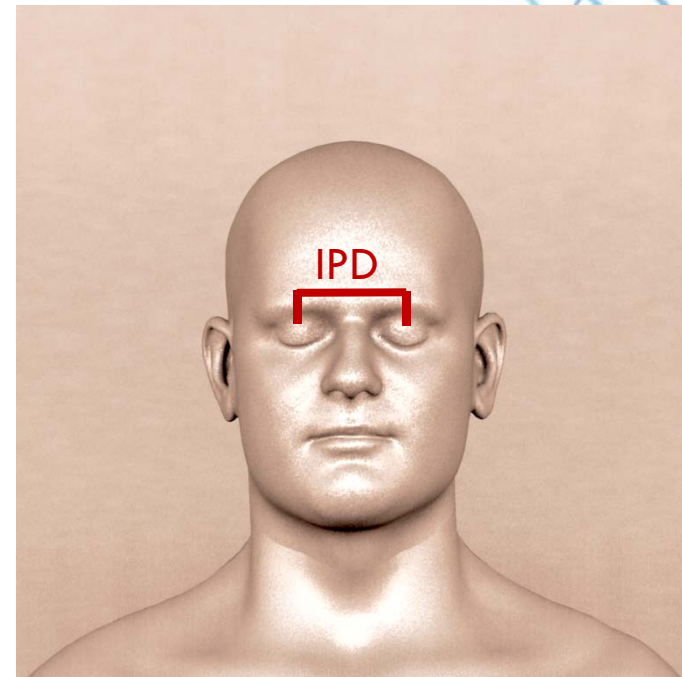
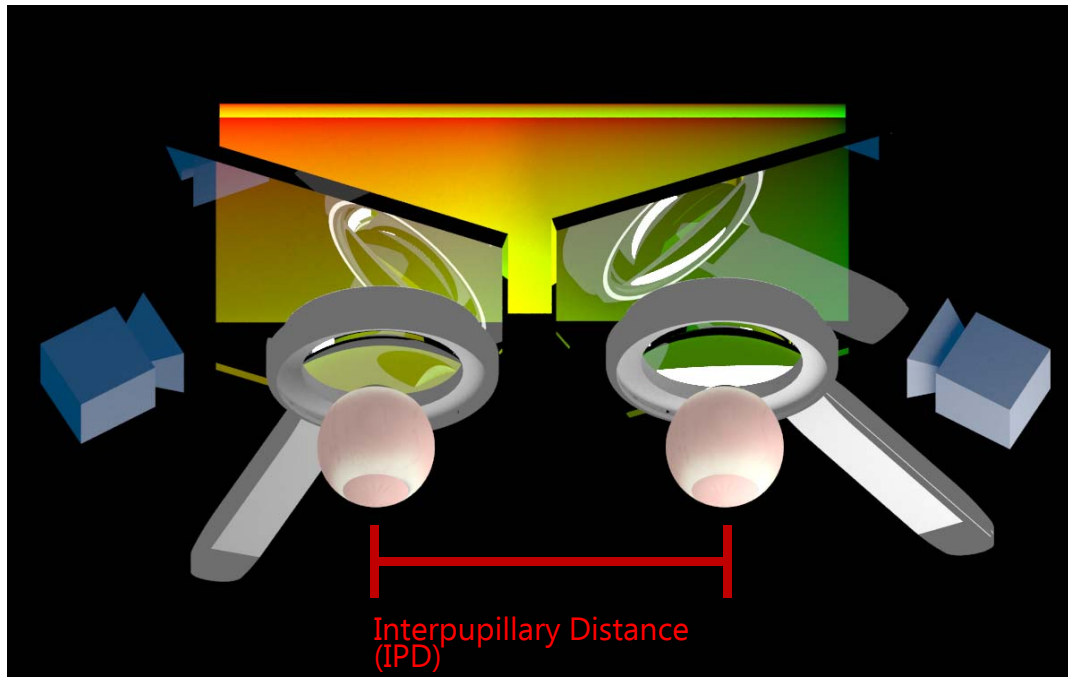


SIMULATED MODEL



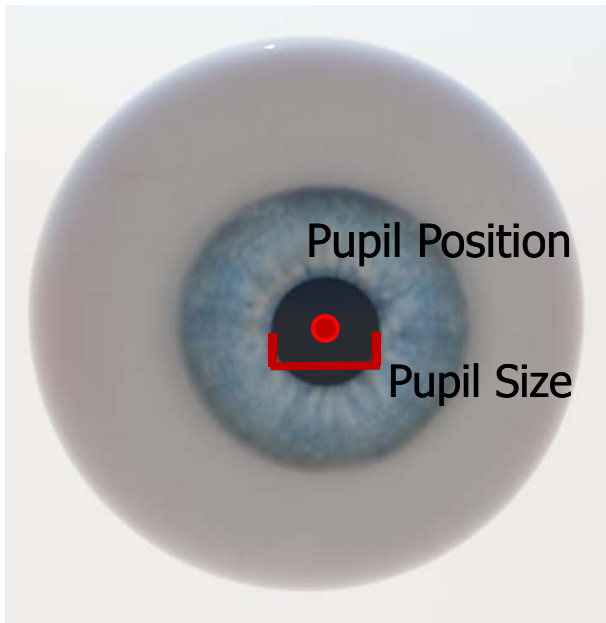
[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

## CALIBRATION / USER

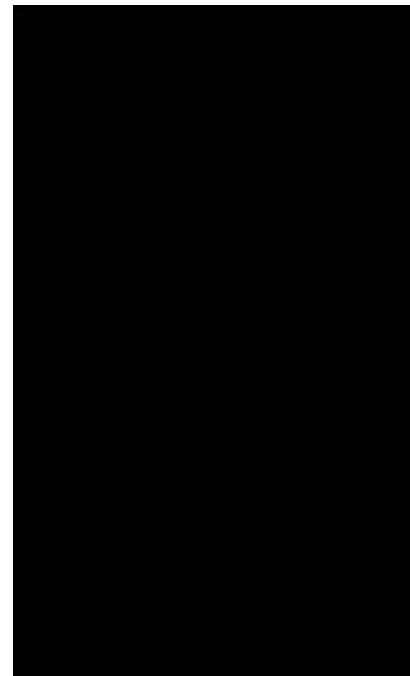


[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

## PUPIL TRACKING



PHYSICAL EYE MODEL



SCREEN CAPTURE



[Stengel, Grogorick, Eisemannx2, Magnor – ACM MM 2015]

## TRACKING PERFORMANCE / DESKTOP

- two cores on i7@3.5Ghz

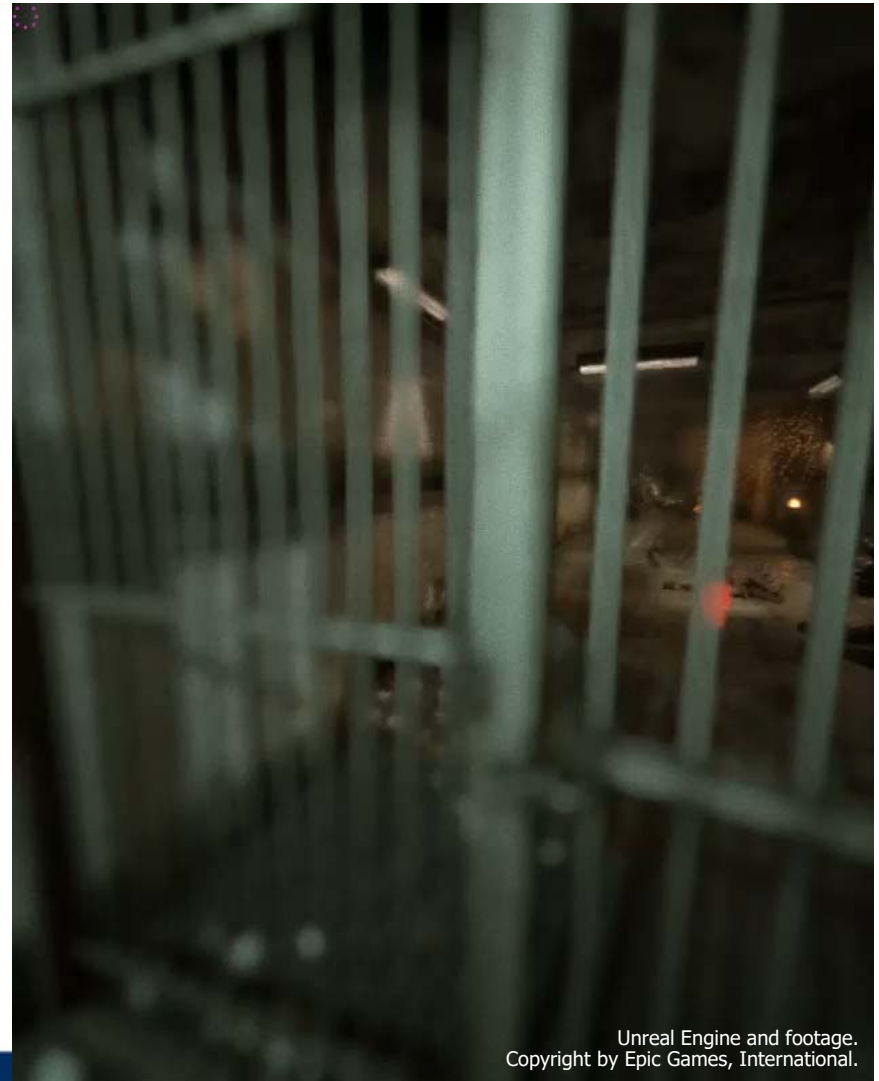
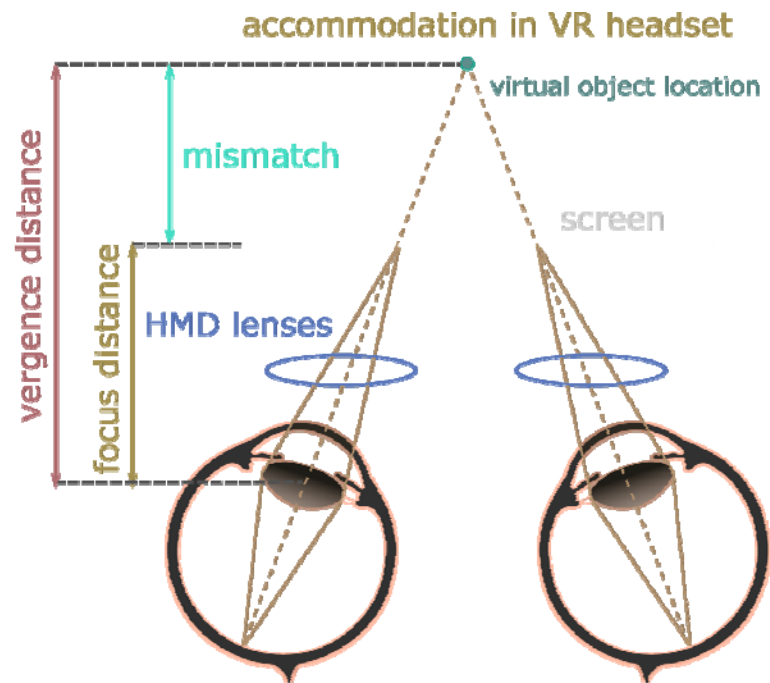
Processing step	Timings
Camera frame capture	11 ms
<del>Occlusion metric</del>	<del>2 ms</del>
<del>Pupil Detection (occluded)</del>	<del>2 ms</del>
Pupil Detection (visible)	0.9 ms
Gaze computation	< 0.1 ms
	<del>~ 16.0 ms</del>
	~ 12.0 ms (total)

may be skipped for many users

~ 5 ms

~ 1 ms

# Accommodation Simulation



# Visualization and Perception

- Realistic Rendering
- Perceptual Methods
- Visualization & Interface



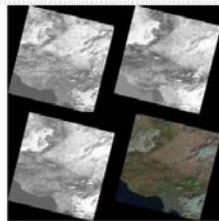
# Effective Data Visualization Requires



- **Large-Scale Rendering**

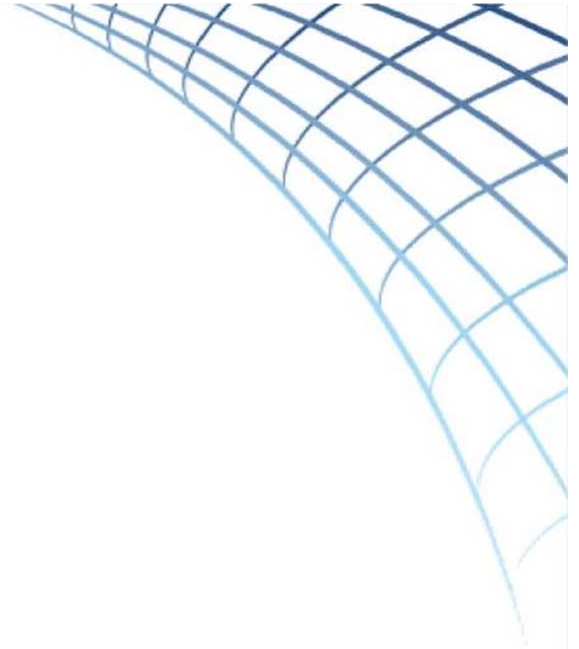


- **Visualization and Perception**



- **Data Analysis**

**Questions?**





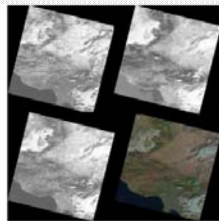
# Effective Data Visualization Requires



- **Large-Scale Rendering**



- **Visualization and Perception**



- **Data Analysis**

## Data Analysis

- High-dimensional/Heterogeneous Data
- Dimensionality Reduction
- Visual Analytics



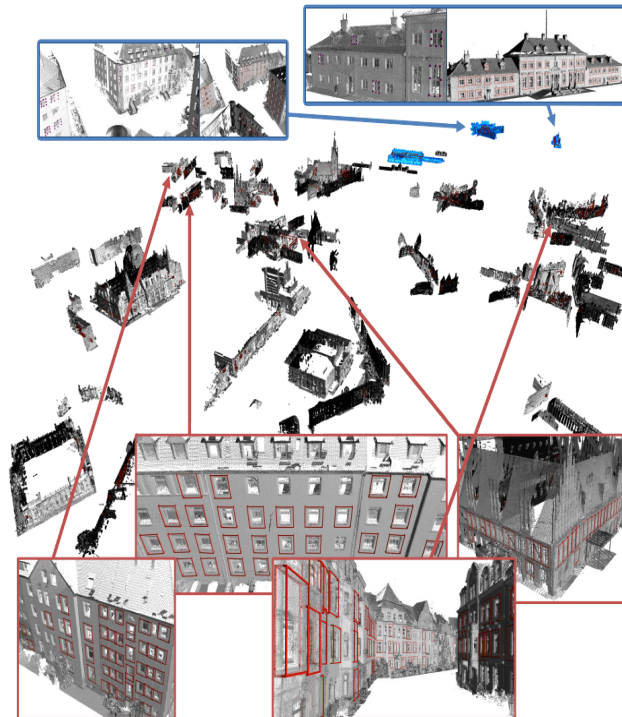
# Data Analysis



[SunkeI, Jansen, Wand, Eisemann, Seidel EG 2012]

## Supported Recognition

- here 128 M points, find all windows: 2 min





[Silva, Eisemann, Bidarra, Coelho - PCG 2015]

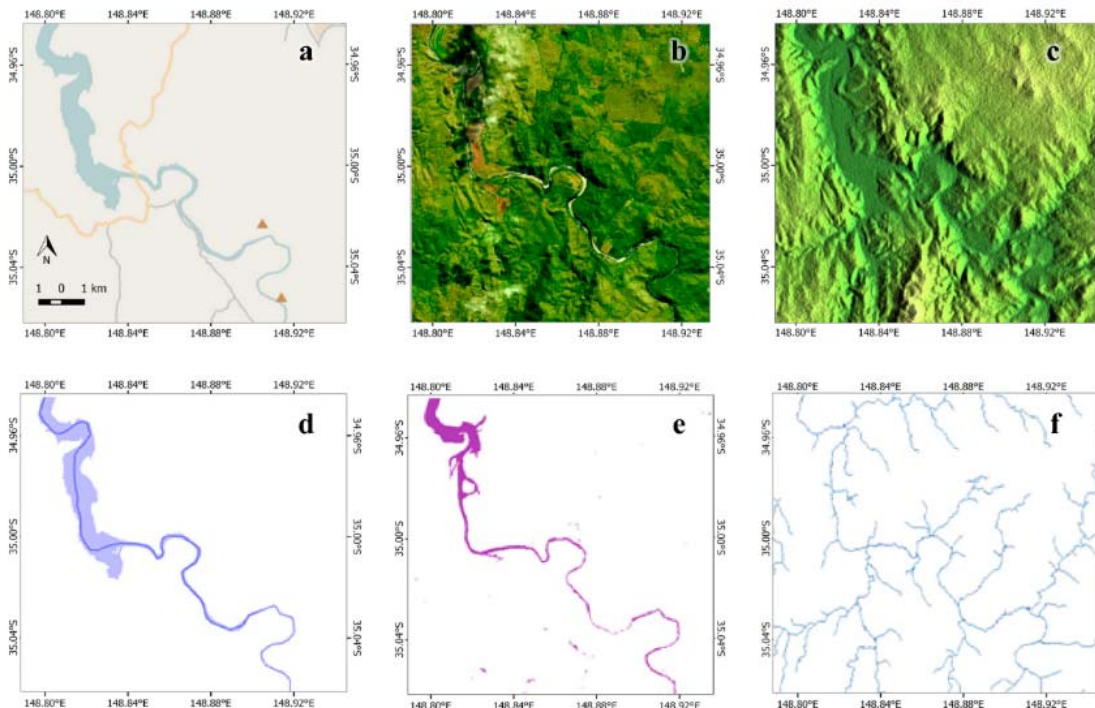
## Model Construction: Blueprints + Rules + ...





## Model Construction

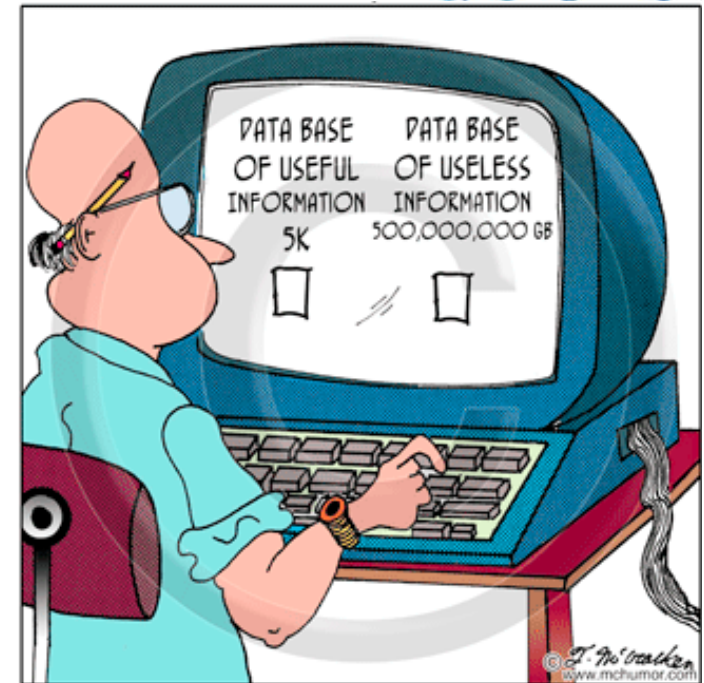
- Integrating Data Sets for River Validation





## Data growth = increase in information?

- What if you do not yet know what "useful" is?

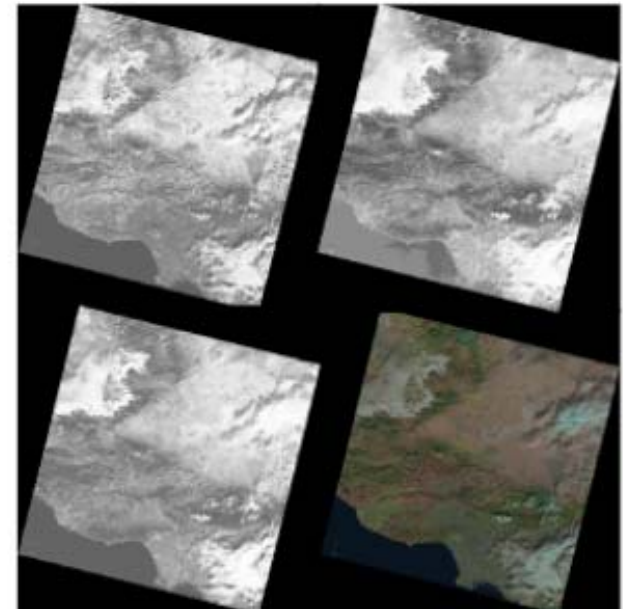


## General Approach to Visual Analytics?

Visual Analytics:

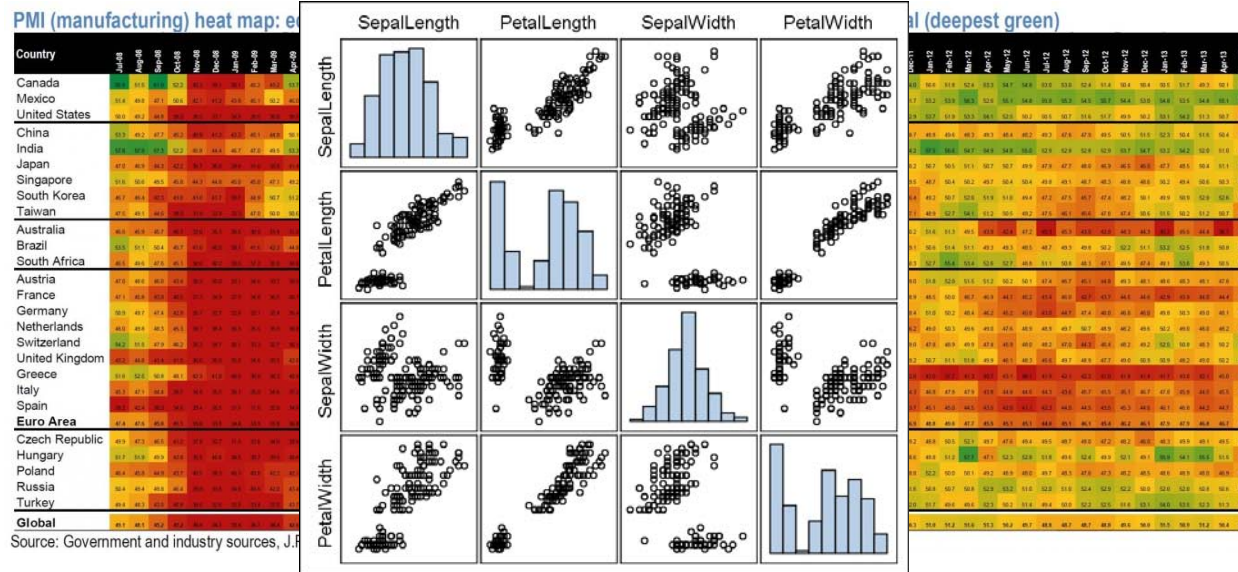
Interactive hypothesis finding via Data

- Many challenges, but we will focus on:
- **Dimensionality**

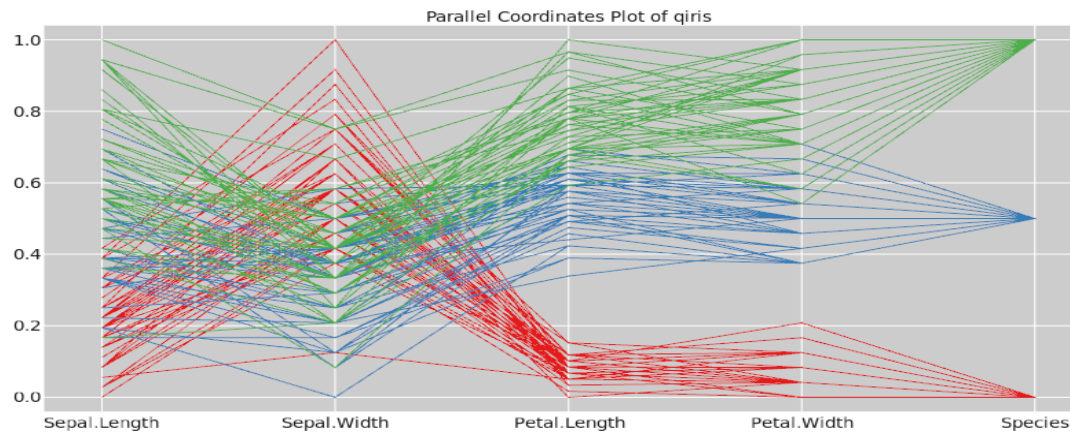


# High-Dimensional Data

- Standard Solutions:

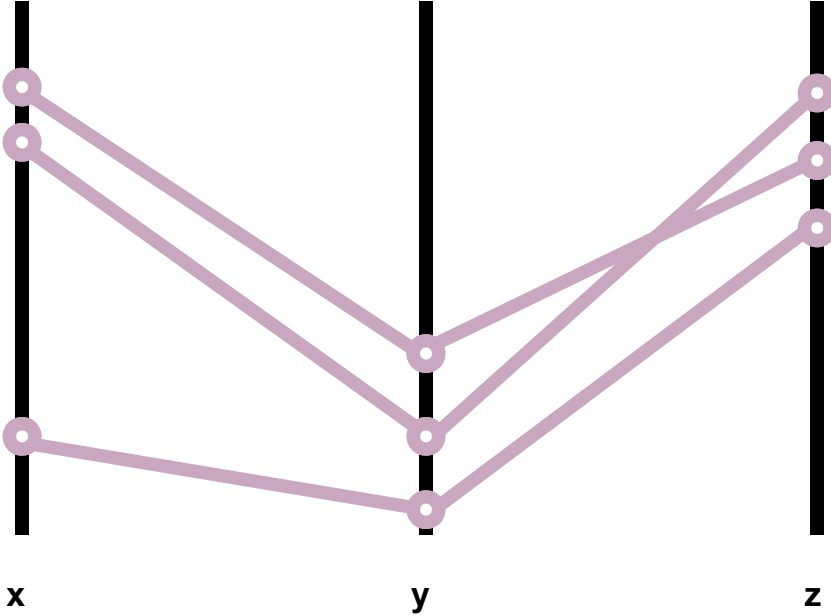


# Parallel Coordinate Plots

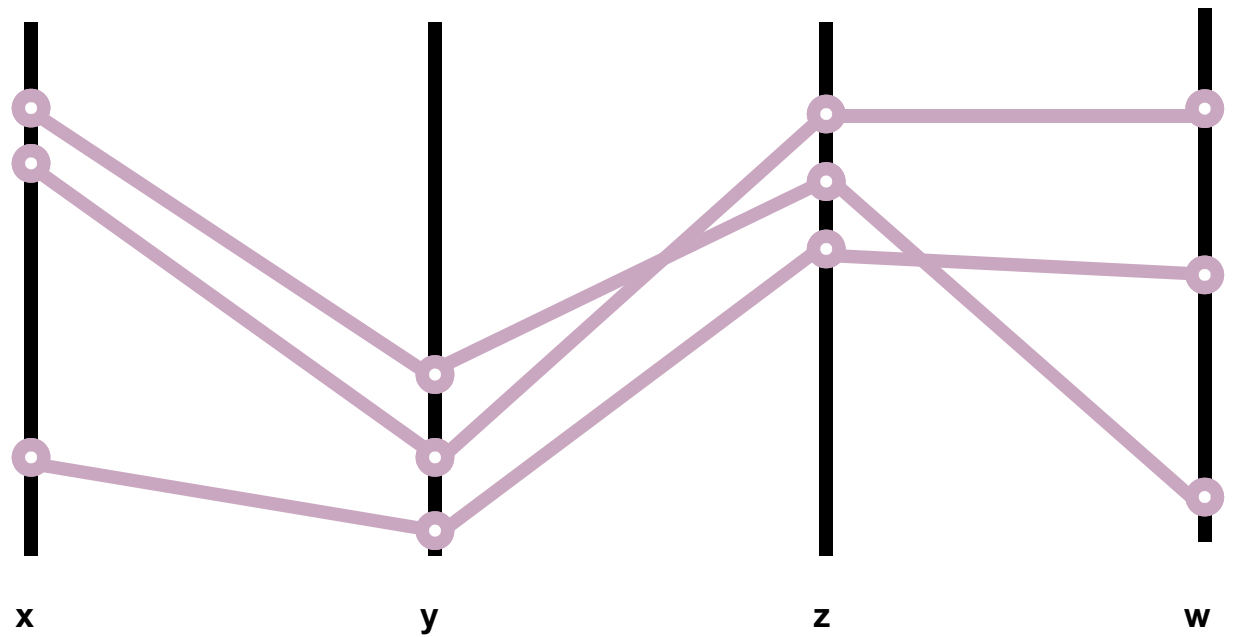


- More dimensions in one view
- Easier detection of patterns/outliers in data

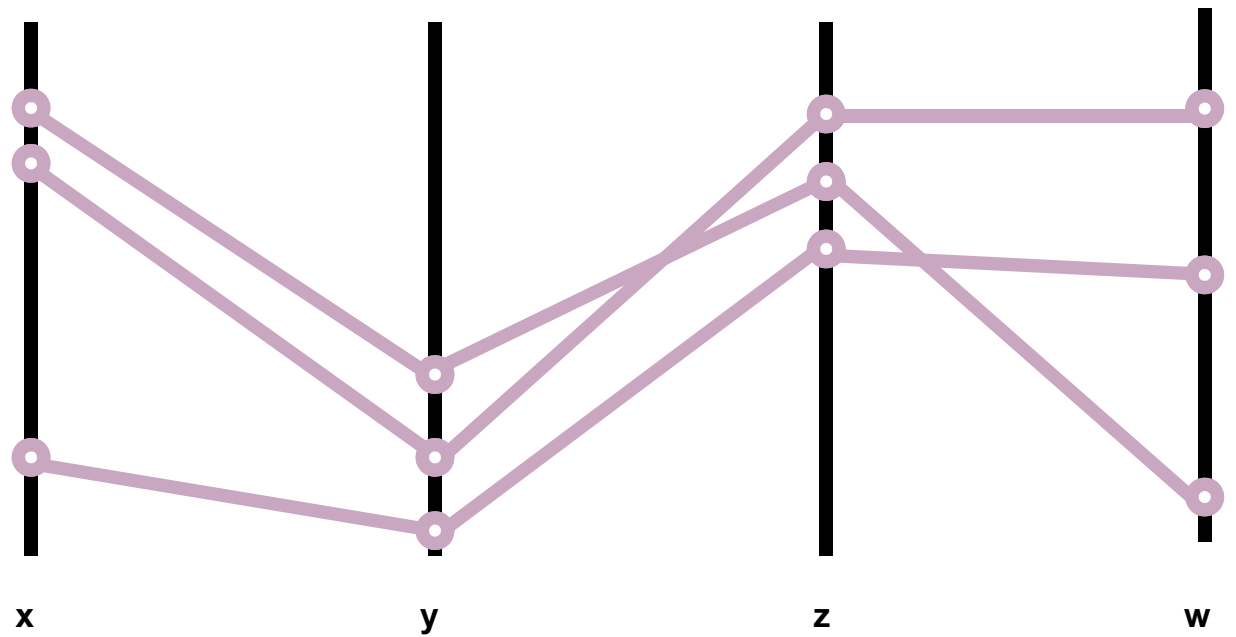
# Parallel Coordinates



# Parallel Coordinates

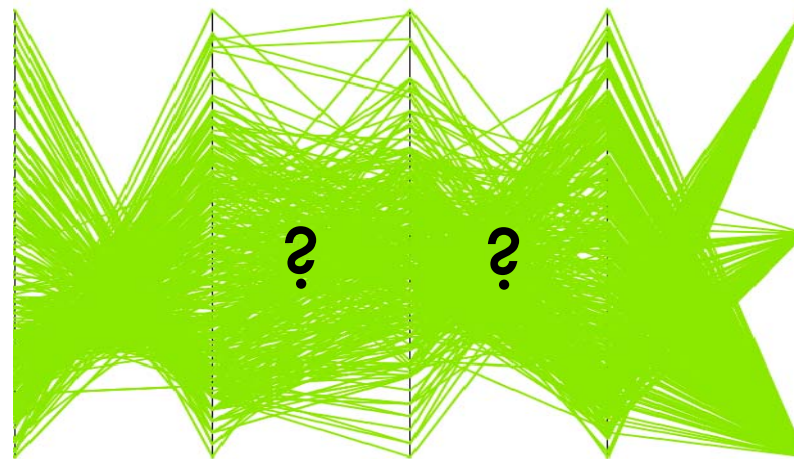


# Parallel Coordinates



## The Problem

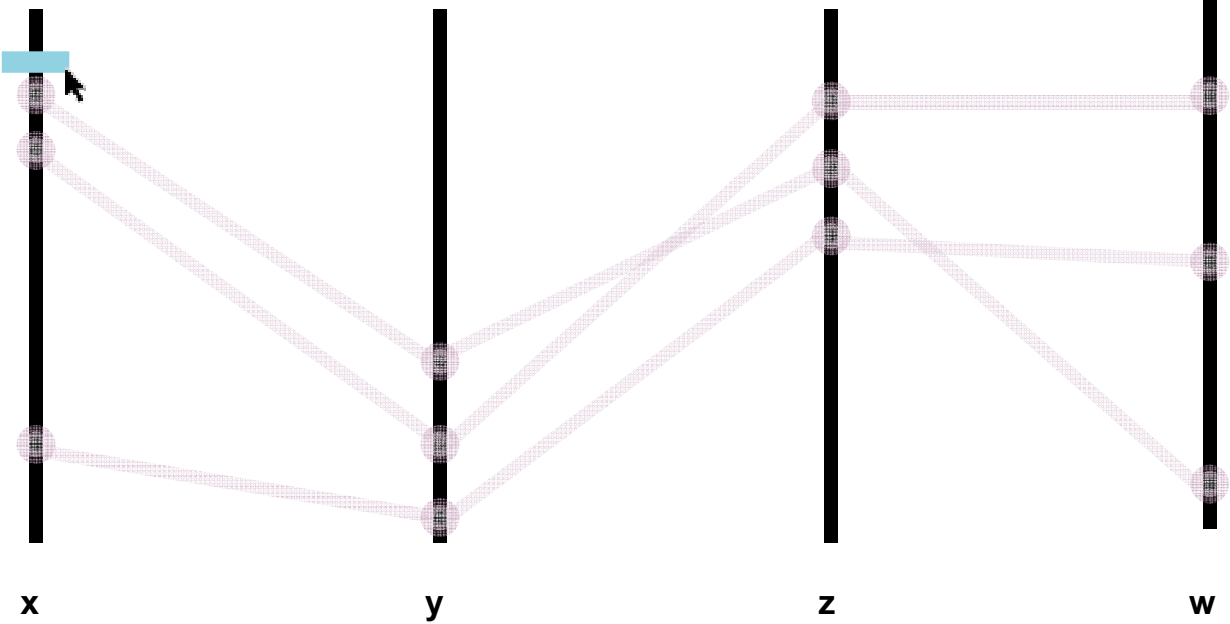
- Clutter!





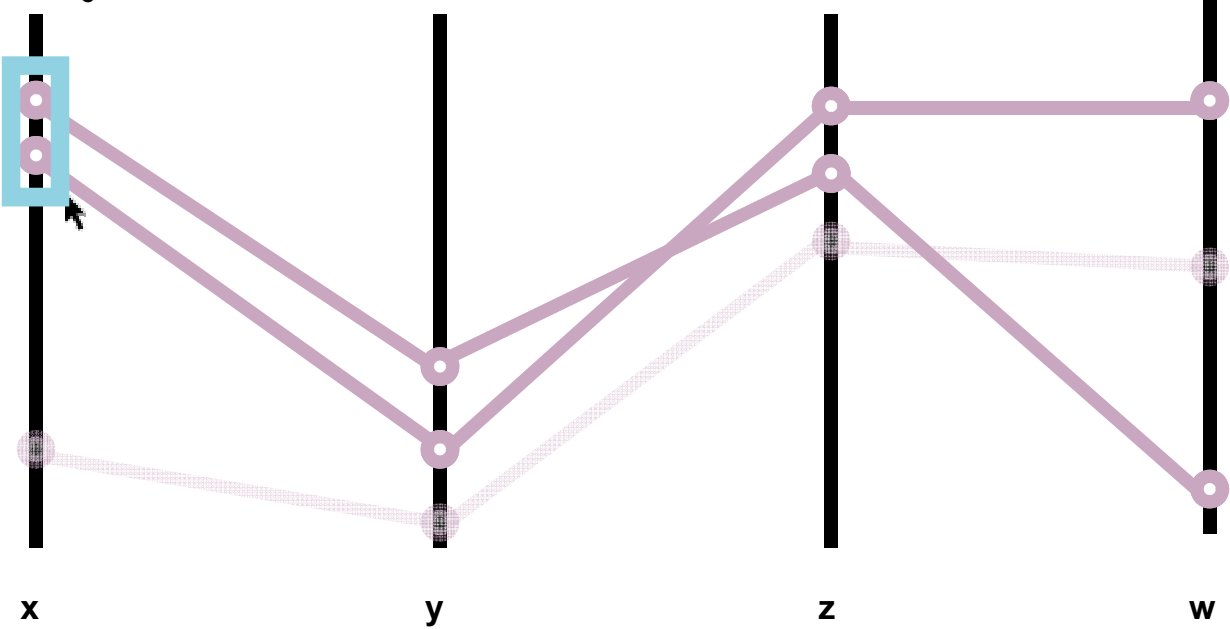
# Parallel Coordinates

Drag a selection box on axis to **brush** data



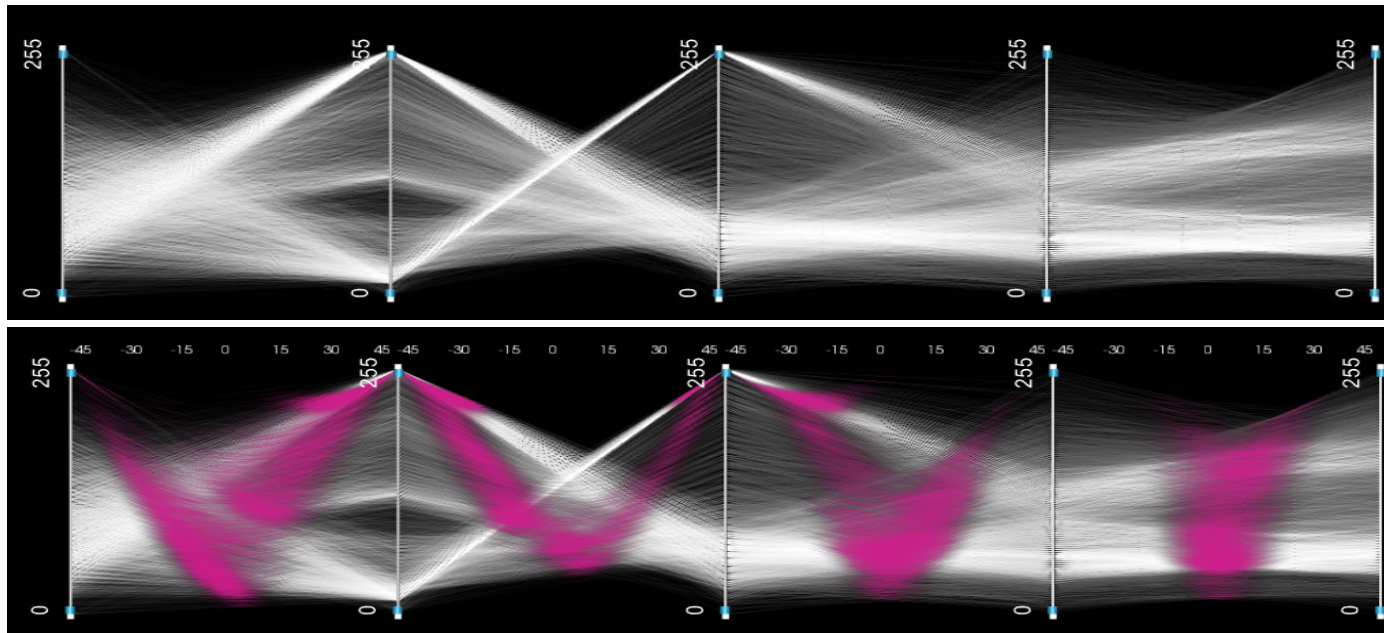
# Parallel Coordinates

Drag a selection box on axis to **brush** data



[Raidou, Eisemann, Breuwer, Eisemann, Vilanova - Vis 2015]

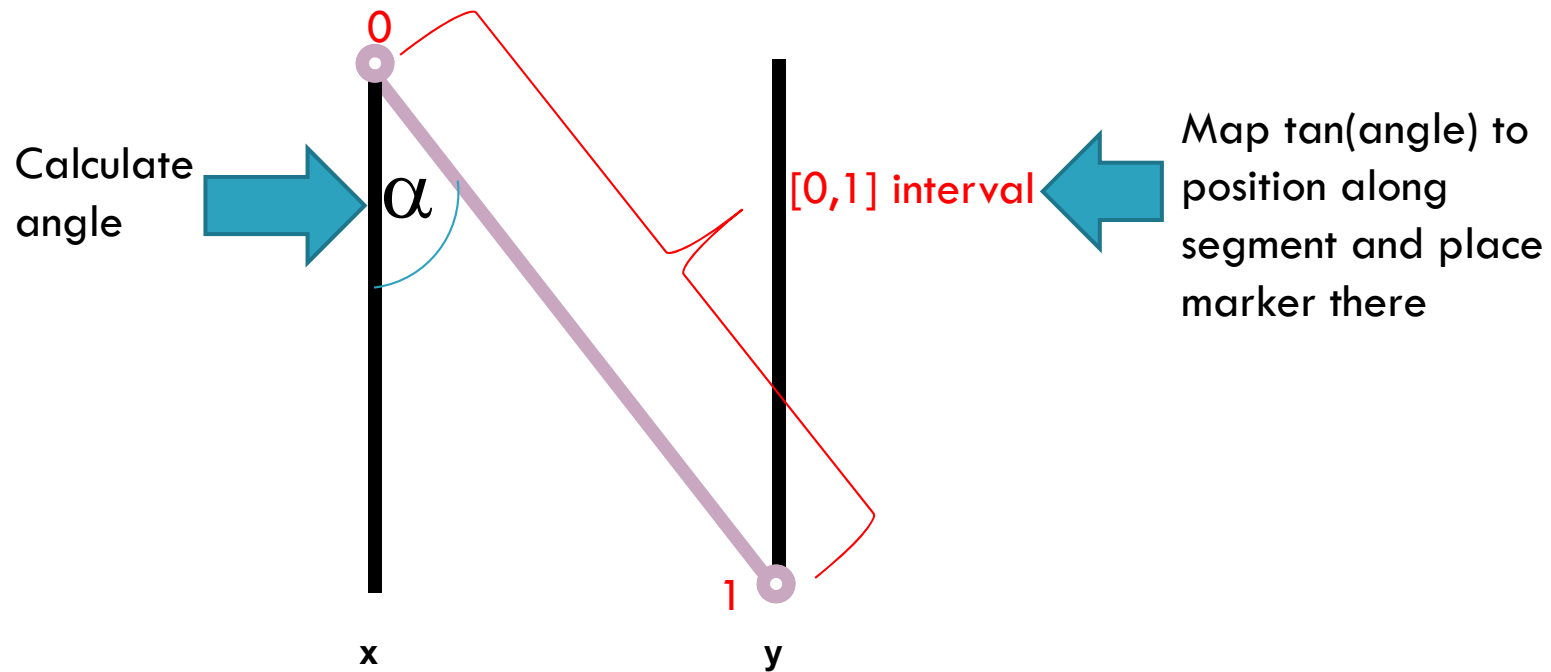
## 5-D Example



**DELFT  
DATA  
SCIENCE**

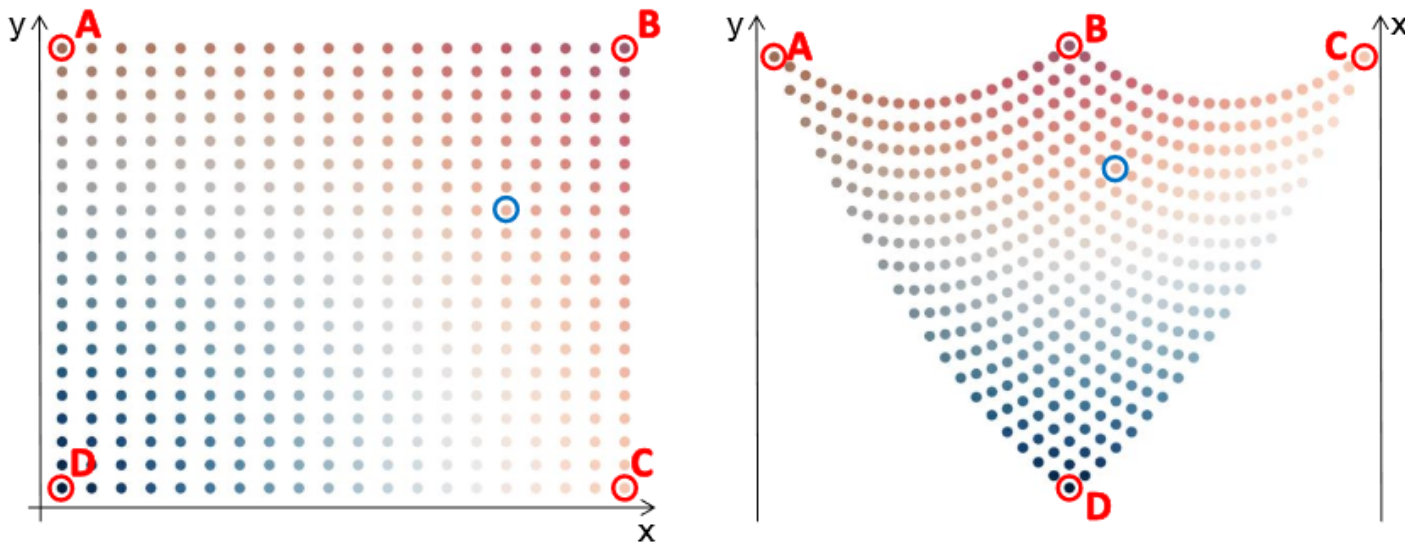
Koninklijk Instituut Van Ingenieurs

## Orientation-Enhanced Parallel Coordinate Plots



[Raidou, Eisemann, Breuwer, Eisemann, Vilanova - Vis 2015]

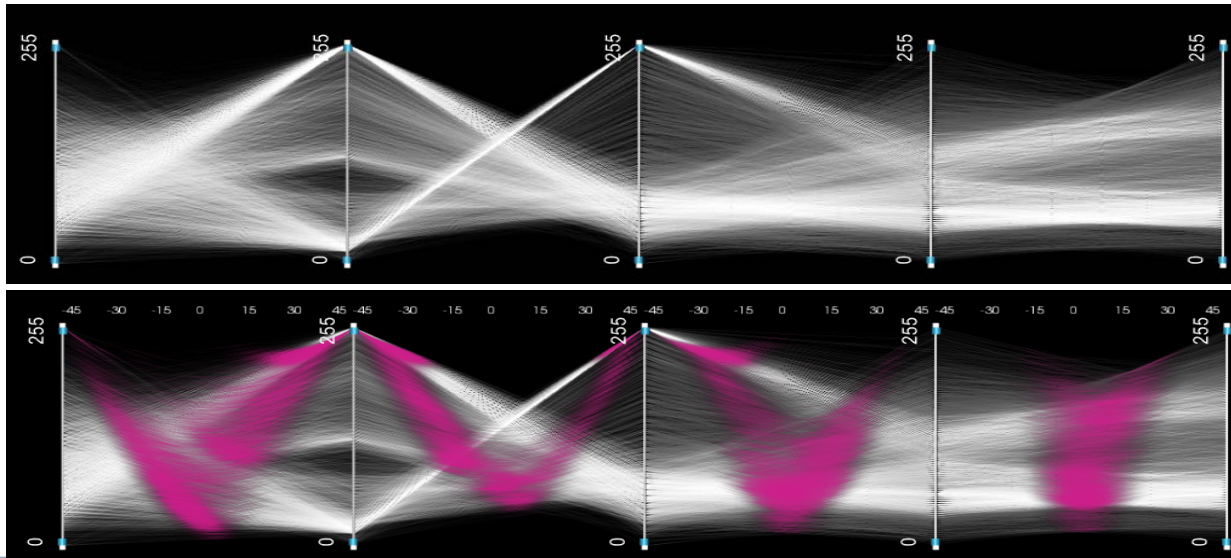
## Orientation-Enhanced Parallel Coordinate Plots



[Raidou, Eisemann, Breuwer, Eisemann, Vilanova - Vis 2015]

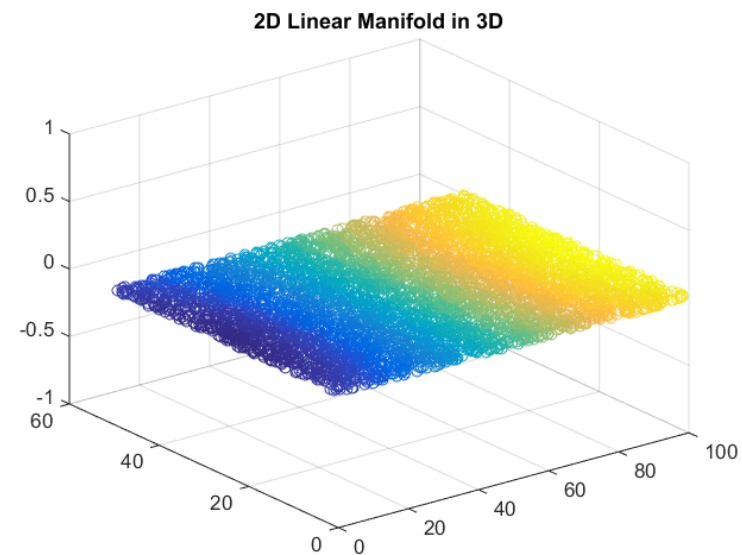
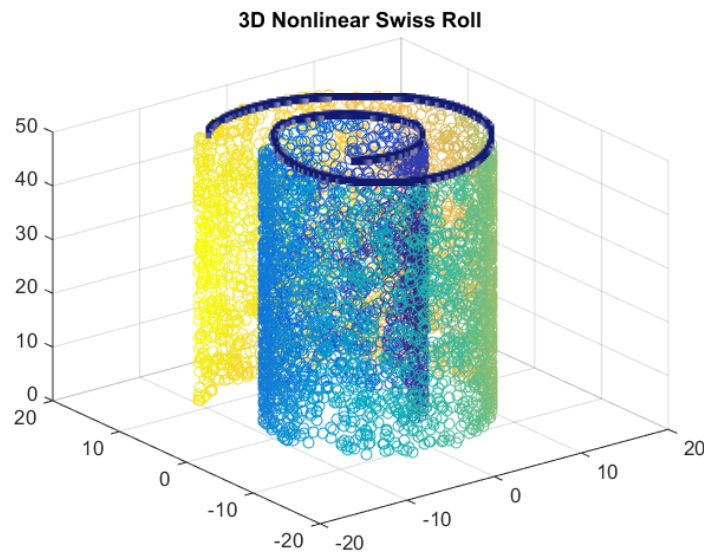
## 5-D Example

- Very effective to spot trends
- Supports interaction similar to the original PCP
- ...but fixed dimensionality



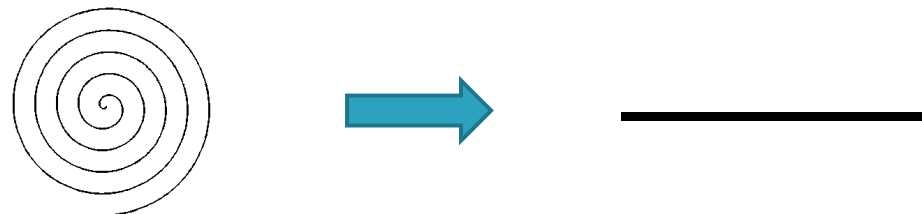
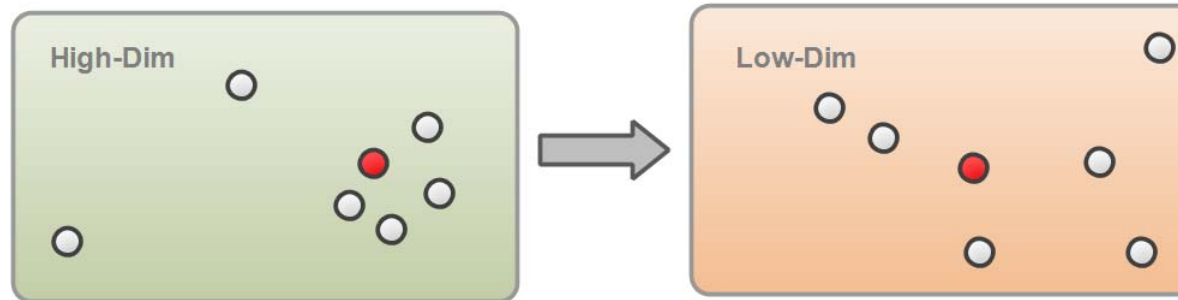
# High-Dimensional Spaces

- A high dimensional space does not imply high dimensionality



## Multi-dimensional Embedding

- Reduce dimensions but maintain neighbors/distances





## Example: Dimensionality Reduction

MNIST  
Dataset

0 0 ...

1 1 ...

2 2 ...

3 3 ...

4 4 ...

5 5 ...

6 6 ...

7 7 ...

8 8 ...

9 9 ...

100K samples  
with 4096 dim.



100K samples  
embedded in 2D

T-SNE: Van der Maaten and Hinton – Journal of Machine Learning 2008



## Challenges of Embedding

- Performance
  - Can be up to hours of calculation
- No Hierarchical information
  - Global embedding

Image Collection



Nature



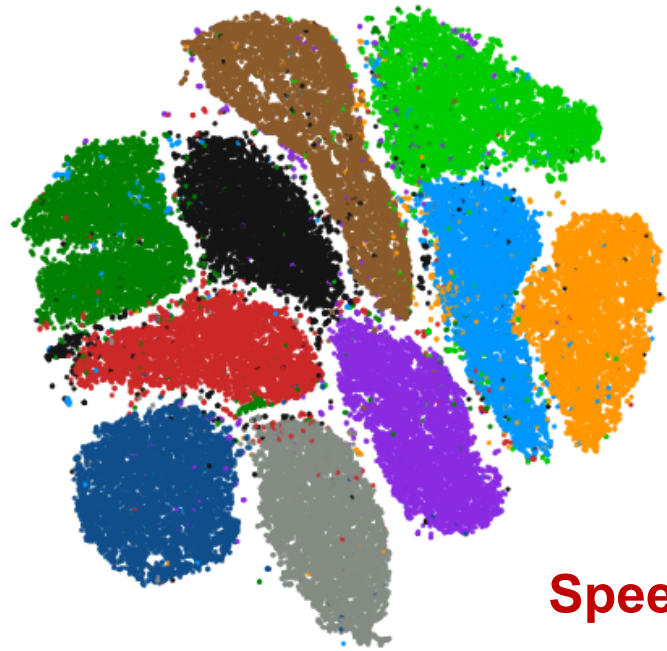
Man-made



## Challenges of Embedding

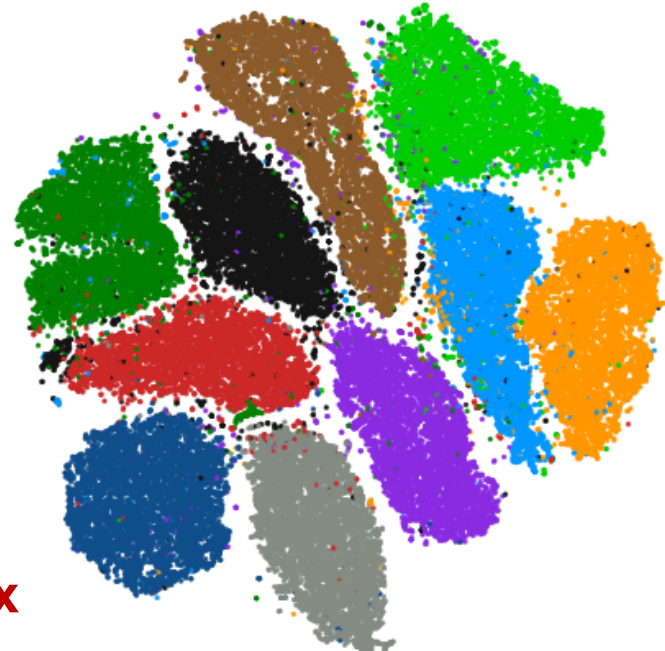
- Performance
  - Can be up to hours of calculation
- No Hierarchical information
  - Global embedding

## Extreme Acceleration



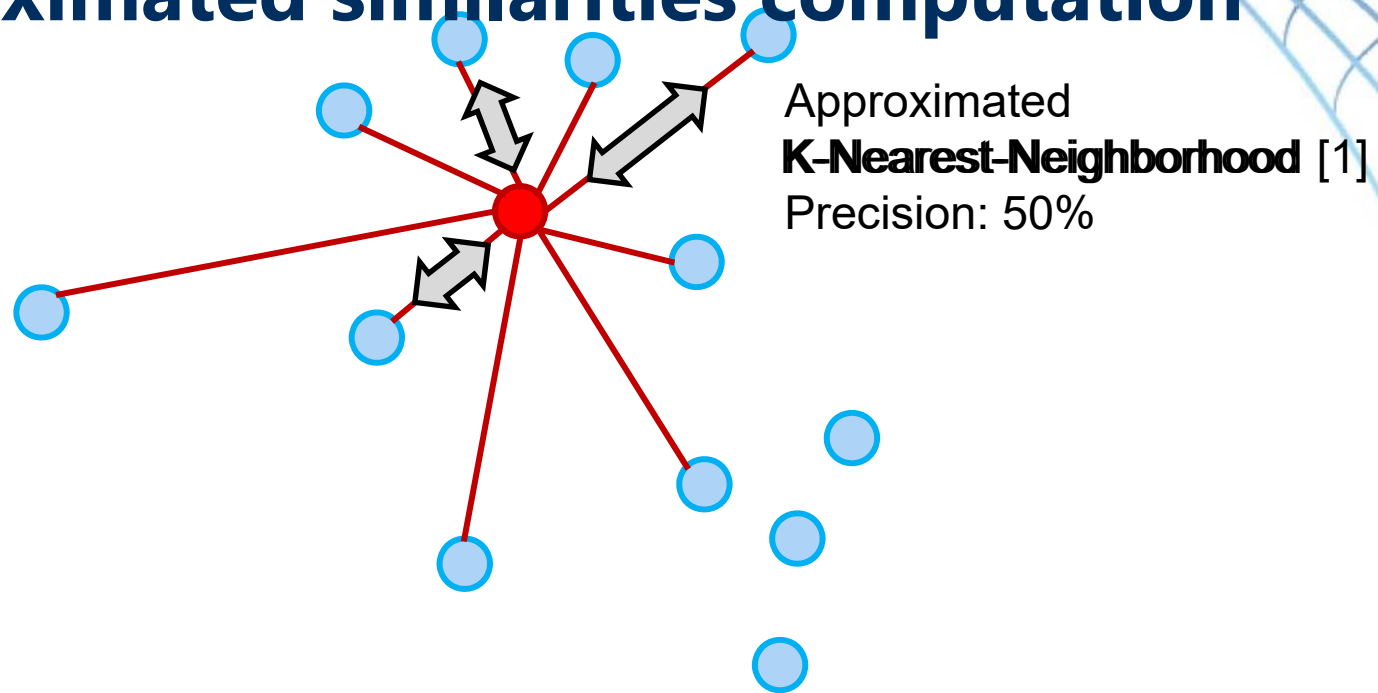
tSNE  
Time: 3191.8 s

**Speed up: 100x**

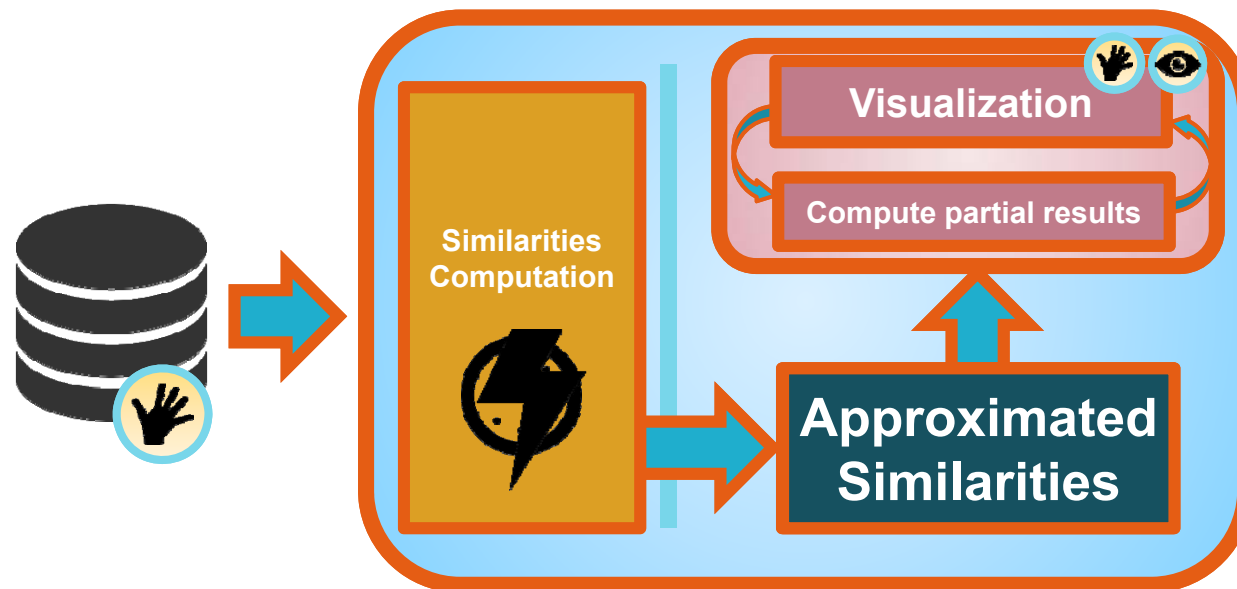


A-tSNE  
Time: 30.1 s

# Approximated similarities computation



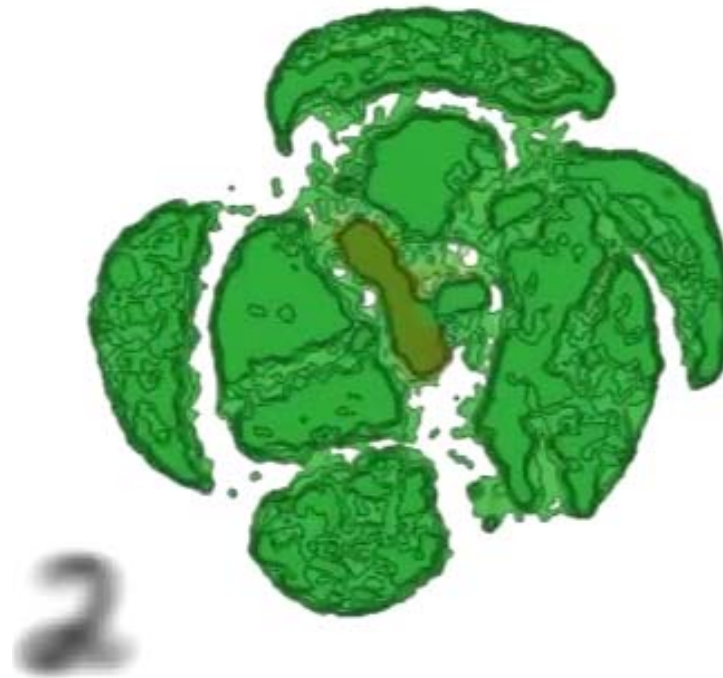
# Approximated tSNE



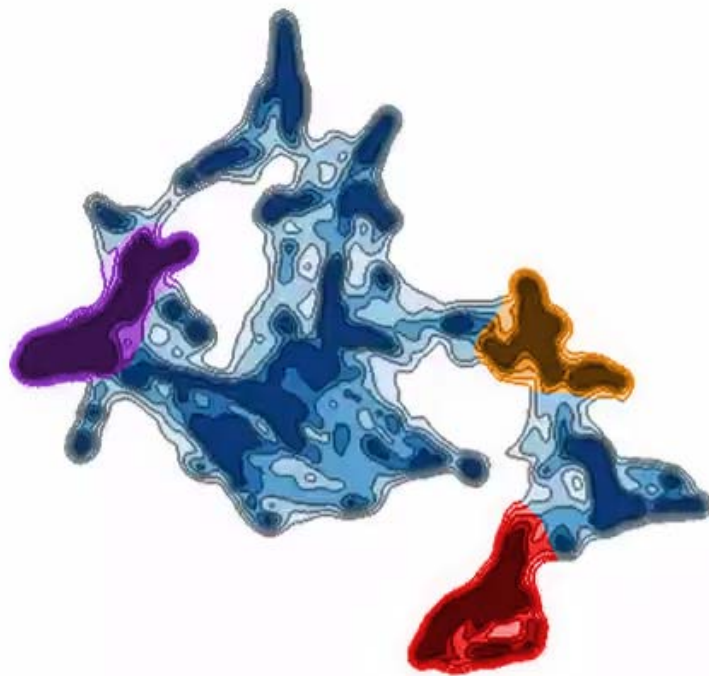
Approximated tSNE

## Steerability & Approximation

- Density-based visualization
  - Interaction support
  - Fast feedback and convergence



Preprocessing: 12 s (on purpose very low precision)



61164 data points (Voxels)

Sagittal



Coronal



Axial



3D Volume

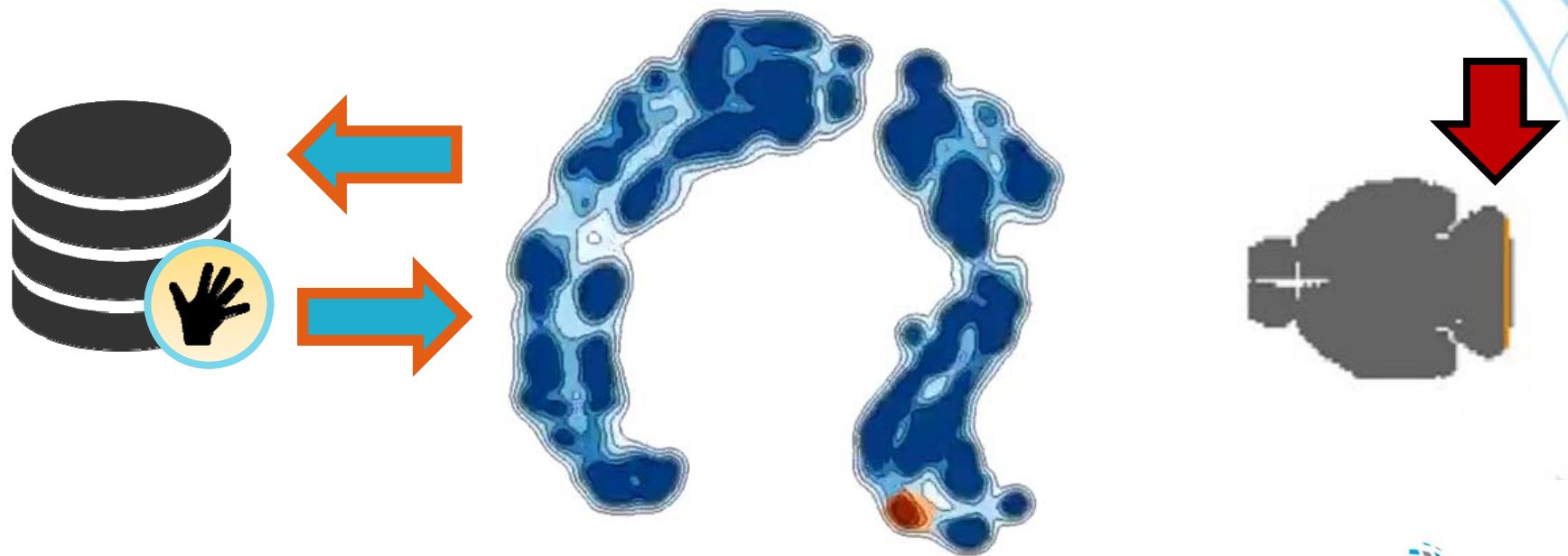


4345 dimensions (Gene expression)





## Case Study I : Gene expression

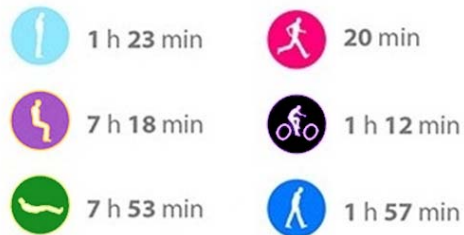


**Speed up: 250x**  
A-tSNE 50 seconds – tSNE 3 hours and 50 minutes



# Case Study II : High-dimensional data streams

Image courtesy of [www.activ8all.com](http://www.activ8all.com)



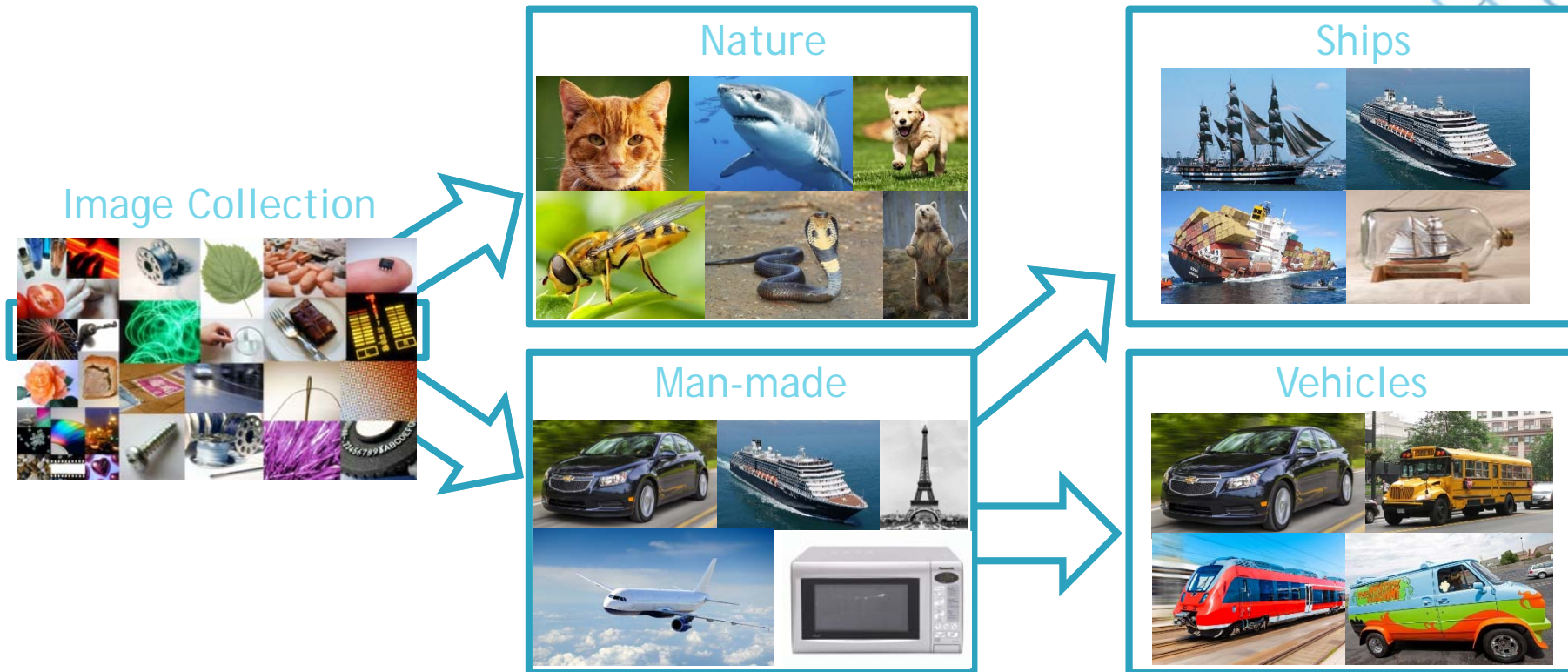
Chest - Ankle - Wrist  
52 Dimensions every 100 ms



## Challenges of Embedding

- Performance
  - Can be up to hours of calculation
- No Hierarchical information
  - Global embedding

# How to structure data hierarchically without knowing about the hierarchy?

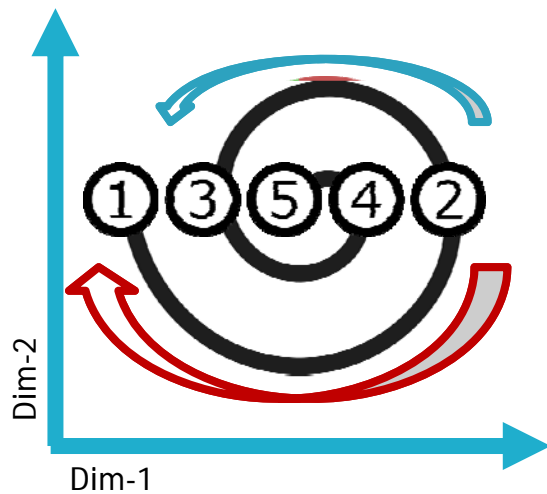


## General Idea

- We want to find good representatives of each class
- Then subsample the data



## Non-Linear DR with Landmarks



### Non linear

[Landmark-SNE, Landmark-ISOMAP]



### Hybrid techniques

[LSP, P-LSP, LAMP, LoCH, Pekalska]



# Hierarchical Stochastic Neighbor Embedding

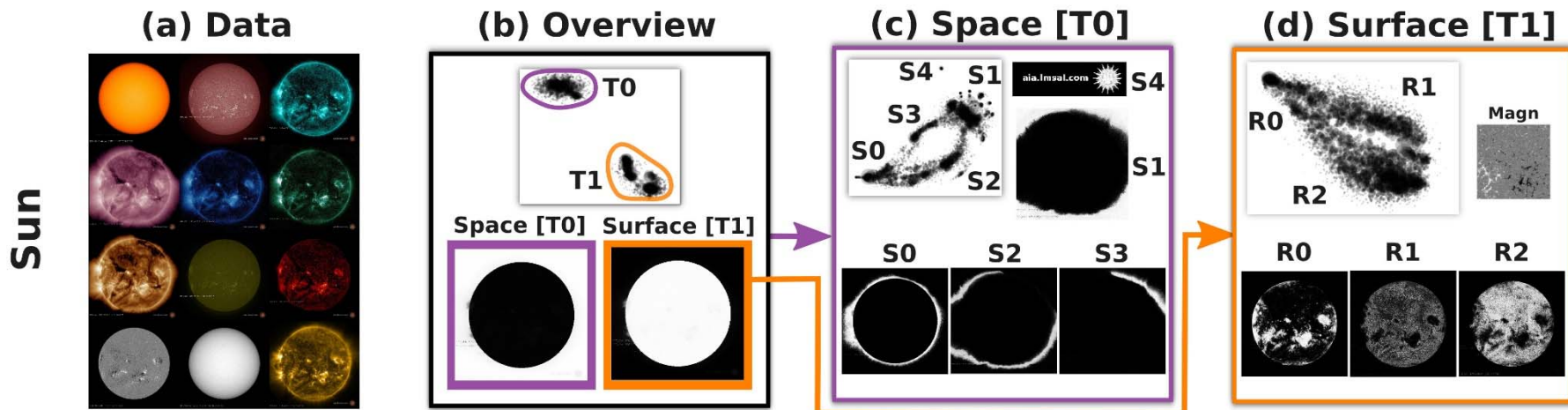
- Multiscale Dimensionality Reduction
  - Non-linear DR
  - Landmark based
- Hierarchical exploration of the data
  - Overview-first & Details-on-Demand
  - Filter & Drill-in



[Pezzotti, Hoelt, Leliveldt, Eisemann, Vilanova – EuroVis 2016]  
[Pezzotti, Leliveldt, van der Maaten, Hoelt, Eisemann, Vilanova – TVCG2016]

# Hierarchical Dimensionality Reduction

- Organize Data at Different Scales

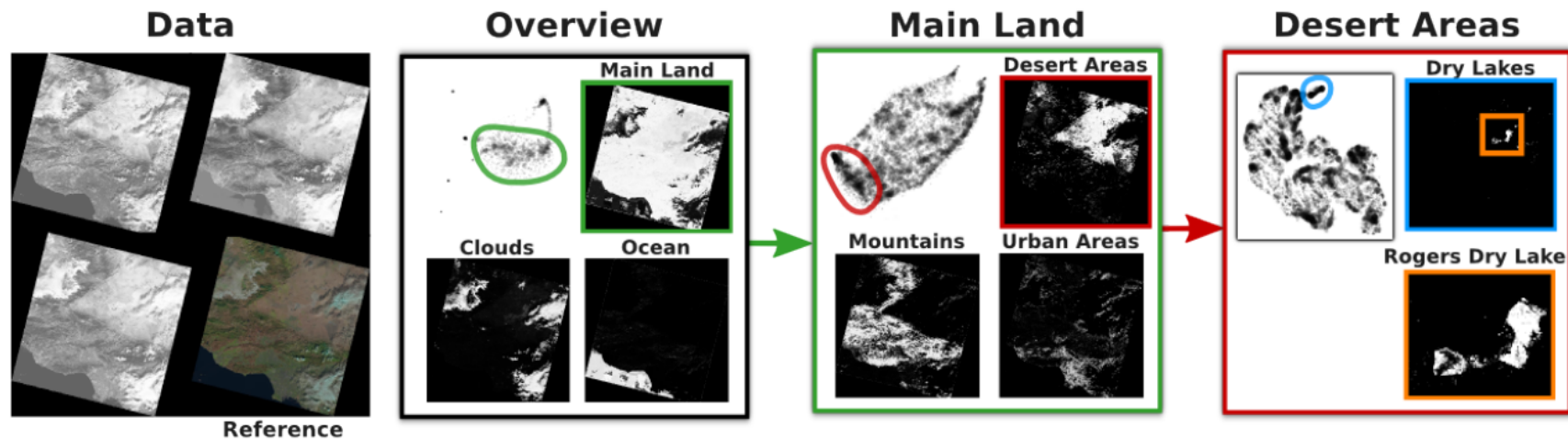




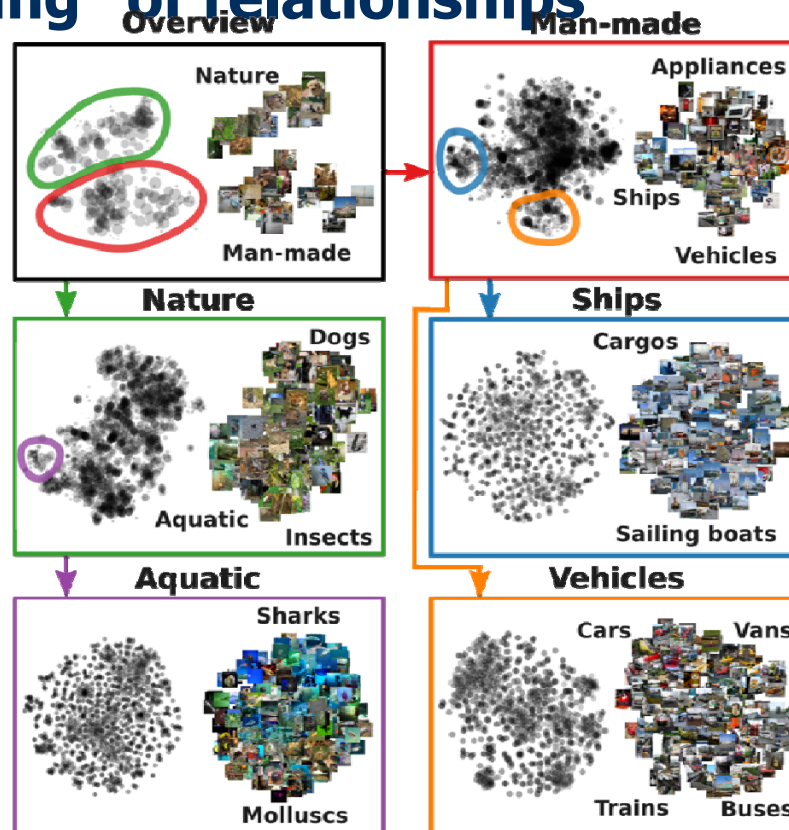
[Pezzotti, Hoelt, Leliveldt, Eisemann, Vilanova – EuroVis 2016]  
[Pezzotti, Leliveldt, van der Maaten, Hoelt, Eisemann, Vilanova – TVCG2016]

## Hierarchical Dimensionality Reduction

- Organize Data at Different Scales



# "Understanding" of relationships



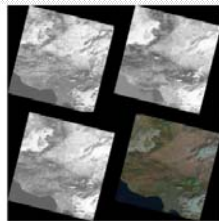
# Effective Data Visualization Requires



- **Large-Scale Rendering**



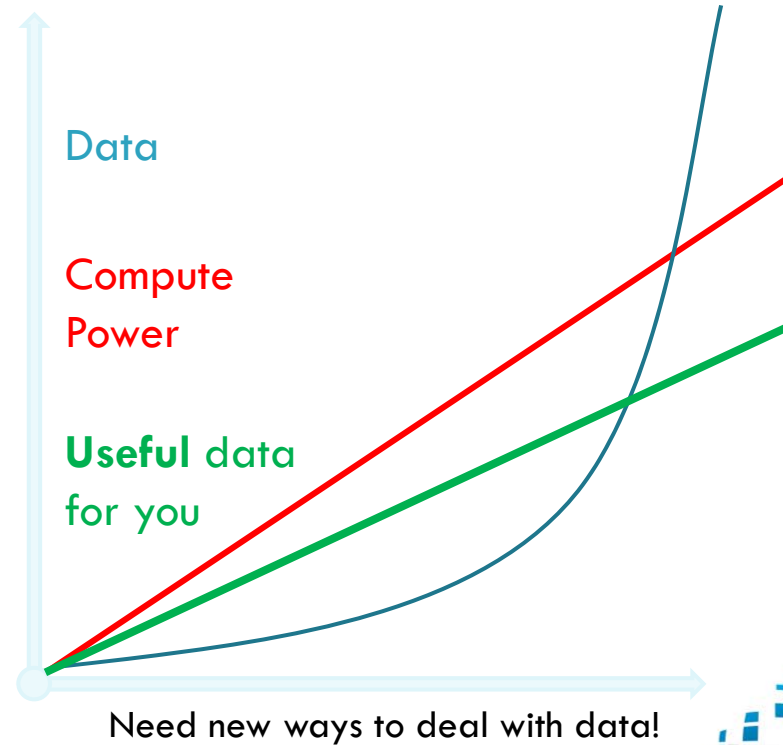
- **Visualization and Perception**



- **Data Analysis**

## Data Development

- **Processing**
- **Analysis**
- **Interaction**
- **Visualization**
- **Guidance**



## Large-Scale Rendering

- Ray Tracing
- Graphics Pipeline
- Specialized Methods for Different Data Types
  - Height-Field Data, Voxel Data, Data Management, Compression

# Visualization and Perception

- Realistic Rendering
- Perceptual Methods
- Visualization & Interface



## Data Analysis

- High-dimensional/Heterogeneous Data
- Dimensionality Reduction
- Visual Analytics



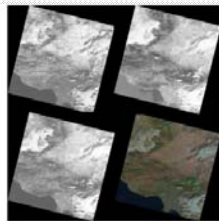
# Effective Data Visualization Requires



- **Large-Scale Rendering**

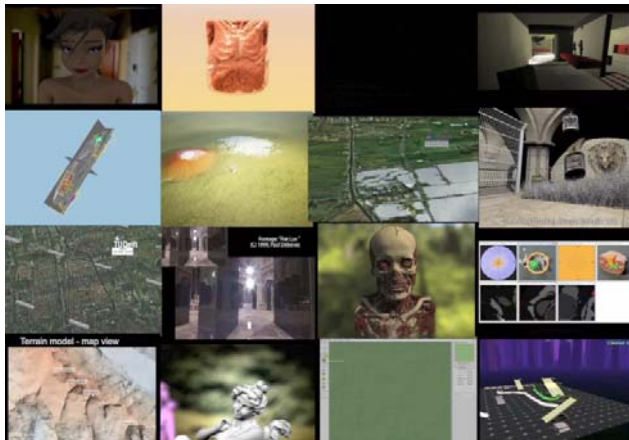


- **Visualization and Perception**



- **Data Analysis**





**Thank you very much  
for your attention!**



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